EECS 170A Professor Burke Section B Homework #3 Solutions and Grading Criteria

1) Answer a-d for the figure shown below:

- a) Do the equilibrium conditions prevail? How do you know? (5 pts total) Yes because E_F is constant. (no points if reason not given)
- b) Sketch the electrostatic potential (V) inside the semiconductor as a function of x. (5 pts total)



Graph must be linear with a positive slope between x = 0 and x=L/2 and negative slope between x = L/2 and x = L. It does not matter where the graph is centered vertically as long as it has the correct shape.

c) Sketch the electric field () inside the semiconductor as a function of x. (5 pts total)



Graph must be a negative constant between x = 0 and x=L/2 and positive constant between x = L/2 and x = L.

d) Roughly sketch n and p versus x. (10 pts total)



n and *p* graphs must be centered around n_i for credit. Graphs should be mirrors of each other. *n* graph should look like V graph. N and *p* graphs are 5 pts each.

2) Answer a-d for the figure shown below:

a) Do the equilibrium conditions prevail? How do you know? (5 pts total) Yes because E_F is constant. (no points if reason not given)

b) Sketch the electrostatic potential (V) inside the semiconductor as a function of x. (5 pts total)



Graph must have correct shape. Center of graph should be at L/2. It does not matter where the graph is centered vertically as long as it has the correct shape.

c) Sketch the electric field () inside the semiconductor as a function of x. (5 pts total)

Graph must be positive, have correct shape, and be centered around L/2.



d) Roughly sketch n and p versus x. (10 pts total)



n and *p* graphs must be centered around n_i for credit. Graphs should be mirrors of each other. *n* graph should look like *V* graph. *n* and *p* graphs are 5 pts each. If *n* and *p* cross n_i then only 3 pts each.

- 3) Answer a-d for the figure shown below:
 - a) Do the equilibrium conditions prevail? How do you know? (5 pts total) Yes because E_F is constant. (no points if reason not given)
 - b) Sketch the electrostatic potential (V) inside the semiconductor as a function of x. (5 pts total)



Graph must have correct shape. Slope changes occur at L/3 and 2L/3. It does not matter where the graph is centered vertically as long as it has the correct shape.

c) Sketch the electric field () inside the semiconductor as a function of x. (5 pts total)



Graph must be positively centered around L/3, negatively centered around 2L/3, and have the correct shape.

d) Roughly sketch n and p versus x. (10 pts total)



n and *p* graphs must be centered around n_i for credit. Graphs should be mirrors of each other. n graph should look like V graph. n and p graphs are 5 pts each. If n and p cross n_i then only 3 pts each.

- 4) For Si at T = 300K calculate $E_C E_F$ and sketch E_c , E_F , E_i , and E_V as in figure 2.18 of the book for the following cases: a) $N_D = 10^{14} \text{ cm}^{-3}$; $N_A \ll N_D$. (5 pts total)
 - $n = N_D = 10^{14} \text{ cm}^{-3}$ 1 pts $n = N_C(2/pi^{1/2})F_{1/2}(\eta_c)$ $F_{1/2} = \frac{1}{2} npi^{1/2}/N_C = \frac{1}{2} (10^{14} cm^{-3})(pi^{1/2})/(3.217x10^{19} cm^{-3}) = 2.75x10^{-6}$ $(E_C - E_F) = -kT \ln(n/N_C) = -(0.0259eV)\ln(10^{14}/3.217x10^{19}) = .328eV (.3 - .4 eV accepted.)$ 1 pts
 - 1 pts
 - 2 pts

b) $N_D = 10^{20} \text{ cm}^{-3}$; $N_A \ll N_D$. (5 pts total) 1 pts $n = N_D = 10^{20} \text{ cm}^{-3}$ $n = N_C(2/pi^{\frac{1}{2}})F_{1/2}(\eta_c)$ $F_{1/2} = \frac{1}{2} npi^{\frac{1}{2}}/N_C = \frac{1}{2} (10^{20} \text{ cm}^{-3})(pi^{\frac{1}{2}})/(3.217 \times 10^{19} \text{ cm}^{-3}) = 2.75$ 1 pts 1 pts 1 pts *From graph:* $\eta_c = 2.2$ $(E_C - E_F) = -\eta_c kT = -2.2(0.0259eV) = -.057eV (.05 - .065eV accepted)$ 1 pts c) $N_A = 10^{14} \text{ cm}^{-3}$; $N_D \ll N_A$. (5 pts total) 1 pts $p = N_A = 10^{14} \text{ cm}^{-3}$ 1 pts $n = n_i^2/p = (10^{20} \text{ cm}^{-6})/(10^{14} \text{ cm}^{-3}) = 10^6 \text{ cm}^{-3}$ 1 pts $n = N_C(2/pi^{\frac{1}{2}})F_{1/2}(\eta_c)$ $F_{1/2} = \frac{1}{2} n p i^{1/2} / N_C = \frac{1}{2} (10^6 \text{ cm}^{-3}) (p i^{1/2}) / (3.217 \times 10^{19} \text{ cm}^{-3}) = 2.75 \times 10^{-14} (E_C - E_F) = -kT \ln(n/N_C) = -(0.0259 eV) \ln(10^6/3.217 \times 10^{19}) = .801 \text{ eV} (.75 eV - .85 \text{ eV} accepted)$ 2 pts

d)
$$N_A = 10^{20} \text{ cm}^{-3}$$
; $N_D << N_A$. (5 pts total)
1 pts $p = N_A = 10^{20} \text{ cm}^{-3}$
1 pts $n = n_i^2/p = (10^{20} \text{ cm}^{-6})/(10^{20} \text{ cm}^{-3}) = 1 \text{ cm}^{-3}$
1 pts $n = N_C(2/pi^{\frac{1}{2}})F_{1/2}(\eta_c)$
 $F_{1/2} = \frac{1}{2} npi^{\frac{1}{2}}/N_C = \frac{1}{2} (1 \text{ cm}^{-3})(pi^{\frac{1}{2}})/(3.217 \times 10^{19} \text{ cm}^{-3}) = 2.75 \times 10^{-20}$
2 pts $(E_C - E_F) = -kT \ln(n/N_C) = -(0.0259 \text{ eV})\ln(1/3.217 \times 10^{19}) = 1.163 \text{ eV} (1 \text{ eV} - 1.3 \text{ eV} accepted)$

e)
$$N_A = N_D = 10^{20} \text{ cm}^{-3}$$
. (5 pts total)
1 pts $n = \frac{N_D - N_A}{2} + \left[\left(\frac{N_D - N_A}{2}\right)^2 + n_i^2\right]^{\frac{1}{2}} = n_i = 10^{10} \text{ cm}^{-3}$
1 pts $p = n_i = 10^{10} \text{ cm}^{-3}$
3 pts $E_C - E_F = E_C - E_i = .567 \text{ eV}$ (can be calculated with equations, but needs to contain 3 significant figures)