

1	2	3	4	5	Total
/5	/5	/5	/5	/5	/45

**FIVE PROBLEMS TOTAL. DO NOT ASSUME YOU WILL GET PARTIAL CREDIT.**

**DO NOT BEGIN THE EXAM  
UNTIL YOU ARE TOLD TO  
DO SO.**

**PROBLEM ONE: (5 points)**

For a piece of Si at 300 K, there is no doping, in other words it is *intrinsic*. Find the resistivity to within 10%. (Hint: find the density of electrons and mobility first, then calculate the resistivity.)

$n = p = n_i$  since this is an intrinsic material with no doping

$$\mu_n = 1358 \text{ cm}^2/\text{V-s}$$

$$\mu_p = 461 \text{ cm}^2/\text{V-s}$$

$$\rho = 1/[q(\mu_n n + \mu_p p)]$$

$$= 1/[q(\mu_n n_i + \mu_p n_i)]$$

$$= 1/[q n_i (\mu_n + \mu_p)]$$

$$= 1/[1.6 \times 10^{-19} \text{ C}](10^{10} \text{ cm}^{-3})(1358 \text{ cm}^2/\text{V-s} + 461 \text{ cm}^2/\text{V-s})]$$

$$= 3.43 \times 10^{11} \text{ } \mu\Omega\text{-cm}$$

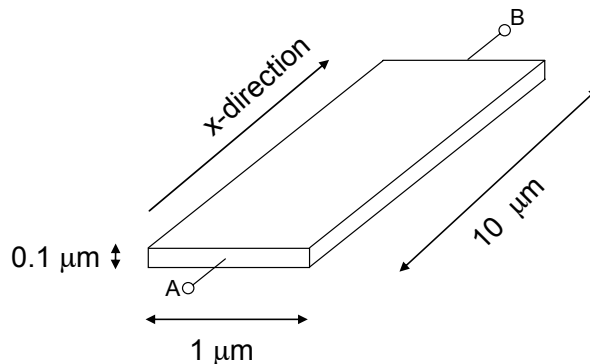
**Acceptable Range:  $3.1\text{-}3.7 \times 10^{11} \text{ } \mu\Omega\text{-cm}$**

**Grading Criteria:**

**1 point if  $p$ ,  $n$ ,  $\mu_n$ , and  $\mu_p$  correct**

**1 point for correct  $\rho$  equation**

**3 points for correct answer within range**

**PROBLEM TWO: (5 points)**

Consider the piece of Si above.

At  $x=0$  (which is the “A” end), the electron density is  $10^{14} \text{ cm}^{-3}$ .

At  $x=10 \mu\text{m}$  (which is the “B” end), the electron density is  $0 \text{ cm}^{-3}$ .

The electron density varies linearly with  $x$  in between.

Assume the electric field is zero everywhere inside.

Approximate  $D_N=35 \text{ cm}^2/\text{s}$ .

Calculate the electron current density and current in the  $x$ -direction.

Make sure to get the sign correct.

If you say there is positive current, you mean current flows in the direction of the arrow in the figure.

(Hint: Is the current due to drift or diffusion?)

*(Current is due to diffusion since the electric field is equal to zero)*

$$\begin{aligned} J_N &= qD_N \frac{dn}{dx} \\ &= (1.6 \times 10^{-19} \text{ C})(35 \text{ cm}^2/\text{s})(-10^{14} \text{ cm}^{-3}) / (10 \mu\text{m} \times 10^{-4} \text{ cm}/\mu\text{m}) \\ &= -.56 \text{ A-cm}^{-2} \end{aligned}$$

*Acceptable Range: 0.50 - 0.60 a-cm<sup>-2</sup>*

$$\begin{aligned} I &= JA \\ &= (-.56 \text{ A-cm}^{-2})(1 \mu\text{m} \times 10^{-4} \text{ cm}/\mu\text{m})(0.1 \mu\text{m} \times 10^{-4} \text{ cm}/\mu\text{m}) \\ &= -5.6 \times 10^{-10} \text{ A} \end{aligned}$$

*Acceptable Range: 0.50 – 0.60 nA*

**Grading Criteria:**

*1 point for correct current density equation*

*1 point for plugging in the numbers correctly into the current density equation, including the minus sign*

*1 point for correct current density within the given range*

*1 point for correct current equation*

*1 point for correct current equation within range*

**PROBLEM THREE: (5 points)**

Consider an n-n junction with an abrupt doping profile. The doping level on the left hand side is  $10^{15} \text{ cm}^{-3}$ , and on the right hand side it is  $5 \times 10^{17} \text{ cm}^{-3}$ . Assume equilibrium conditions below.

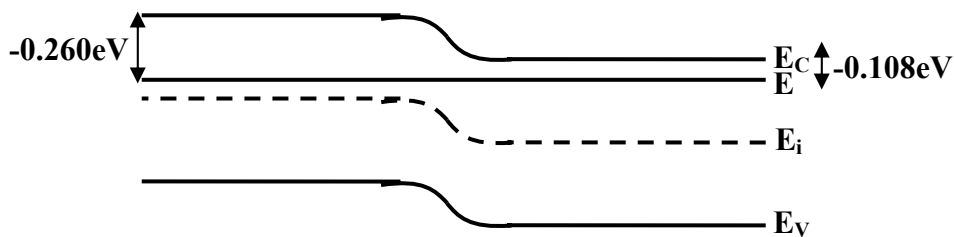
- a) Draw the energy band diagram for the junction. Make sure you calculate  $E_F - E_C$  on both sides of the junction and label it on the diagram.

$$E_F - E_C = kT \ln(n/N_C)$$

$$N_C = 2.51 \times 10^{19} \text{ cm}^{-3} (m_n^*/m_o^*)^{3/2} = 3.22 \times 10^{19} \text{ cm}^{-3}$$

$$(E_F - E_C)_{\text{left}} = (0.0259 \text{ eV}) \ln(10^{15} \text{ cm}^{-3} / 3.22 \times 10^{19} \text{ cm}^{-3}) = -0.269 \text{ eV}$$

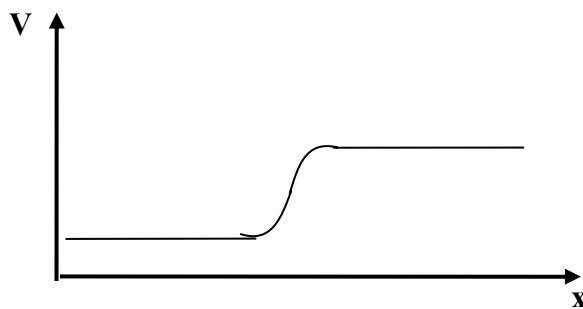
$$(E_F - E_C)_{\text{right}} = (0.0259 \text{ eV}) \ln(5 \times 10^{17} \text{ cm}^{-3} / 3.22 \times 10^{19} \text{ cm}^{-3}) = -0.108 \text{ eV}$$

**Grading Criteria:**

*1 point for getting both  $E_F - E_C$  correct*

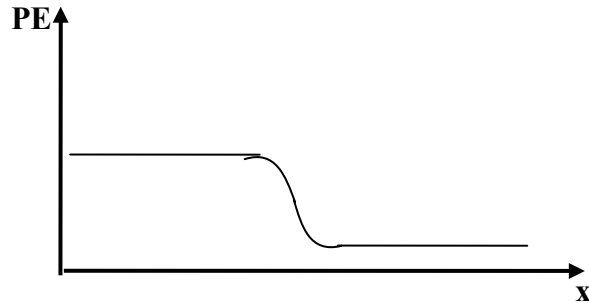
*1 point for correct band diagram*

- b) Sketch the electrostatic potential (voltage) vs. position.

**Grading Criteria:**

*1 point for getting correct diagram*

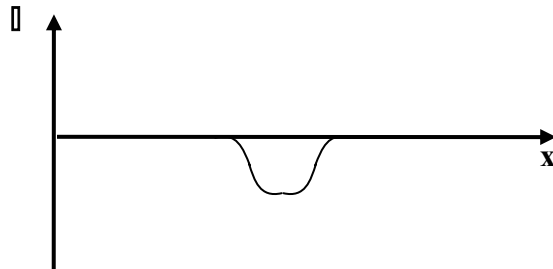
c) Sketch the potential energy vs. position.



**Grading Criteria:**

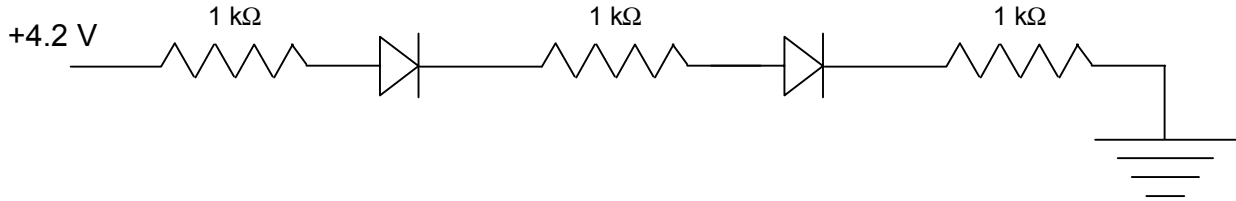
**1 point for getting correct diagram**

d) Sketch the electric field vs. position.



**Grading Criteria:**

**1 point for getting correct diagram**

**PROBLEM FOUR: (5 points)**

How much current is flowing in this circuit?

$$V_{diode} = 0.6V$$

$$\text{Acceptable Range: } 0.5V - 0.7V$$

$$I = V/R$$

$$= (4.2V - 2(0.6V))/3000\Omega$$

$$= 1mA$$

$$\text{Acceptable Range: } 0.8-1.2mA$$

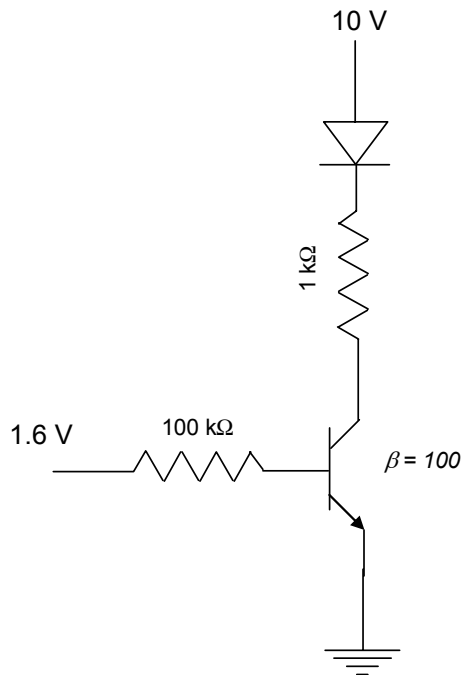
**Grading Criteria:**

*1 point for correct voltage for diode within given range*

*4 points for correct answer within given range*

12-07-2004

Sec.B: Peter Burke 4 to 6 pm

**PROBLEM FIVE: (5 points)**Find  $V_C$  for this circuit.

$$V_{diode} = 0.6V$$

$$V_{BE} = V_B - V_E = 0.6V$$

$$V_E = 0V$$

$$V_B = 0.6V$$

$$I_B = (1.6V - V_B)/100000\Omega = (1.6V - 0.6V)/100000\Omega = 10\mu A$$

$$I_C = \beta I_B = (100)(10\mu A) = 1mA$$

$$I_C = (10V - 0.6V - V_C)/1000\Omega$$

$$(10V - 0.6V - V_C)/1000\Omega = 1mA$$

$$9.4V - V_C = 1V$$

$$V_C = 8.4V$$

$$\text{Acceptable Range: } 8.2V - 8.6V$$

**Grading Criteria:**

1 point for correct  $V_{diode}$  within range 0.5V-0.7V

1 point for correct  $V_{BE}$  value within range 0.6V-0.7V

1 point for correct collector versus base current equation

2 points for correct answer within range (but only one if you calculate  $V_C$  correctly but mislabel it)