Announcements:

1. HW # 2 will be posted online (due Wed)
2. Next lecture will be a review by TA to prepare for the midterm

EECS 70A: Network Analysis

Lecture 4

Review & agenda

Last lecture:

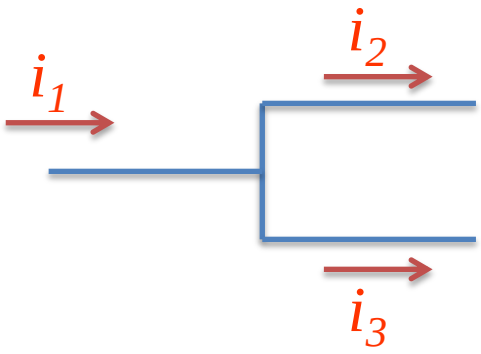
- Resistor circuits
  - Series
  - Parallel
- Kirchoff's current law (KCL)

Today

- Examples of KCL
- Kirchoff's voltage law (KVL)
- Examples with KVL, KCL, Ohm
- Δ-Y transformations

Kirchoff's current law

You have already seen:



$$i_1 = i_2 + i_3$$

Like water in a river…

More generally:

Sum of currents *entering* node = sum of currents *leaving* node.

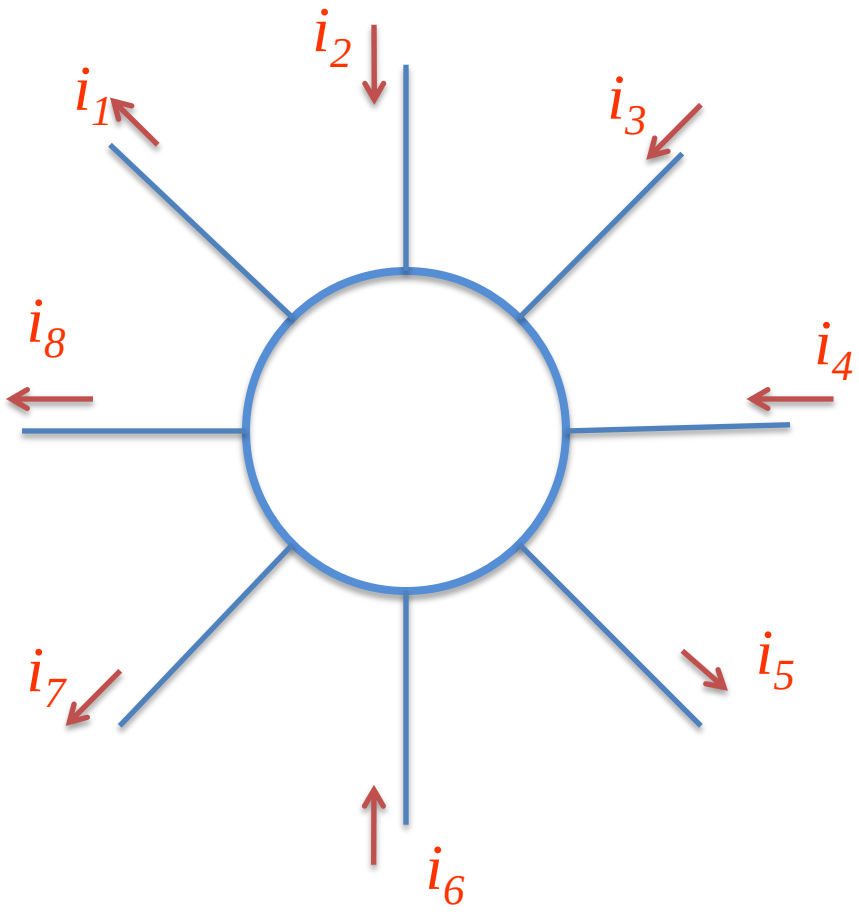
Stated as Kirchoff's current law (KCL):

$$\sum_{n=1}^{N} i_n = 0$$

Current *entering* a node: i_n positive
Current *leaving* a node: i_n negative

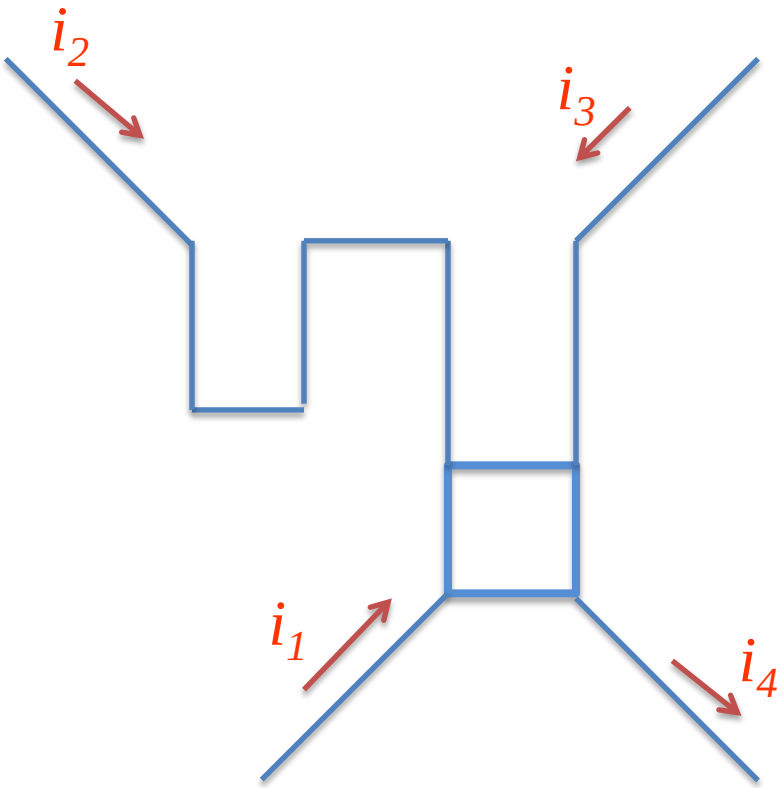
KCL examples

Find a relationship among $i_1, i_2, i_3, i_{4...}$ (instructor)



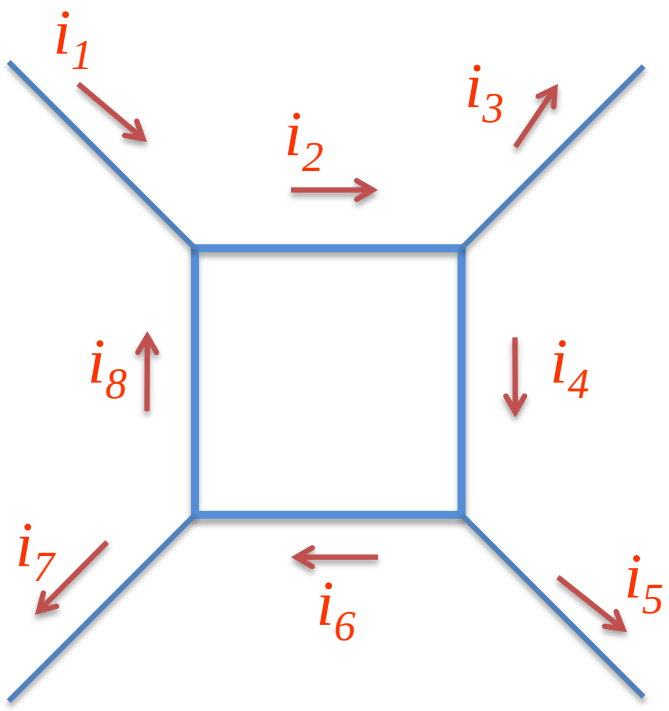
KCL examples

Find a relationship among $i_1, i_2, i_3, i_{4...}$ (students)



KCL examples

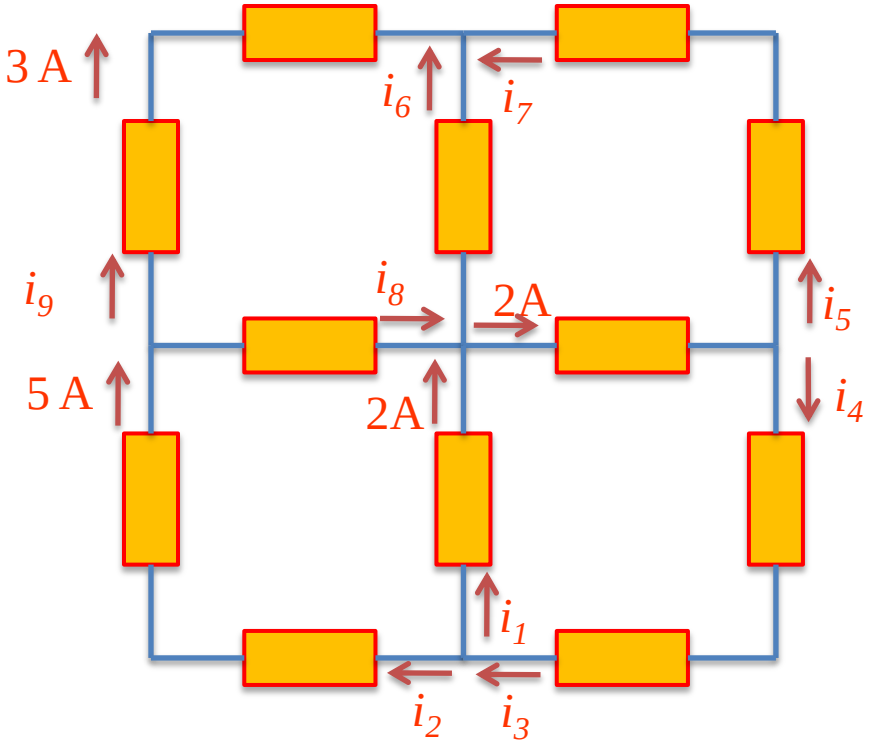
Find a relationship among $i_1, i_2, i_3, i_{4...}$ (instructor)



KCL examples

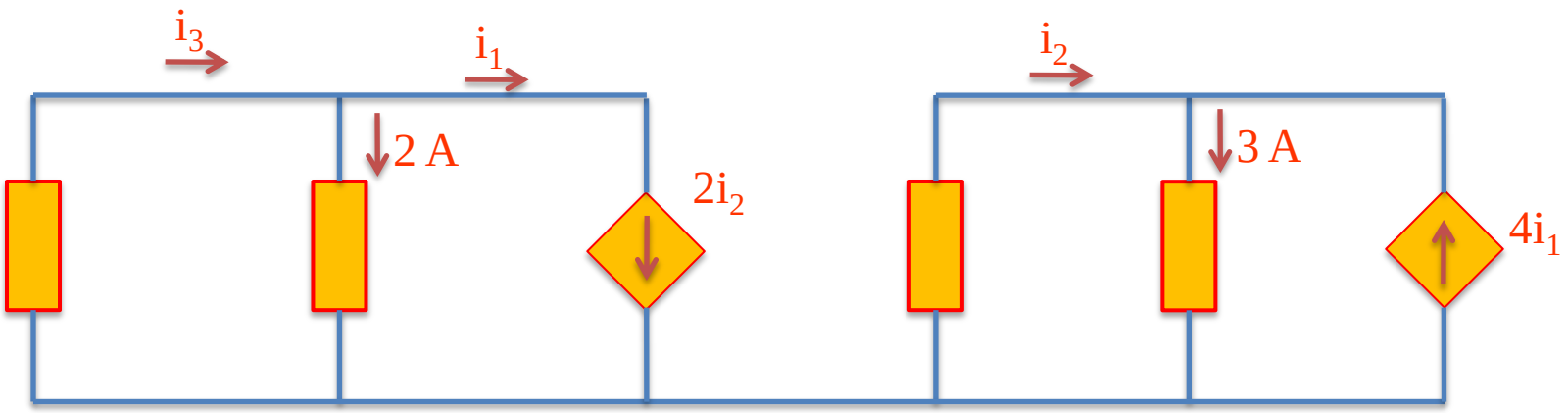
a) Find the # of nodes in this circuit. (Instructor)

b) Find is i_1 thru i_9 in this circuit. (Instructor)
Hint: Apply KCL at each node.



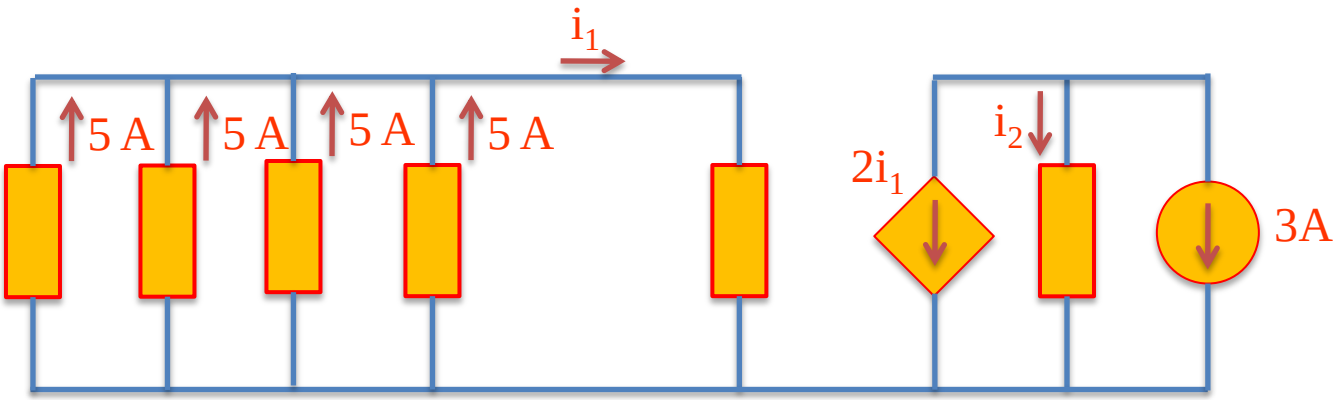
a) Find the # of nodes in this circuit. (Instructor)
b) Find is i_1 i_2 & i_3 in this circuit. (Instructor)
Hint: Apply KCL at each node.

KCL examples



a) Find the # of nodes in this circuit. (students)
b) Find is i_1 & i_2 in this circuit. (students)
Hint: Apply KCL at each node.

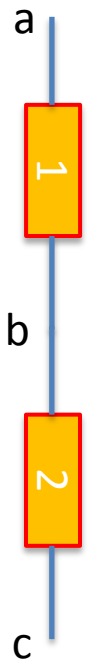
KCL examples



Questions?

Voltage addition in circuits

From lecture #2:



$$V_{ab} \equiv \int_a^b E dx$$

$$V_{bc} \equiv \int_b^c E dx$$

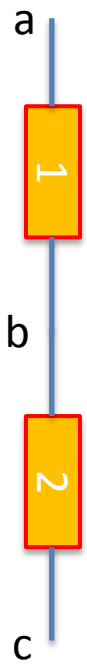
$$\Rightarrow V_{ac} \equiv \int_a^c E dx = \int_a^b E dx + \int_b^c E dx = V_{ab} + V_{bc}$$

$$V_{ac} = V_{ab} + V_{bc}$$

V_{ab} = "voltage drop" across element # 1

V_{bc} = "voltage drop" across element # 2

Closing the loop:

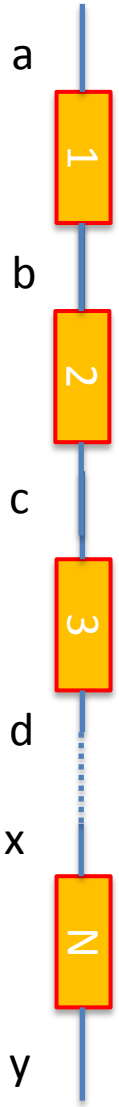


$$V_{ac} = V_{ab} + V_{bc}$$

V_{ab} = “voltage drop” across element # 1

V_{bc} = “voltage drop” across element # 2

Generalize loop to N-elements:



$$V_{ay} = V_{ab} + V_{bc} + V_{cd} + \ldots + V_{xy}$$

V_{ab} = “voltage drop” across element # 1

V_{bc} = “voltage drop” across element # 2

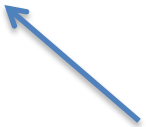
V_{cd} = “voltage drop” across element # 3

V_{xy} = “voltage drop” across element # N

Kirchoff's voltage law

$$\sum_{n=1}^{N} v_n = 0$$

around *any* closed loop.

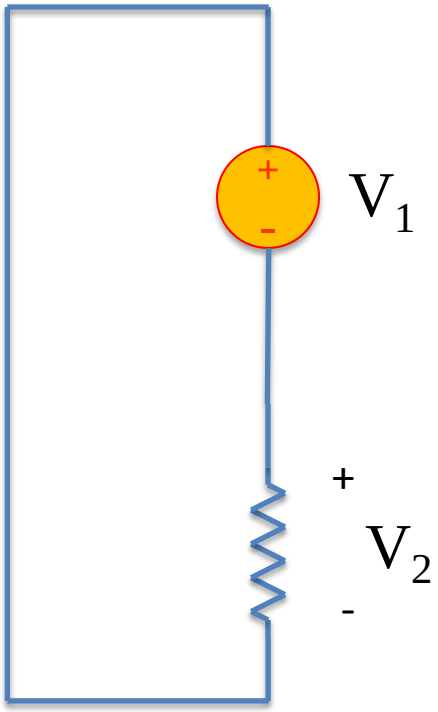


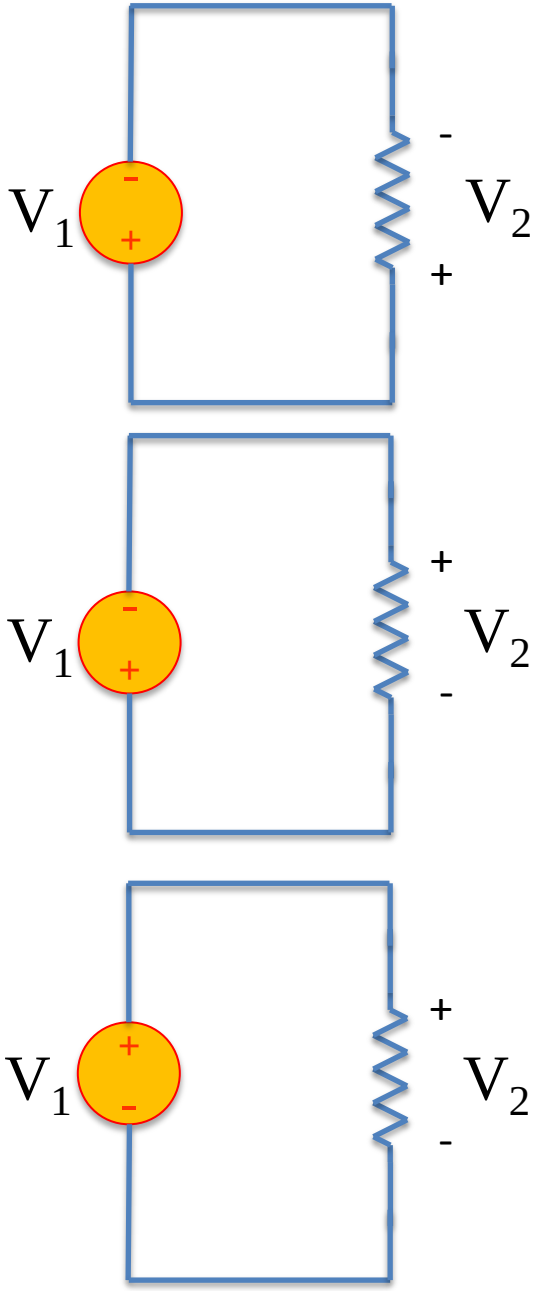
voltage *drops*

If the voltage is *dropping* as you go around the loop, the voltage drop v_n is *positive*.

KVL application

If the voltage is *dropping* as you go around the loop, the voltage drop v_n is *positive*.

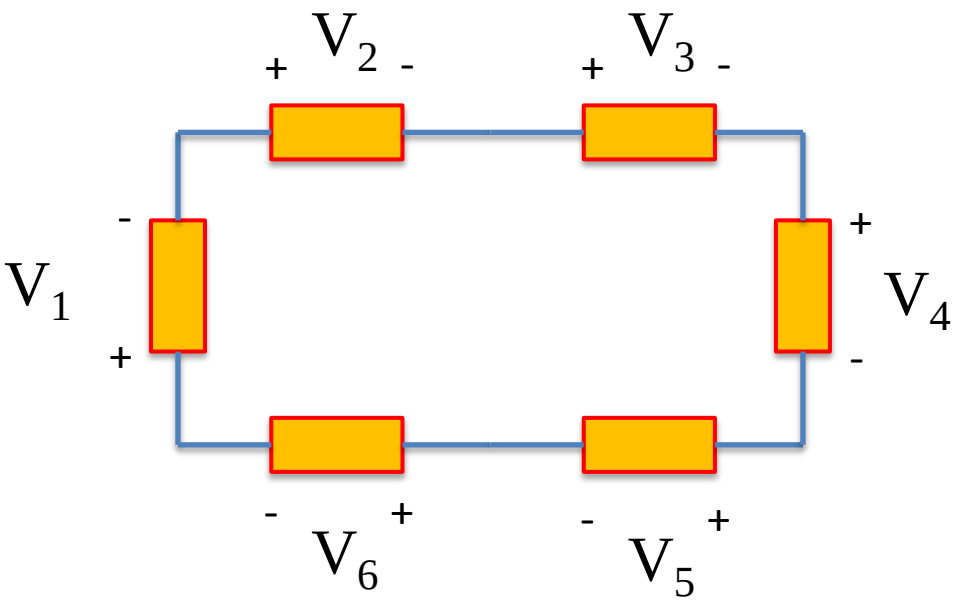




KVL examples

If the voltage is *dropping* as you go around the loop, the voltage drop v_n is *positive*.

Apply KVL to the circuit below (instructor)



KVL examples

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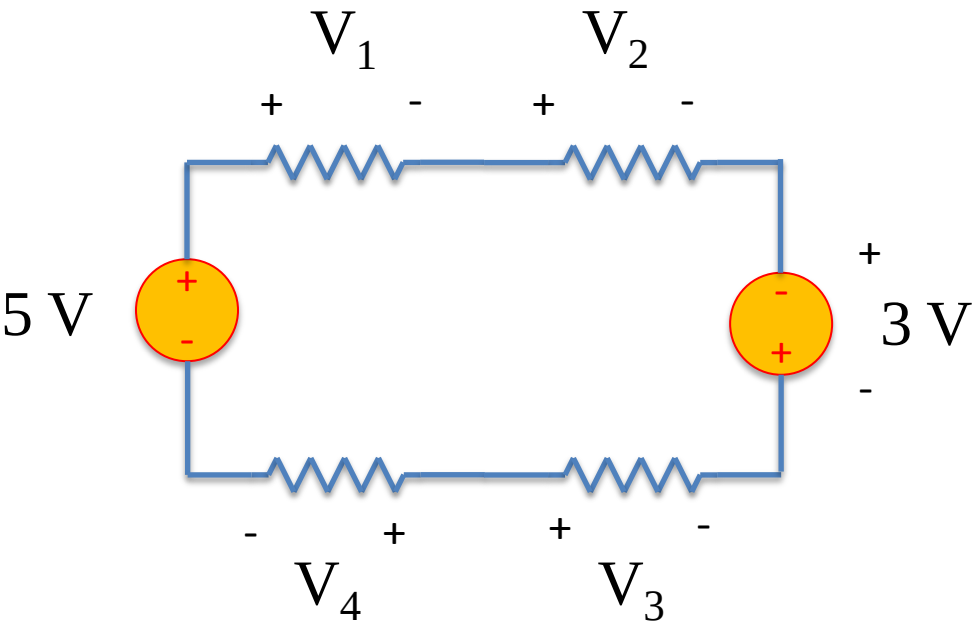
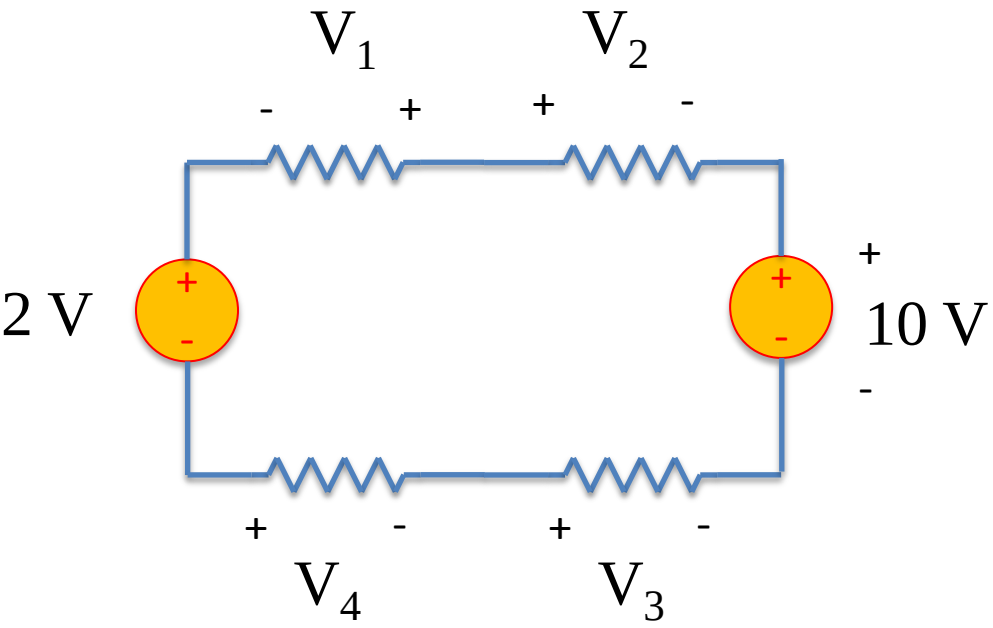


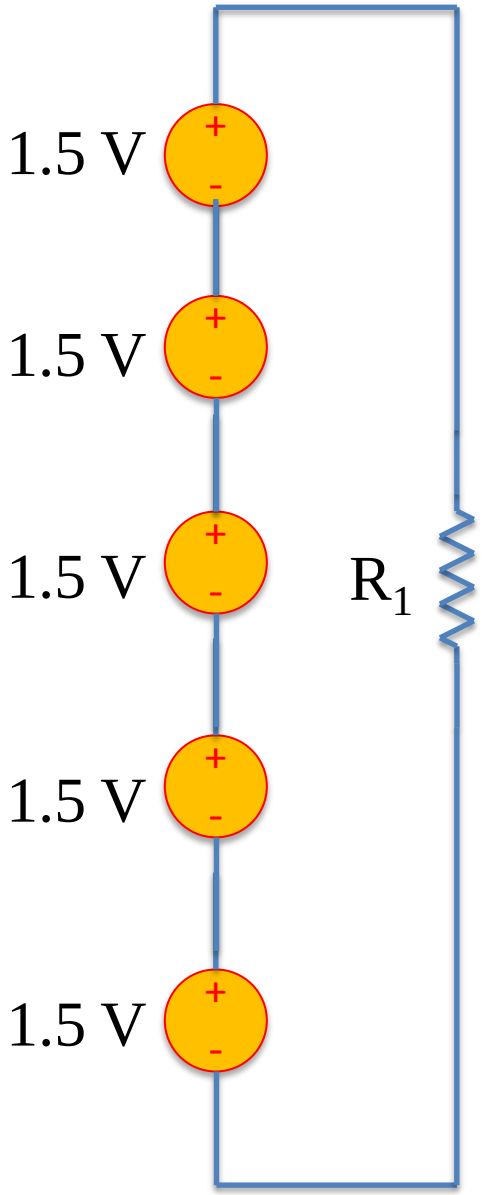
KVL examples

If the voltage is *dropping* as you go around the loop, the voltage drop v_n is *positive*.

Apply KVL to the circuit below (student)



Find the voltage across R1 (student)

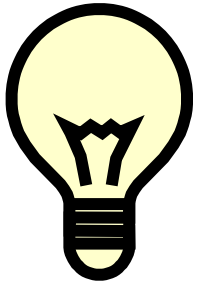


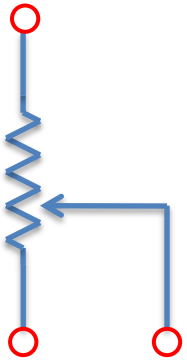
Demo…

Dimming circuit

Given the four elements below:

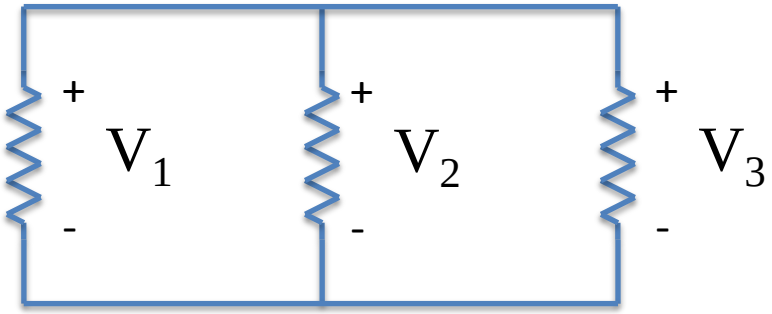
1. Design a circuit that continuously dims the light.
   (It needs to go from completely dim to completely bright.)
2. Calculate the power supplied by the battery when the bulb is brightest and when it is off.



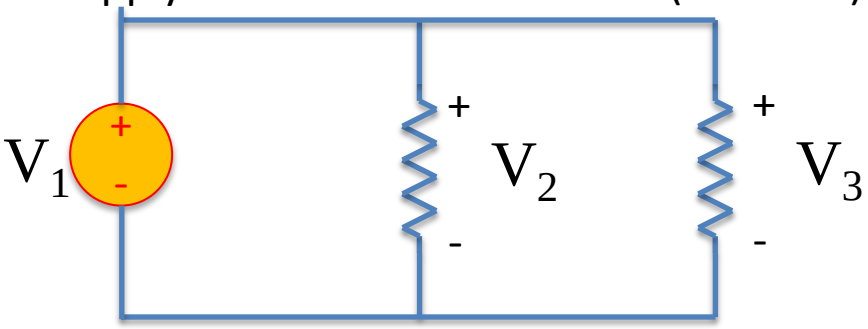


KVL examples

Apply KVL to the circuit below (instructor)



Apply KVL to the circuit below (students)



KVL examples

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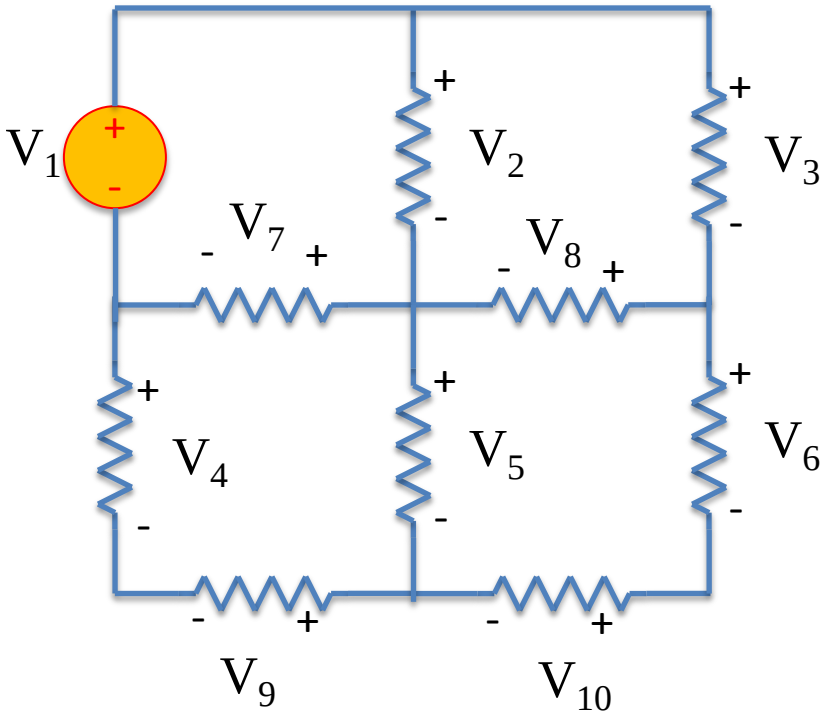
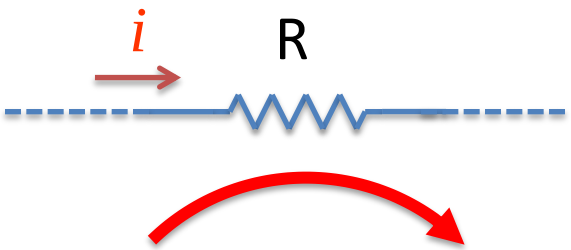
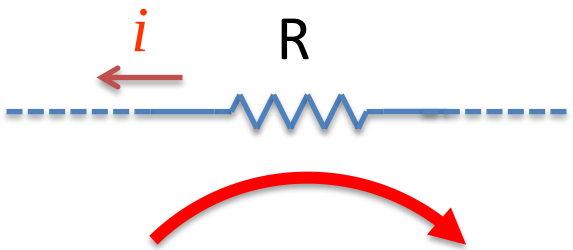


Questions?

Sign of voltage drop



Voltage drop
= + i R



Voltage drop
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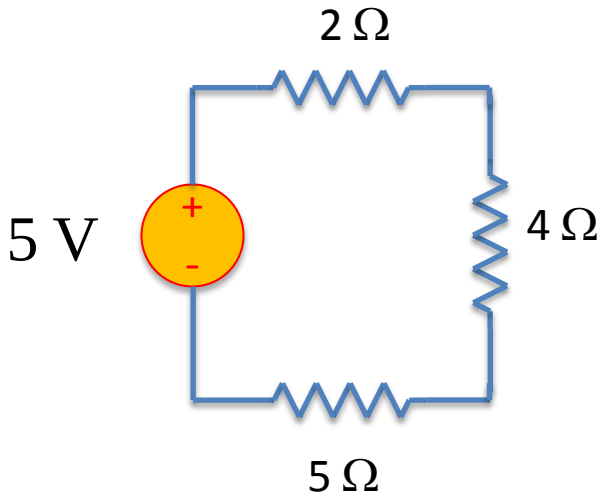
Combining KVL + Ohm

Find the current flowing in this circuit (instructor):



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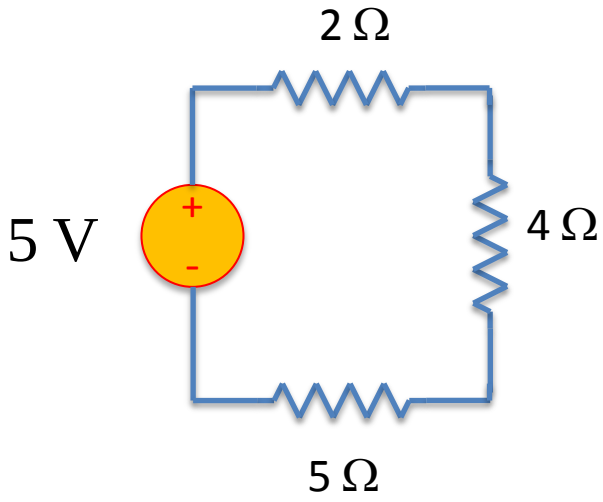
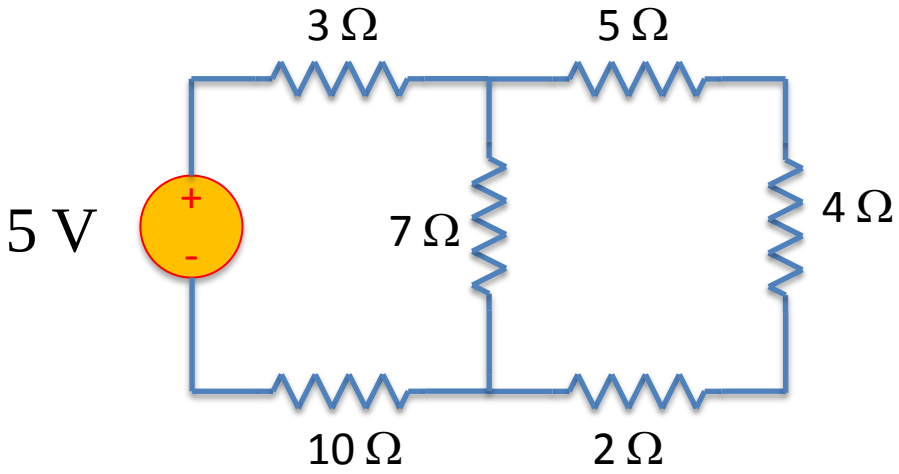


Combining KVL + KCL + Ohm

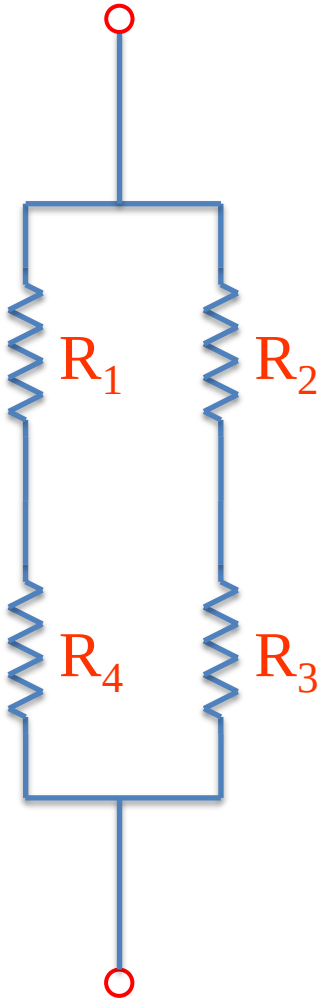
Find the currents flowing in the circuit below (instructor):



Questions?

Example problems

Solve for R_{eq}. (students).



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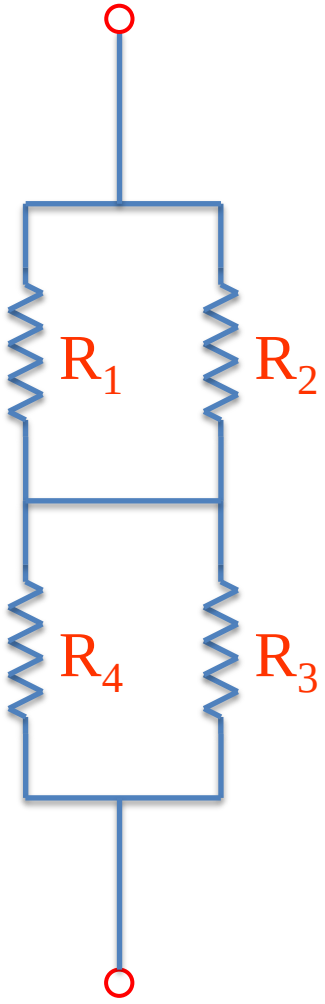

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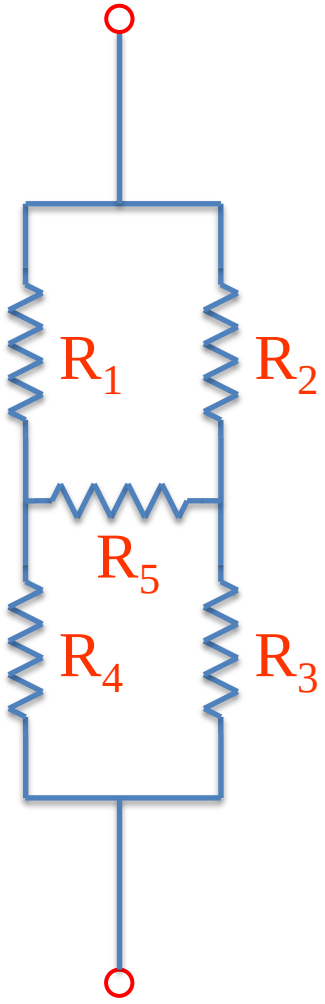
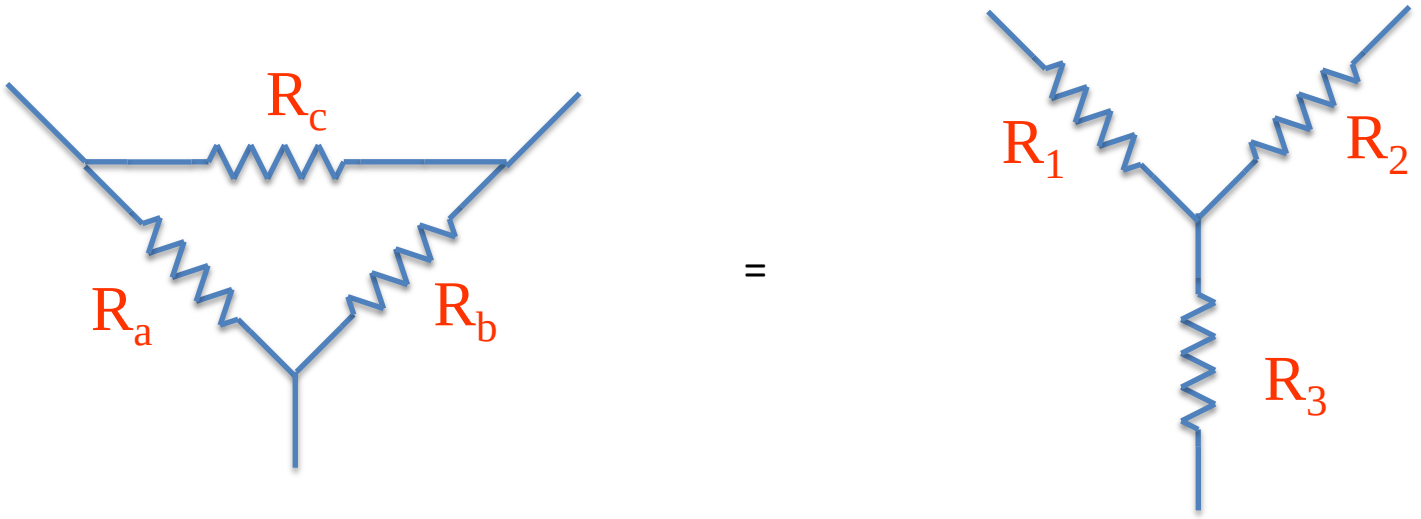


Δ-Y transformations



If:

$$R_1 = \frac{R_b R_c}{R_a + R_b + R_c}$$

$$R_2 = \frac{R_c R_a}{R_a + R_b + R_c}$$

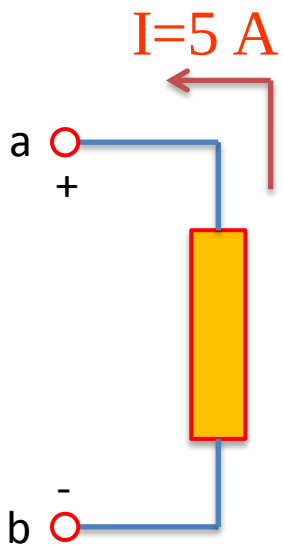
$$R_3 = \frac{R_a R_b}{R_a + R_b + R_c}$$

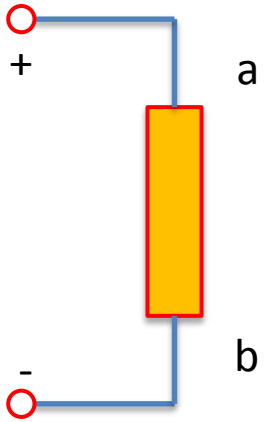
$$R_a = \frac{R_1 R_2 + R_2 R_3 + R_3 R_1}{R_1}$$

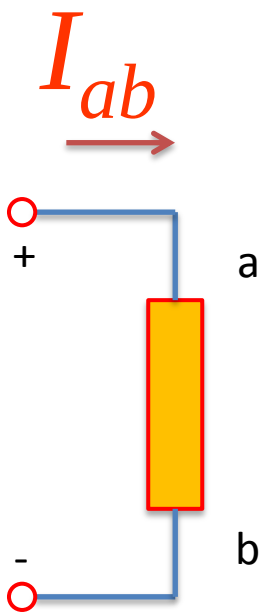
$$R_b = \frac{R_1 R_2 + R_2 R_3 + R_3 R_1}{R_2}$$

$$R_b = \frac{R_1 R_2 + R_2 R_3 + R_3 R_1}{R_3}$$

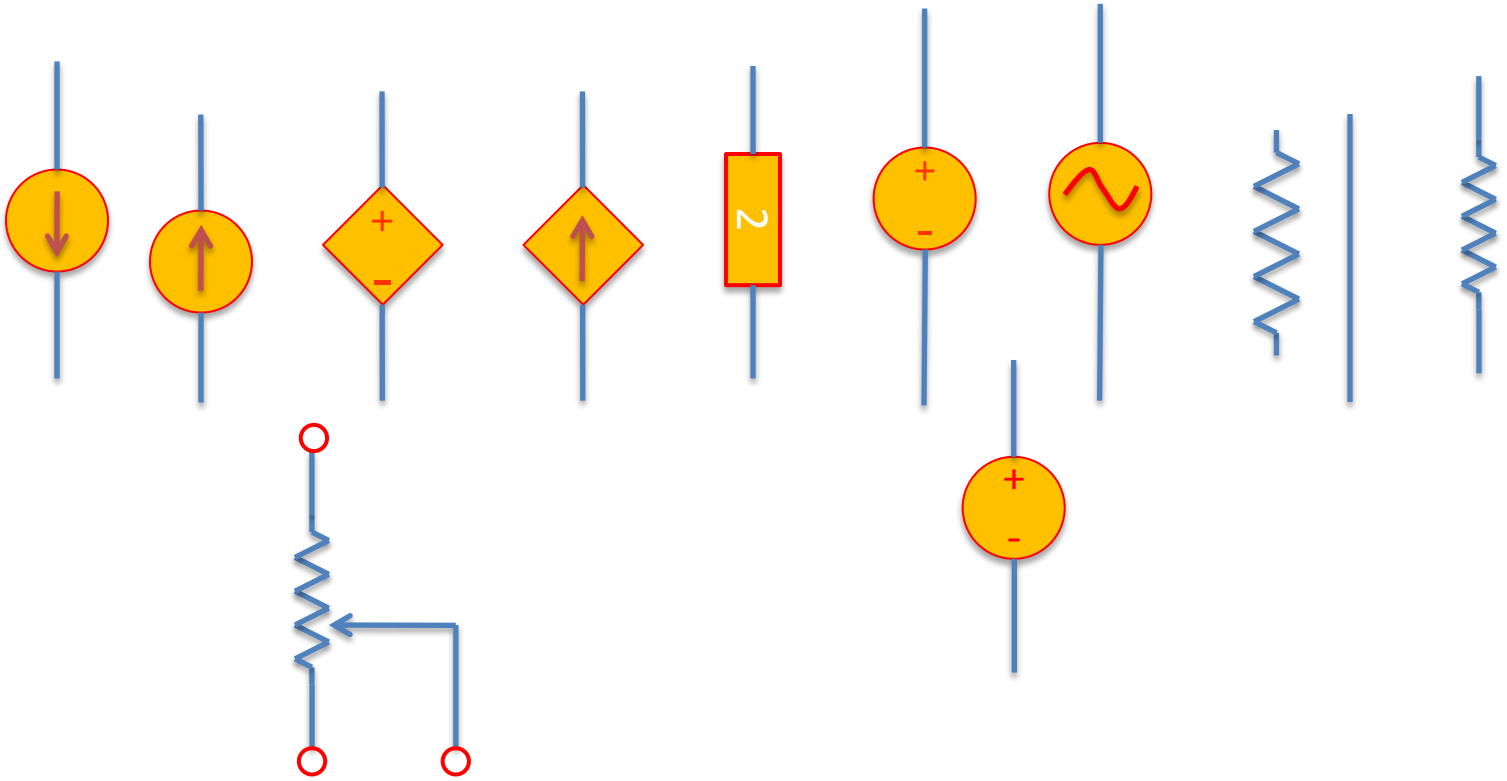
Symbol library







Symbol library



Symbol & circuit library