

**ECE 113A**  
**Professor Burke (15400) Section A**  
**Homework #5 Solutions and Grading Criteria**

A voltage  $V_A$  of 0.4144V is being applied to a step junction with n and p side dopings of  $N_A = 10^{15} \text{ cm}^{-3}$  and  $N_D = 10^{15} \text{ cm}^{-3}$ , respectively.  $n_i = 10^{10} \text{ cm}^{-3}$ .

*Under equilibrium conditions:*

$$\begin{aligned} p_{p,o} &= N_A = 10^{15} \text{ cm}^{-3} \\ n_{p,o} &= n_i^2/N_A = 10^5 \text{ cm}^{-3} \\ n_{n,o} &= N_D = 10^{15} \text{ cm}^{-3} \\ p_{n,o} &= n_i^2/N_D = 10^5 \text{ cm}^{-3} \end{aligned}$$

*For depletion region boundaries:*

$$\begin{aligned} \Delta n_p(-x_p) &= (n_i^2/N_A)(\exp[qV_A/kT] - 1) \\ &= (10^5 \text{ cm}^{-3})(\exp[0.4144V/0.259V] - 1) \\ &= 8.92 \times 10^{11} \text{ cm}^{-3} \\ \Delta p_n(x_n) &= (n_i^2/N_D)(\exp[qV_A/kT] - 1) \\ &= (10^5 \text{ cm}^{-3})(\exp[0.4144V/0.259V] - 1) \\ &= 8.92 \times 10^{11} \text{ cm}^{-3} \\ n_p &= n_{p,o} + \Delta n_p(-x_p) \exp[-x''/L_N] \\ p_n &= p_{n,o} + \Delta p_n(x_n) \exp[-x'/L_P] \end{aligned}$$

- 1) Calculate p on the p side at the interface. **(6 pts)**

*Since  $\Delta n_p(-x_p) \ll p_{p,o}$ , low-level injection prevails. Therefore, the majority carrier concentration is approximately unchanged.*

$$p_p = p_{p,o} = 10^{15} \text{ cm}^{-3} \quad (\text{exact answer required or no credit})$$

- 2) Calculate p on the p side 10 diffusion lengths away from the interface. **(6 pts)**

$$p_p = p_{p,o} = 10^{15} \text{ cm}^{-3} \quad (\text{exact answer required or no credit})$$

- 3) Calculate p on the p side 20 diffusion lengths away from the interface. **(6 pts)**

$$p_p = p_{p,o} = 10^{15} \text{ cm}^{-3} \quad (\text{exact answer required or no credit})$$

- 4) Calculate p on the p side 30 diffusion lengths away from the interface. **(6 pts)**

$$p_p = p_{p,o} = 10^{15} \text{ cm}^{-3} \quad (\text{exact answer required or no credit})$$

- 5) Calculate n on the p side at the interface. **(6 pts)**

$$\begin{aligned} n_p &= n_{p,o} + \Delta n_p(-x_p) \exp[0] \\ &= 10^5 \text{ cm}^{-3} + 8.92 \times 10^{11} \text{ cm}^{-3} \\ &= 8.92 \times 10^{11} \text{ cm}^{-3} \quad (8-10 \times 10^{11} \text{ cm}^{-3} \text{ for credit}) \end{aligned}$$

- 6) Calculate n on the p side 10 diffusion lengths away from the interface. **(6 pts)**

$$\begin{aligned} n_p &= n_{p,o} + \Delta n_p(-x_p) \exp[-10] \\ &= 10^5 \text{ cm}^{-3} + 8.92 \times 10^{11} \text{ cm}^{-3} \exp[-10] \\ &= 4.06 \times 10^7 \text{ cm}^{-3} \quad (3-5 \times 10^7 \text{ cm}^{-3} \text{ for credit}) \end{aligned}$$

- 7) Calculate n on the p side 20 diffusion lengths away from the interface. **(6 pts)**

$$\begin{aligned} n_p &= n_{p,o} + \Delta n_p(-x_p) \exp[-20] \\ &= 10^5 \text{ cm}^{-3} + 8.92 \times 10^{11} \text{ cm}^{-3} \exp[-20] \\ &= 1.02 \times 10^5 \text{ cm}^{-3} \quad (0.8-1.2 \times 10^5 \text{ cm}^{-3} \text{ for credit}) \end{aligned}$$

- 8) Calculate n on the p side 30 diffusion lengths away from the interface. **(6 pts)**

$$n_p = n_{p,o} + \Delta n_p(-x_p) \exp[-30]$$

$$= 10^5 \text{ cm}^{-3} + 8.92 \times 10^{11} \text{ cm}^{-3} \exp[-30]$$

$$= 10^5 \text{ cm}^{-3} \quad (\text{exact answer required or no credit})$$

- 9) Calculate p on the n side at the interface. (6 pts)

$$p_n = p_{n,o} + \Delta p_n(x_n) \exp[0]$$

$$= 10^5 \text{ cm}^{-3} + 8.92 \times 10^{11} \text{ cm}^{-3}$$

$$= 8.92 \times 10^{11} \text{ cm}^{-3} \quad (8 \cdot 10 \times 10^{11} \text{ cm}^{-3} \text{ for credit})$$

- 10) Calculate p on the n side 10 diffusion lengths away from the interface. (6 pts)

$$p_n = p_{n,o} + \Delta p_n(x_n) \exp[-10]$$

$$= 10^5 \text{ cm}^{-3} + 8.92 \times 10^{11} \text{ cm}^{-3} \exp[-10]$$

$$= 4.06 \times 10^7 \text{ cm}^{-3} \quad (3 \cdot 5 \times 10^7 \text{ cm}^{-3} \text{ for credit})$$

- 11) Calculate p on the n side 20 diffusion lengths away from the interface. (6 pts)

$$p_n = p_{n,o} + \Delta p_n(x_n) \exp[-20]$$

$$= 10^5 \text{ cm}^{-3} + 8.92 \times 10^{11} \text{ cm}^{-3} \exp[-20]$$

$$= 1.02 \times 10^5 \text{ cm}^{-3} \quad (0.8 \cdot 1.2 \times 10^5 \text{ cm}^{-3} \text{ for credit})$$

- 12) Calculate p on the n side 30 diffusion lengths away from the interface. (6 pts)

$$p_n = p_{n,o} + \Delta p_n(x_n) \exp[-30]$$

$$= 10^5 \text{ cm}^{-3} + 8.92 \times 10^{11} \text{ cm}^{-3} \exp[-30]$$

$$= 10^5 \text{ cm}^{-3} \quad (\text{exact answer required or no credit})$$

- 13) Calculate n on the n side at the interface. (6 pts)

Since  $\Delta p_n(x_n) \ll n_{n,o}$ , low-level injection prevails. Therefore, the majority carrier concentration is approximately unchanged.

$$n_n = n_{n,o} = 10^{15} \text{ cm}^{-3} \quad (\text{exact answer required or no credit})$$

- 14) Calculate n on the n side 10 diffusion lengths away from the interface. (6 pts)

$$n_n = n_{n,o} = 10^{15} \text{ cm}^{-3} \quad (\text{exact answer required or no credit})$$

- 15) Calculate n on the n side 20 diffusion lengths away from the interface. (6 pts)

$$n_n = n_{n,o} = 10^{15} \text{ cm}^{-3} \quad (\text{exact answer required or no credit})$$

- 16) Calculate n on the n side 30 diffusion lengths away from the interface. (6 pts)

$$n_n = n_{n,o} = 10^{15} \text{ cm}^{-3} \quad (\text{exact answer required or no credit})$$

- 17) Make a dimensioned log(p or n) versus x sketch of both the majority and minority carrier concentrations in the quasineutral regions of the device (4 pts)

(If any answer in #1-16 are wrong, no points for this section. No partial credit.)

