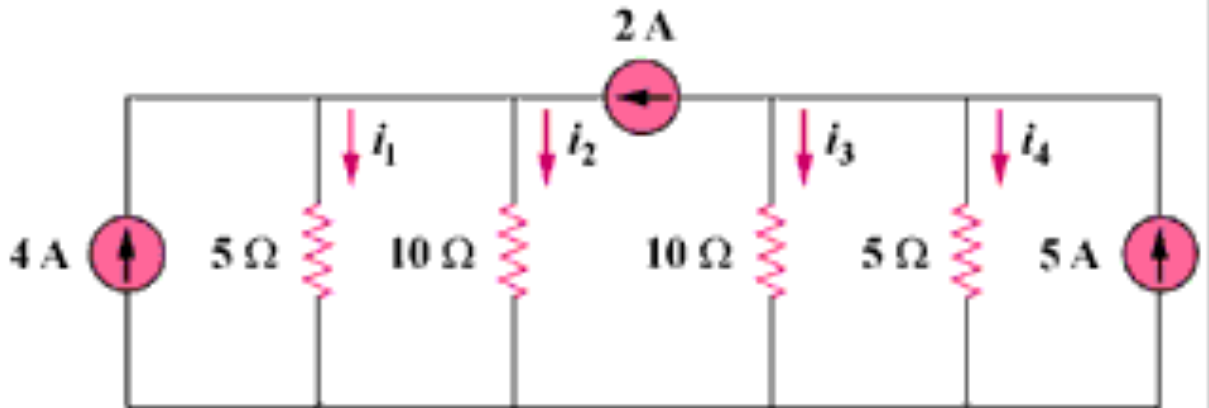


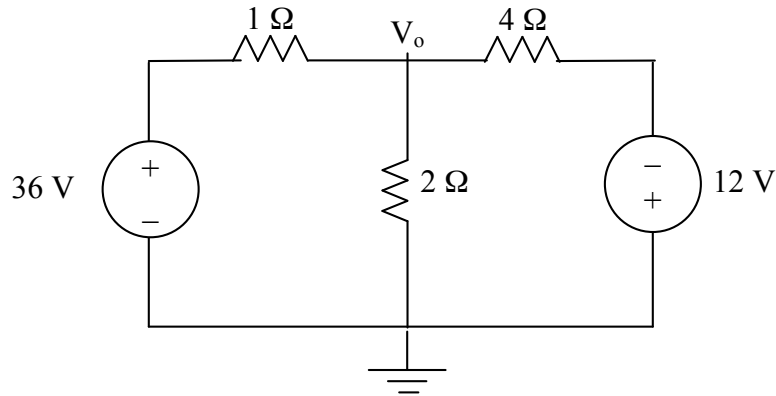
1	2	3	4	5	6	Total
/20	/20	/20	/20	/10	/10	/100

**DO NOT BEGIN THE EXAM  
UNTIL YOU ARE TOLD TO  
DO SO.**

**PROBLEM ONE: (20 points)**

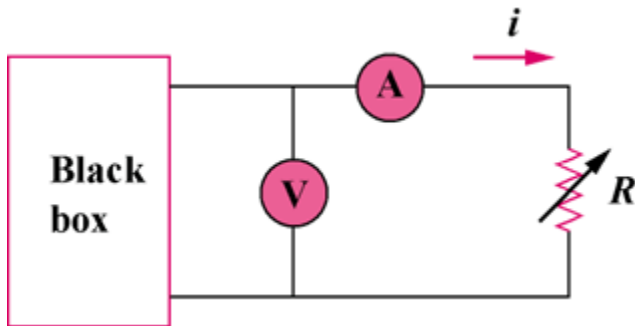
Given the circuit below, calculate the currents  $i_1$  through  $i_4$ .



**PROBLEM TWO(20 points):**Find  $V_o$  in the circuit below.

**PROBLEM THREE(20 points):**

A black box with a circuit in it is connected to a variable resistor. An ideal ammeter (with zero resistance) and an ideal voltmeter (with infinite resistance) are used to measure current and voltage as shown below. The results are shown in the table below.

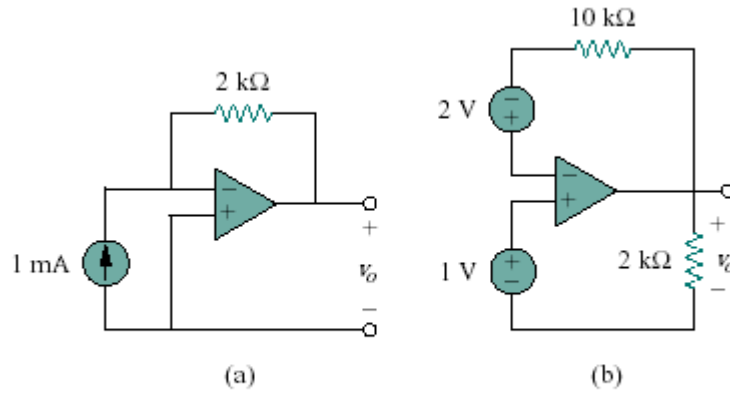


- (a) Find  $i$  when  $R = 4 \Omega$ .  
 (b) Determine the maximum power from the box.

$R(\Omega)$	$V(V)$	$i(A)$
2	3	1.5
8	8	1.0
14	10.5	0.75

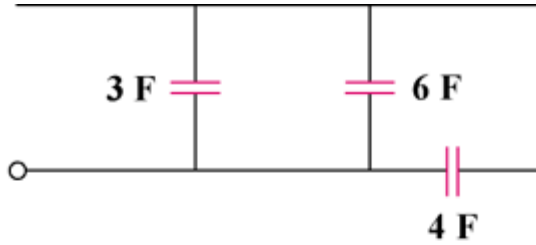
**PROBLEM FOUR(20 points):**

Obtain  $v_o$  for each of the op amp circuits below.



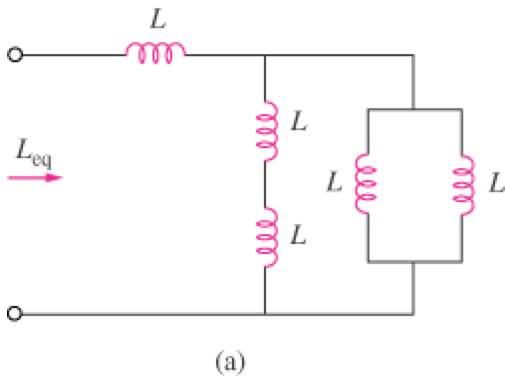
**PROBLEM FIVE (10 points):**

Determine the equivalent capacitance the circuit below.



**PROBLEM SIX(10 points):**

Find  $L_{eq}$  in the circuit below.

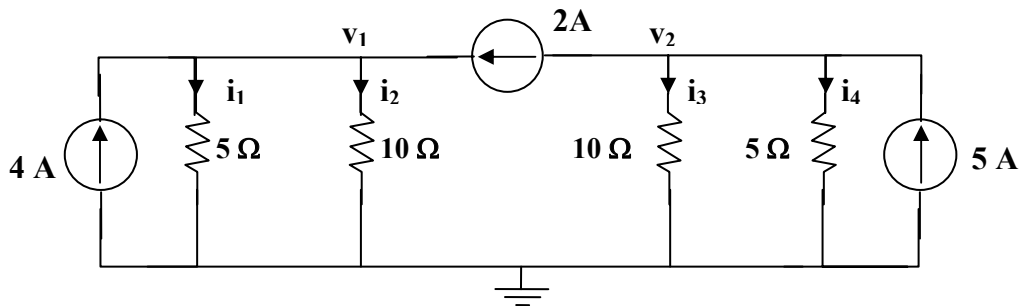


EECS70A / CSE 70A Network Analysis I  
Prof. Peter Burke

Midterm II solution

Grading criteria for all questions: no credits for answers without units and - 3pts for calculation error

Problem 1:



At node 1,

$$4 + 2 = v_1/(5) + v_1/(10) \longrightarrow v_1 = 20$$

At node 2,

$$5 - 2 = v_2/(10) + v_2/(5) \longrightarrow v_2 = 10$$

$$i_1 = v_1/(5) = \underline{4 \text{ A}}, i_2 = v_1/(10) = \underline{2 \text{ A}}, i_3 = v_2/(10) = \underline{1 \text{ A}}, i_4 = v_2/(5) = \underline{2 \text{ A}}$$

Grading criteria: 3pts for only KCL at ground or at one node

5pts for only KCL equation or mesh equation with wrong sign

10pts for correct KCL equation at  $V_1$  and  $V_2$  or mesh equation with incorrect answer

Problem 2:



At the top node, KVL gives

$$\frac{V_o - 36}{1} + \frac{V_o - 0}{2} + \frac{V_o - (-12)}{4} = 0$$

$$1.75V_o = 33V \quad \text{or} \quad V_o = 18.86V$$

Alternatively, mesh analysis can be used

$$i_1 = 17.14A, \quad i_2 = 7.71A$$

$$V_o = 2(i_1 - i_2) = 18.86V$$

Grading criteria: 5pts for only KCL or mesh equation with wrong sign  
 5pts for correct mesh current  $i_1$  and  $i_2$  on mesh analysis  
 10pts for correct KCL or mesh equation with incorrect answer

Problem 3:

We replace the box with the Thevenin equivalent.

$$\text{When } i = 1.5, \quad v = 3, \quad \text{which implies that } V_{Th} = 3 + 1.5R_{Th} \quad (1)$$

$$\text{When } i = 1, \quad v = 8, \quad \text{which implies that } V_{Th} = 8 + R_{Th} \quad (2)$$

From (1) and (2),  $R_{Th} = 10 \text{ ohms}$  and  $V_{Th} = 18 \text{ V}$ .

$$(a) \quad \text{When } R = 4, \quad i = V_{Th}/(R + R_{Th}) = 18/(4 + 10) = \underline{\underline{1.2857 \text{ A}}}$$

$$(b) \quad \text{For maximum power, } \underline{\underline{R = R_{Th}}}$$

$$P_{max} = (V_{Th})^2/4R_{Th} = 18^2/(4 \times 10) = \underline{\underline{8.1 \text{ watts}}}$$

$$= i^2 R_{Th} = (0.9)^2 \times 10 = \underline{\underline{8.1 \text{ watts}}}$$

Grading criteria: No credit for final answers without  $R_{Th}$ ,  $V_{Th}$   
 2pts for showing equivalent circuit in the box ( $R_{Th}$ ,  $V_{Th}$ )  
 3pts for correct  $i$  equation  
 3pts for correct power equation showing  $R = R_{Th}$

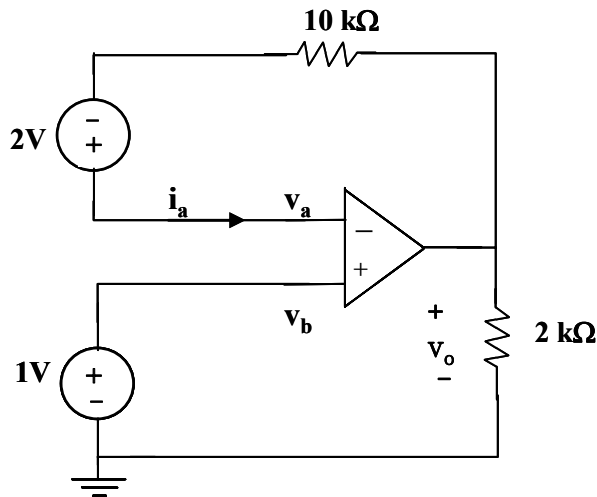
5pts for correct  $R_{Th}$  and  $V_{Th}$

Problem 4:

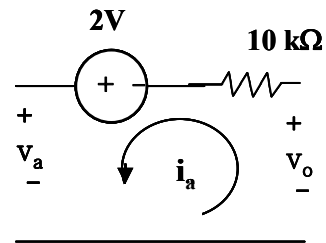
- (a) If  $v_a$  and  $v_b$  are the voltages at the inverting and noninverting terminals of the op amp.

$$v_a = v_b = 0$$

$$1\text{mA} = \frac{0 - v_0}{2\text{k}} \quad \longrightarrow \quad v_0 = \underline{-2\text{V}}$$



(a)



(b)

Since  $v_a = v_b = 1\text{V}$  and  $i_a = 0$ , no current flows through the 10 kΩ resistor.

From Fig. (b),

$$-v_a + 2 + v_0 = 0 \quad \longrightarrow \quad v_0 = v_a - 2 = 1 - 2 = \underline{-1\text{V}}$$

Grading criteria: 3 pts for correct  $V_a$  and  $V_b$  for each question

5pts for correct KCL equation for (a) with wrong answer

-3pts for wrong sign of final answer with correct steps

Problem 5:

$$C_{eq} = 3F // 6F // 4F = 3+6+4 = 13F$$

Grading criteria: 3pts for showing parallel connection with wrong answer  
-3pts for calculation error

Problem 6:

$$L // L = 0.5L, \quad L + L = 2L$$

$$L_{eq} = L + 2L // 0.5L = L + \frac{2L \times 0.5L}{2L + 0.5L} = 1.4L = \underline{\underline{1.4L}}$$

Grading criteria: 3pts for showing correct connections with wrong answer  
-3pts for calculation error