

Thu 4th week

(1)

~~Thu 2nd week~~

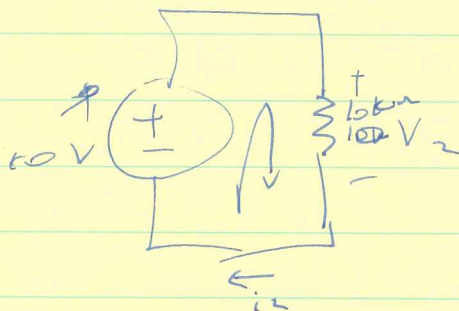
$\sum_{n=1}^N i_n = 0$  node  
 $\sum_{m=1}^M \sum_{n=1}^N v_{mn} = 0$  Loop

$V_m =$  voltage drop.

~~As you go around loop if~~

e.g.

$\rightarrow i_1$



2 nodes



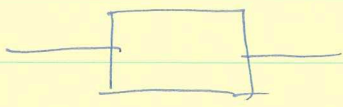
KVL  $-10V + V_2 = 0$   
 $\Rightarrow V_2 = 10V$

KCL  $\Rightarrow i_1 = i_2$

Ohm's law =  $V_2 = i_2 R \Rightarrow i_2 = \frac{10V}{10k\Omega} = 1mA$

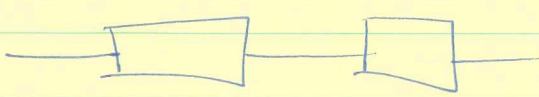
Done. Know I, V everywhere.

Absolute V vs relative?



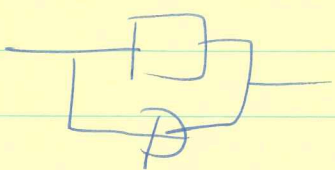
Stands for any circuit element (Resistor or source)

2 circuit elements connected like this

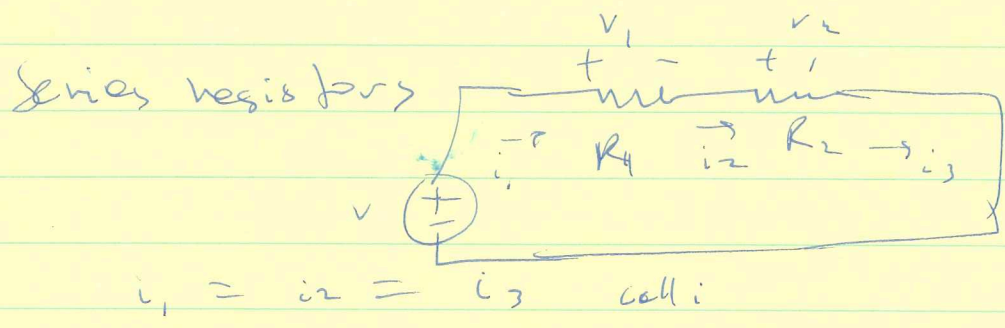


are said to be in series.

2 circuit elements connected like this



are said to be in parallel.



$$V_1 = iR_1$$

$$V_2 = iR_2$$

$$-V + V_1 + V_2 = 0 \quad \text{KVL}$$

$R_1, R_2, V$  knowns  
 $i, V_1, V_2$  not known.

3 eqns, 3 unknown, general theorem  
linear algebra

$$i = \frac{V}{R_1 + R_2}$$

$$R_{eq} = R_1 + R_2$$

$$\Rightarrow \frac{R_1}{\parallel} \frac{R_2}{\parallel} = \frac{R_{eq}}{\parallel}$$

$N$  resistors in series  $R_{eq} = \sum_n R_n$

Analogy voltage divider.  
 Elaborate

⑤

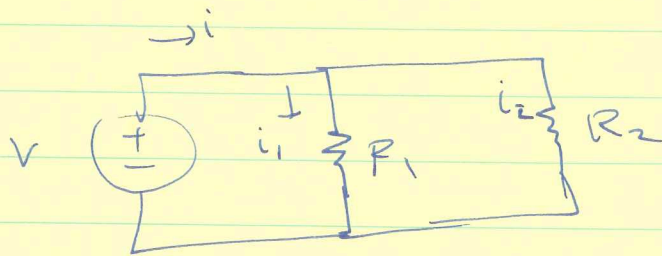
Very important example

0.12      1M2  
~~~~~

—      1.00000  
         1.0000001M2  
~~~~~

Be reasonable. Ignore 0.12

### Parallel resistors



$$V = i_1 R_1 = i_2 R_2$$

$$i_1 = V/R_1 = V/R_2$$

$$\text{KCL} \Rightarrow i = i_1 + i_2$$

$$i = \frac{V}{R_1} + \frac{V}{R_2} = V \left( \frac{1}{R_1} + \frac{1}{R_2} \right) = \frac{V}{R_{eq}}$$

$$\frac{1}{R_{eq}} = \frac{1}{R_1} + \frac{1}{R_2} \Leftrightarrow R_{eq} = \frac{R_1 R_2}{R_1 + R_2}$$

N in parallel

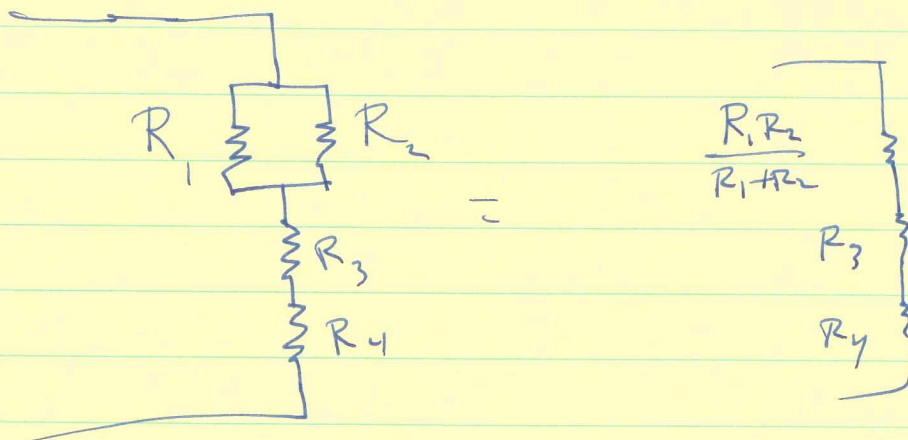
$$\frac{1}{R_{eq}} = \sum_n \frac{1}{R_n}$$



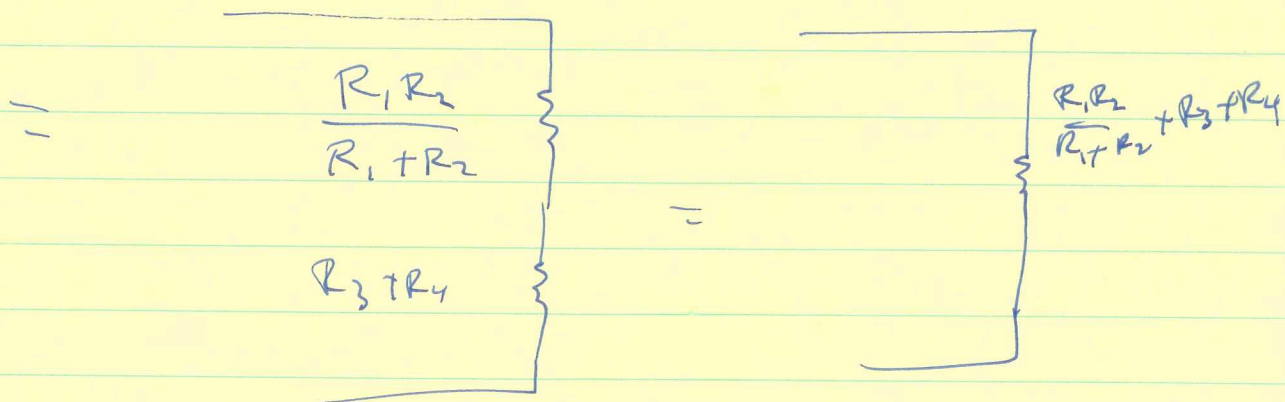
$R_1 \parallel R_2$  means  
 $R_1$  in parallel with  $R_2$



Eg.

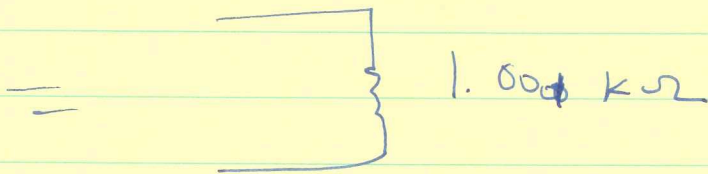
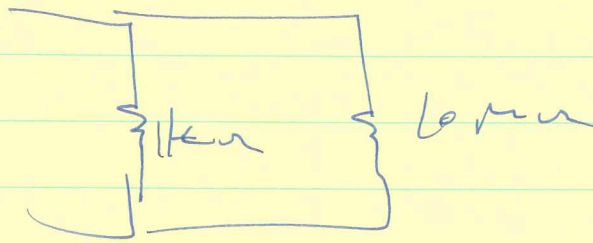


What is  $R_{eq}$ ?



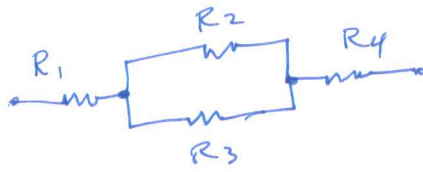


Important example

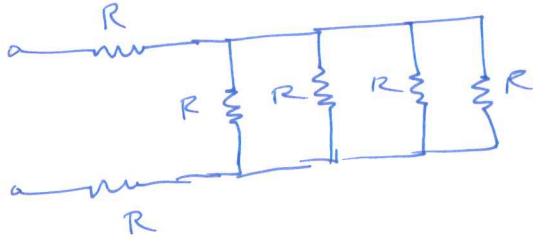


be reasonable. ignore 10μA.

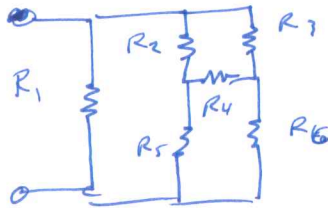
eg.



$$R_{eq} = ?$$

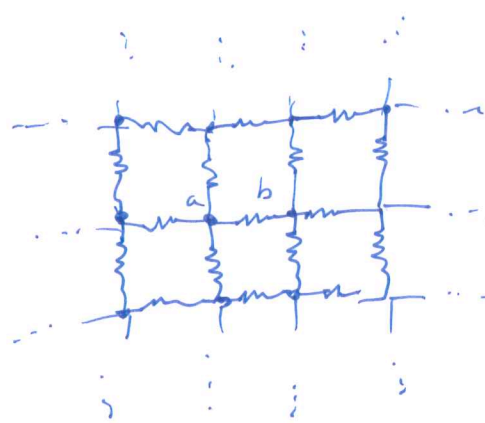


$$R_{eq} = ?$$



$$R_{eq} = ?$$

Teaser:



$$R_{ab} = ?$$