

which is defined by the  $y$ -parameters discussed previously. The intrinsic resistance can be lumped with the extrinsic base resistance as well as the emitter resistance.

Device properties are often expressed in terms of  $z$ - (impedance) and  $h$ -parameters, we describe them briefly. For the  $y$ -parameter discussed in § 8-2,  $i_1$  and  $i_2$  are the independent variables describing a network and  $v_1, v_2$  are the dependent variables. For  $z$ -parameters, the independent variables are  $v_1$  and  $v_2$ . For convenience, we write out the relevant relationships, they are  $i_1$  and  $i_2$ . For convenience, we write out the relevant relationships, they are  $i_1$  and  $i_2$ .

$$\begin{bmatrix} i_1 \\ i_2 \end{bmatrix} = \begin{bmatrix} y_{11} & y_{12} \\ y_{21} & y_{22} \end{bmatrix} \begin{bmatrix} v_1 \\ v_2 \end{bmatrix} \quad (4-90)$$

$$\begin{bmatrix} v_1 \\ v_2 \end{bmatrix} = \begin{bmatrix} z_{11} & z_{12} \\ z_{21} & z_{22} \end{bmatrix} \begin{bmatrix} i_1 \\ i_2 \end{bmatrix} \quad (4-91)$$

$$\begin{bmatrix} v_1 \\ v_2 \end{bmatrix} = \begin{bmatrix} h_{11} & h_{12} \\ h_{21} & h_{22} \end{bmatrix} \begin{bmatrix} i_1 \\ i_2 \end{bmatrix} \quad (4-92)$$

determined  $y$ 's for both the common-base and the common-emitter circuits. Once these parameters are known, the  $z$ - and the  $h$ -parameters are determined. For example, let us find  $z_{11}$  in terms of the  $y$ -parameters.  $z_{11}$  is the ratio of  $v_1$  over  $i_1$  when  $i_2 = 0$ , Eq. (4-90) implies that:

$$v_2 = -\frac{y_{21}}{y_{22}} v_1 \quad (4-93)$$

Using this result into Eq. (4-90), it is found that:

$$i_1 = y_{11}v_1 - y_{12}\frac{y_{21}}{y_{22}}v_1 = \left( \frac{y_{11}y_{22} - y_{12}y_{21}}{y_{22}} \right) v_1 \quad (4-94)$$

Therefore,  $z_{11}$  is

$$z_{11} = \left. \frac{v_1}{i_1} \right|_{i_2=0} = \frac{y_{22}}{\Delta y} \quad (4-95)$$

$$\Delta y = y_{11}y_{22} - y_{12}y_{21} \quad (4-96)$$

$z_{11}$  is a conversion table for the small-signal parameters.  $z_{11}$  expressed in Eq. (4-95) is indeed listed at the proper entry in the figure. The derivations of other relationships are straightforward and not discussed further.

FIGURE 4-17. Conversion table between the  $s$ -,  $y$ -,  $z$ -, and  $h$ -parameters.

$y_{11} = \frac{1}{z_{11}}$	$y_{12} = \frac{z_{12}}{z_{11}z_{22} - z_{21}z_{12}}$	$y_{21} = \frac{-z_{21}}{z_{11}z_{22} - z_{21}z_{12}}$	$y_{22} = \frac{1}{z_{22}}$
$z_{11} = \frac{1}{y_{11}}$	$z_{12} = \frac{-y_{12}}{y_{11}y_{22} - y_{21}y_{12}}$	$z_{21} = \frac{y_{21}}{y_{11}y_{22} - y_{21}y_{12}}$	$z_{22} = \frac{1}{y_{22}}$
$h_{11} = \frac{z_{11}}{z_{22}}$	$h_{12} = \frac{z_{12}}{z_{22}}$	$h_{21} = -\frac{z_{21}}{z_{22}}$	$h_{22} = \frac{1}{z_{22}}$
$s_{11} = \frac{1}{h_{11}}$	$s_{12} = \frac{-h_{12}}{h_{11}h_{22} - h_{21}h_{12}}$	$s_{21} = \frac{h_{21}}{h_{11}h_{22} - h_{21}h_{12}}$	$s_{22} = \frac{1}{h_{11}}$
$z_{11} = \frac{1}{s_{11}}$	$z_{12} = \frac{-s_{12}}{s_{11}s_{22} - s_{21}s_{12}}$	$z_{21} = \frac{s_{21}}{s_{11}s_{22} - s_{21}s_{12}}$	$z_{22} = \frac{1}{s_{11}}$
$h_{11} = \frac{z_{11}}{z_{22}}$	$h_{12} = \frac{z_{12}}{z_{22}}$	$h_{21} = -\frac{z_{21}}{z_{22}}$	$h_{22} = \frac{1}{z_{22}}$
$s_{11} = \frac{1}{h_{11}}$	$s_{12} = \frac{-h_{12}}{h_{11}h_{22} - h_{21}h_{12}}$	$s_{21} = \frac{h_{21}}{h_{11}h_{22} - h_{21}h_{12}}$	$s_{22} = \frac{1}{h_{11}}$
$z_{11} = \frac{1}{s_{11}}$	$z_{12} = \frac{-s_{12}}{s_{11}s_{22} - s_{21}s_{12}}$	$z_{21} = \frac{s_{21}}{s_{11}s_{22} - s_{21}s_{12}}$	$z_{22} = \frac{1}{s_{11}}$
$h_{11} = \frac{z_{11}}{z_{22}}$	$h_{12} = \frac{z_{12}}{z_{22}}$	$h_{21} = -\frac{z_{21}}{z_{22}}$	$h_{22} = \frac{1}{z_{22}}$
$s_{11} = \frac{1}{h_{11}}$	$s_{12} = \frac{-h_{12}}{h_{11}h_{22} - h_{21}h_{12}}$	$s_{21} = \frac{h_{21}}{h_{11}h_{22} - h_{21}h_{12}}$	$s_{22} = \frac{1}{h_{11}}$
$z_{11} = \frac{1}{s_{11}}$	$z_{12} = \frac{-s_{12}}{s_{11}s_{22} - s_{21}s_{12}}$	$z_{21} = \frac{s_{21}}{s_{11}s_{22} - s_{21}s_{12}}$	$z_{22} = \frac{1}{s_{11}}$
$h_{11} = \frac{z_{11}}{z_{22}}$	$h_{12} = \frac{z_{12}}{z_{22}}$	$h_{21} = -\frac{z_{21}}{z_{22}}$	$h_{22} = \frac{1}{z_{22}}$
$s_{11} = \frac{1}{h_{11}}$	$s_{12} = \frac{-h_{12}}{h_{11}h_{22} - h_{21}h_{12}}$	$s_{21} = \frac{h_{21}}{h_{11}h_{22} - h_{21}h_{12}}$	$s_{22} = \frac{1}{h_{11}}$
$z_{11} = \frac{1}{s_{11}}$	$z_{12} = \frac{-s_{12}}{s_{11}s_{22} - s_{21}s_{12}}$	$z_{21} = \frac{s_{21}}{s_{11}s_{22} - s_{21}s_{12}}$	$z_{22} = \frac{1}{s_{11}}$
$h_{11} = \frac{z_{11}}{z_{22}}$	$h_{12} = \frac{z_{12}}{z_{22}}$	$h_{21} = -\frac{z_{21}}{z_{22}}$	$h_{22} = \frac{1}{z_{22}}$

$$z = z/R_o, \quad y = y/R_o, \quad h_{11}/R_o = h_{11}, \quad h_{21} = h_{21}, \quad h_{12} = h_{12}, \quad h_{22} = h_{22}R_o.$$