

PROBLEM ONE: (20 points)

A) (10 points) What is the relationship between the resistance R and resistivity ρ of a wire of diameter d and length L ?

$$R = \frac{L}{A} \rho = \frac{L}{\left(\frac{d}{2}\right)^2 \pi} \rho$$

B) (10 points) Calculate the resistance of a copper wire that is 100 feet long and 3 mm in diameter. Express your answer in units of Ω . Get your answer right to within 10%. Assume the resistivity of copper is $10 \mu\Omega\text{-cm}$.

$$R = \frac{100 \text{ feet}}{\left(\frac{3 \text{ mm}}{2}\right)^2 \pi} 10 \mu\Omega\text{-cm}$$

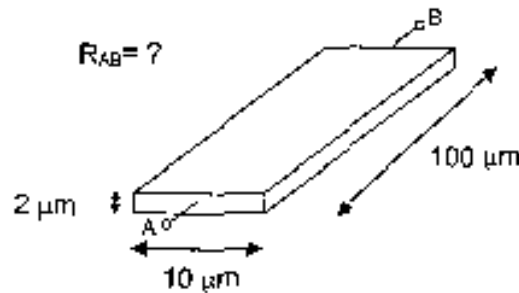
Convert to MKSA

$$= \frac{100 \times 12 \times 2.54 \times 10^{-2} \text{ m}}{\left(\frac{3 \times 10^{-3} \text{ m}}{2}\right)^2 \pi} 10 \times 10^{-6} \times 10^{-2} \Omega\text{-m}$$

$$= 10^2 \times 2 + 1 - 6 - 2 \times 6 \quad \frac{12 \cdot 2.54 \cdot 4}{9 \pi} \Omega$$

$$= 10^{-1} \times 4.31 \Omega = 0.43 \Omega$$

PROBLEM TWO: (40 points)



A new semiconductor is discovered. Scientists find that the mobility of electrons is approximately 20,000 cm²/V-s, and that the effective mass of electrons is equal to the free electron mass.

A) (20 points)

The material is doped n-type so that $n = 10^{18} \text{ cm}^{-3}$.

Find the resistivity ρ of the semiconductor to within 10% in units of $\mu\Omega\text{-cm}$.

$$\rho = \frac{1}{q\mu n} = \frac{1}{1.6 \times 10^{-19} \text{ C} \cdot 20,000 \text{ cm}^2/\text{V-s} \cdot 10^{18} \text{ cm}^{-3}}$$

$$= \frac{1}{1.6 \times 10^{-19} \text{ C} \cdot 2 \cdot 10^4 \cdot 10^{-4} \text{ m}^2/\text{V-s} \cdot 10^{18} \cdot 10^6 \text{ m}^{-3}}$$

$$= \frac{1}{1.6} \cdot \frac{1}{2} \cdot 10^{-19+4-4+18-6} = 0.31 \cdot 10^{-5} \Omega\text{-m} = 3.1 \cdot 10^{-6} \Omega\text{-m}$$

B) (20 points)

For this hypothetical semiconductor, what is the average time between scattering events τ ?

$$\mu = \frac{q\tau}{m} \Rightarrow \tau = \frac{m\mu}{q} = \frac{9.1 \cdot 10^{-31} \text{ kg} \cdot 2 \cdot 10^4 \cdot 10^{-4} \text{ m}^2/\text{V-s}}{1.6 \cdot 10^{-19} \text{ C}}$$

$$= 11.39 \text{ ps}$$

$= 3.1 \cdot 10^{-6} \Omega\text{-m}$
 $= 3.1 \cdot 10^{-2} \mu\Omega\text{-cm}$

PROBLEM THREE (40 points):

The two figures below represent two different Si wafers at 300 K.

E_S _____
 E_F

E_V _____

Figure 1

E_C _____
 E_F

E_V _____

Figure 2

A) (10 points) For figure 1, which is larger, n or p?

n

B) (10 points) For figure 2, which is larger, n or p?

n

C) (10 points) Is n for figure 1 larger than n for figure 2?

Yes

D) (10 points) Is p for figure 1 larger than p for figure 2?

No.