

1	2	3	4	5	6	Total
/10	/10	/20	/20	/20	/20	/100

**DO NOT BEGIN THE EXAM
UNTIL YOU ARE TOLD TO
DO SO.**

PROBLEM ONE: (10 points)

A) State and describe Thevenin's Theorem.

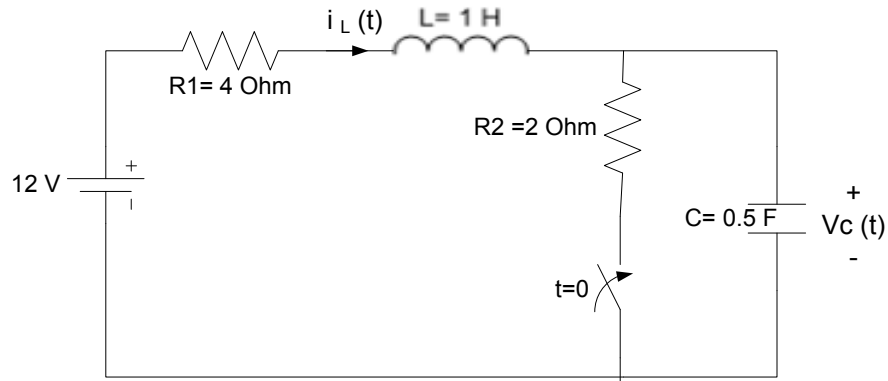
B) State and describe Norton's Theorem.

PROBLEM TWO(10 points):

Describe the concepts of complete response and transient response of linear RLC circuits.

PROBLEM THREE(20 points):

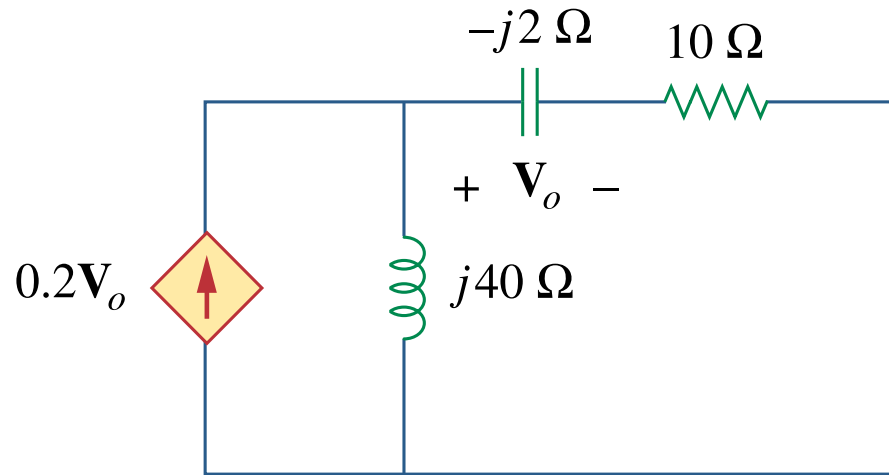
For the following circuit, the switch is closed at $t=0$. Find $v_c(t)$ and $i_L(t)$ for $t > 0$.



PROBLEM FOUR (20 points):

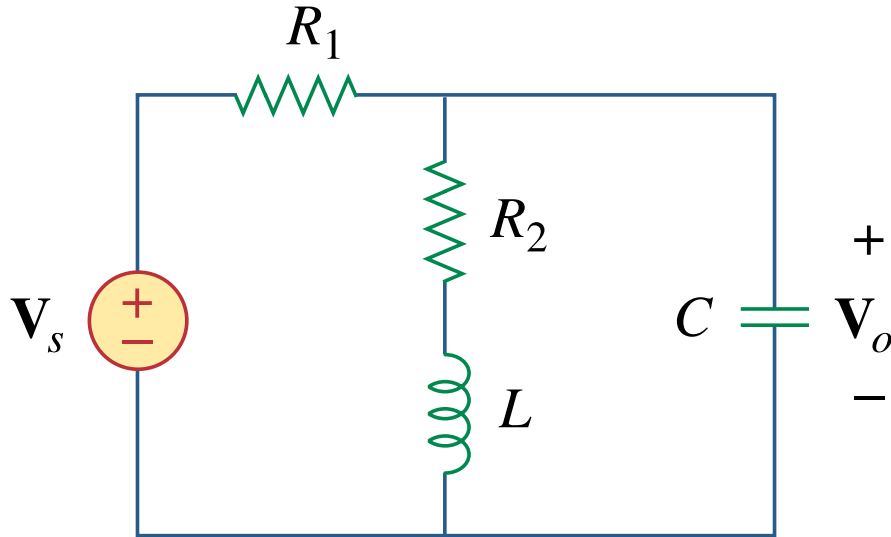
Calculate the output impedance of the circuit shown in the figure below.

Hint: Insert a 1-A current source at the output and find the voltage at the output, then the ratio.



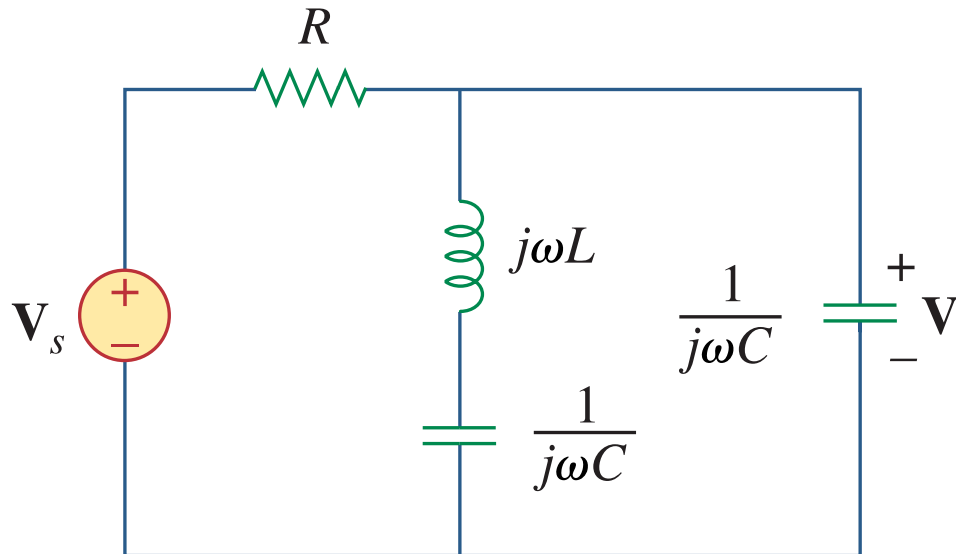
PROBLEM FIVE (20 points):

For the circuit in the figure below, determine the transfer function $H(\omega) = \mathbf{V}_o / \mathbf{V}_s$.



PROBLEM SIX(20 points):

Using nodal analysis obtain V in the circuit of the figure below.



Problem 1:

A) A linear two-terminal circuit can be replaced by an equivalent circuit consisting of a voltage source V_{Th} in series with a resistor R_{Th} , where V_{Th} is the open-circuit voltage at the terminals and R_{Th} is the input or equivalent resistance at the terminals when the independent sources are turned off.

B) A linear two-terminal circuit can be replaced by an equivalent circuit consisting of a current source I_N in parallel with a resistor R_N , where I_N is the short-circuit current through the terminals and R_N is the input or equivalent resistance at the terminals when the independent sources are turned off.

Grading criteria: 3 pts for equivalent circuit with a resistor and a source

5 pts for mentioning R_{Th} and V_{Th} in series

5 pts for mentioning R_N and I_N in parallel

Problem 2:

Complete response = transient response + steady-state response

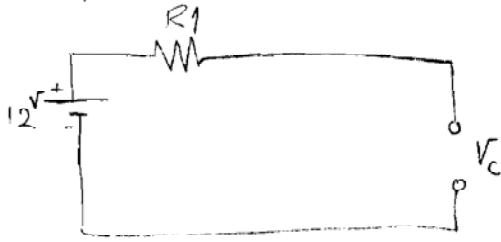
A complete response consists of a transient response (temporary response) and a steady-state response (permanent response). The transient response is the circuit's temporary response that will die out with time. And the steady-state response is the behavior of the circuit a long time after an external excitation is applied.

Grading criteria: 5 pts for mentioning transient and steady-state responses for the complete response

5 pts for temporary responses for the transient response

Problem 3:

$t < 0$:

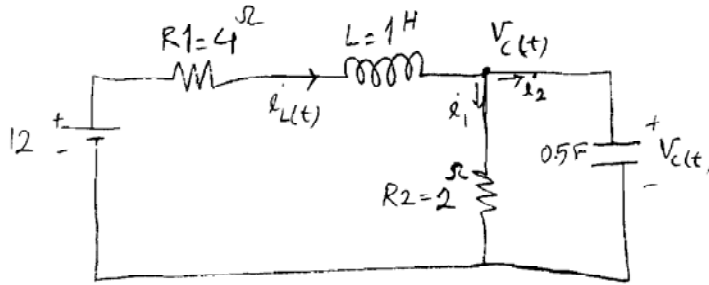


initial conditions:

$$i_L(0^-) = 0 = i_L(0^+)$$

$$V_C(0^-) = 12V = V_C(0^+)$$

$t > 0$:



$$i_L(t) = i_1 + i_2 \quad \text{: KCL}$$

$$i_L = \frac{V_C}{2} + 0.5 \frac{dV_C}{dt} \quad \text{(1)}$$

$$12V = 4i_L + V_L + V_C = 4i_L + 1 \cdot \frac{di_L}{dt} + V_C \quad \text{(2)}$$

$$\text{(1)} \xrightarrow{\frac{d}{dt}} \frac{di_L}{dt} = \frac{1}{2} \frac{dV_C}{dt} + 0.5 \frac{d^2V_C}{dt^2}$$

$$12V = 4 \left(\frac{V_C}{2} + 0.5 \frac{dV_C}{dt} \right) + \left(\frac{1}{2} \frac{dV_C}{dt} + 0.5 \frac{d^2V_C}{dt^2} \right) + V_C$$

$$\Rightarrow 12 = V_C + 2V_C + 2 \frac{dV_C}{dt} + \frac{1}{2} \frac{dV_C}{dt} + \frac{1}{2} \frac{d^2V_C}{dt^2} \Rightarrow \frac{d^2V_C}{dt^2} + 5 \frac{dV_C}{dt} + 6V_C = 12$$

$$\Rightarrow s^2 + 5s + 6 = 0 \rightarrow (s+2)(s+3) = 0 \Rightarrow s = -2 \ \& \ s = -3 \rightarrow \text{Overdamped}$$

$$\Rightarrow V_C(t) = A e^{-2t} + B e^{-3t} + V_{SS}$$

$$V_{SS} = V_C(t \rightarrow \infty) = \frac{2}{4+2} \times 12 = 4 \text{ V}$$

$$V_C(0) = 12 = A + B$$

$$\textcircled{1} \xrightarrow{t=0} i_L(0) = \frac{V_C(0)}{2} + 0.5 \left. \frac{dV_C}{dt} \right|_{t=0} \Rightarrow 0 = \frac{12}{2} + \frac{1}{2} [-2A - 3B] \Rightarrow 2A + 3B = 12$$

$$\begin{cases} A + B = 12 \\ 2A + 3B = 12 \end{cases} \Rightarrow \begin{cases} A = 24 \\ B = -12 \end{cases} \Rightarrow \boxed{V_C(t) = 24e^{-2t} - 12e^{-3t} + 4}$$

$$i_L(t) = \frac{1}{2} V_C(t) + \frac{1}{2} \frac{dV_C}{dt} = 12e^{-2t} - 6e^{-3t} + 2 + \frac{1}{2} [-48e^{-2t} + 36e^{-3t}]$$

$$\Rightarrow \boxed{i_L(t) = -12e^{-2t} + 12e^{-3t} + 2}$$

Grading criteria:

Initial conditions 4pts.

Writing correct KCL/KVL leading to correct second order equation and correct characteristic equation 6pts
(defining the Overdamped case 2pts).

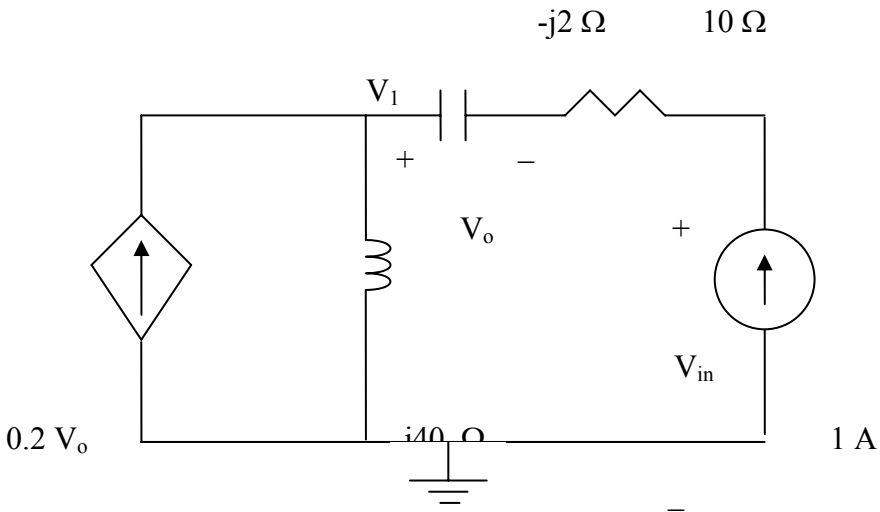
Finding $V_C(t)$ 5pts.

Finding $i_L(t)$ 5pts.

Any attempt 3pts.

Problem 4:

Insert a 1-A current source at the output as shown below.



$$0.2v_o + 1 = \frac{V_1}{j40}$$

$$\text{But } v_o = -1(-j2) = j2$$

$$j2 \times 0.2 + 1 = \frac{V_1}{j40} \longrightarrow V_1 = -16 + j40$$

$$V_{in} = V_1 - V_o + 10 = -6 + j38 = 1 \times Z_{in}$$

$$Z_{in} = \underline{\underline{-6 + j38 \Omega}}$$

Grading criteria:

Adding 1A source 2pts,

Finding V_o 4pts, KCL at the node (or KVL at loop) 5pts,

Finding V_{in} 5pts,

Mentioning $Z_{in} = V_{in}/1A$ and find Z_{in} 4pts.

Writing everything up to end of nodal without solving it 15 pts,

Any wrong attempt 3points

Problem 5:

Consider the circuit in the frequency domain as shown below.

$$\text{Let } \mathbf{Z} = (R_2 + j\omega L) \parallel \frac{1}{j\omega C}$$

$$\mathbf{Z} = \frac{\frac{1}{j\omega C}(R_2 + j\omega L)}{R_2 + j\omega L + \frac{1}{j\omega C}} = \frac{R_2 + j\omega L}{1 + j\omega R_2 - \omega^2 LC}$$

$$\frac{V_o}{V_s} = \frac{\mathbf{Z}}{\mathbf{Z} + R_1} = \frac{\frac{R_2 + j\omega L}{1 - \omega^2 LC + j\omega R_2 C}}{R_1 + \frac{R_2 + j\omega L}{1 - \omega^2 LC + j\omega R_2 C}}$$

$$\frac{V_o}{V_s} = \frac{R_2 + j\omega L}{R_1 + R_2 - \omega^2 LCR_1 + j\omega(L + R_1 R_2 C)}$$

Grading criteria:

Finding Z or writing related nodal 10 pts.

Writing correct voltage divider or solving the nodal correctly and find $H(\omega)$ 10pts.

Any attempt 5 pts.

Problem 6:

$$\frac{V - V_s}{R} + \frac{V}{j\omega L + \frac{1}{j\omega C}} + j\omega CV = 0$$

$$V + \frac{j\omega RCV}{-\omega^2 LC + 1} + j\omega RCV = V_s$$

$$\left(\frac{1 - \omega^2 LC + j\omega RC + j\omega RC - j\omega^3 RLC^2}{1 - \omega^2 LC} \right) V = V_s$$

$$V = \frac{(1 - \omega^2 LC)V_s}{1 - \omega^2 LC + j\omega RC(2 - \omega^2 LC)}$$

Grading criteria:

Writing correct nodal 10pts.

Arranging the nodal in regards to V and Vs 5pts.

Solving the equations and find V correctly 5pts.

Any attempt 5pts.