

Helpful constants for you:

$$c = 3 \cdot 10^8 \text{ m/s}$$

$$e = 1.6 \cdot 10^{-19} \text{ coulombs}$$

$$h = 6.63 \cdot 10^{-34} \text{ J-s}$$

$$m = 9.1 \cdot 10^{-31} \text{ kg}$$

$$k_B = 1.38 \cdot 10^{-23} \text{ J/K}$$

$$k_B T/e = 0.029 \text{ V at room temperature}$$

Schrodinger Equation:

$$i\hbar \frac{\partial}{\partial t} \Psi(\vec{r}, t) = -\frac{\hbar^2}{2m} \nabla^2 \Psi(\vec{r}, t) = -\frac{\hbar^2}{2m} \left( \frac{\partial^2}{\partial x^2} + \frac{\partial^2}{\partial y^2} + \frac{\partial^2}{\partial z^2} \right) \Psi(\vec{r}, t)$$

Drift-Diffusion:

$$\frac{\partial \delta n}{\partial t} = D_n \frac{\partial^2 \delta n}{\partial x^2} + \mu_n E \frac{\partial (\delta n)}{\partial x} - \frac{\delta n}{\tau} + G_n$$

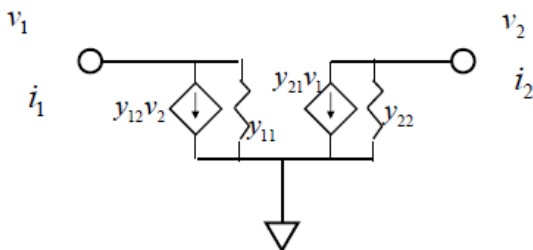
Fermi-Dirac:

$$P(E) = \frac{1}{e^{(E-E_f)/kT} + 1}$$

## Generalized $\pi$ model:

Regardless of which configuration you use, the following  $\pi$  model applies:

$$\begin{pmatrix} i_1 \\ i_2 \end{pmatrix} = \begin{pmatrix} y_{11} & y_{12} \\ y_{21} & y_{22} \end{pmatrix} \begin{pmatrix} v_1 \\ v_2 \end{pmatrix}$$



Common source: 1=gate, 2=drain  
 Common gate: 1=source, 2=drain  
 Common drain: 1=gate, 2= source

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$$U = \frac{|y_{21} - y_{12}|^2}{4[\operatorname{Re}(y_{11}) \cdot \operatorname{Re}(y_{22}) - \operatorname{Re}(y_{12}) \cdot \operatorname{Re}(y_{21})]}$$

$$E_g(\text{Al}_\xi\text{Ga}_{1-\xi}\text{As}) = \begin{cases} 1.424 + 1.247\xi & 0 \leq \xi \leq 0.45 \\ 1.900 + 0.125\xi + 0.143\xi^2 & \xi > 0.45 \end{cases} \quad (1-88)$$

$$\Delta E_v(\xi) = 0.55\xi \quad (\text{in eV}) \quad (1-89)$$

$$\Delta E_c(\xi) = \begin{cases} (1.247 - 0.55)\xi & 0 \leq \xi \leq 0.45 \\ 0.476 + (0.125 - 0.55)\xi + 0.143\xi^2 & \xi > 0.45 \end{cases} \quad (\text{in eV}) \quad (1-90)$$

## HETEROJUNCTION PARAMETERS AT ROOM TEMPERATURE

	$\text{Al}_{0.3}\text{Ga}_{0.7}\text{As}/\text{GaAs}$	$\text{Ga}_{0.51}\text{In}_{0.49}\text{P}/\text{GaAs}$	$\text{InP}/\text{In}_{0.53}\text{Ga}_{0.47}\text{As}$	$\text{In}_{0.52}\text{Al}_{0.48}\text{As}/\text{In}_{0.53}\text{Ga}_{0.47}\text{As}$	$\text{Si}/\text{Si}_{0.8}\text{Ge}_{0.2}$
$\Delta E_g$ (eV)	0.37	Ordered: 0.43 Disordered: 0.46	0.60	0.71	Unstrained: 0.078 Strained: 0.165
$\Delta E_c$ (eV)	0.24	Ordered: 0.03 Disordered: 0.22	0.23	0.50	
$\Delta E_v$ (eV)	0.13	Ordered: 0.40 Disordered: 0.24	0.37	0.21	
$s$ (cm/s)	103	2-200			

## SEMICONDUCTOR MATERIAL PARAMETERS AT ROOM TEMPERATURE

	GaAs	$\text{Al}_{0.3}\text{GaAs}$	$\text{Ga}_{0.51}\text{InP}$	InP	$\text{In}_{0.53}\text{GaAs}$	$\text{In}_{0.52}\text{AlAs}$	Si
$\epsilon_r$	13.1	~12.2	~11.9	12.6	~14.0	~12.5	11.9
$N_c$ ( $\text{cm}^{-3}$ )	$4.7 \times 10^{17}$	—	—	$5.8 \times 10^{17}$	$\sim 2.8 \times 10^{17}$	—	$2.8 \times 10^{19}$
$N_v$ ( $\text{cm}^{-3}$ )	$7.0 \times 10^{18}$	—	—	$1.0 \times 10^{19}$	$\sim 6.0 \times 10^{18}$	—	$1.04 \times 10^{19}$
$n_i$ ( $\text{cm}^{-3}$ )	$1.79 \times 10^6$	—	—	$1.05 \times 10^7$	$6.31 \times 10^{11}$	—	$1.45 \times 10^{10}$
$E_g$ (eV)	1.424 (direct)	1.80 (direct)	1.86 (direct)	1.35 (direct)	0.75 (direct)	1.46 (direct)	1.12 (indirect)
$E_{T-L}$ (eV)	0.28	0.10	0.15	0.61	0.55	0.54	—
$m_n^*/m_0$	0.067	0.092	0.099	0.078	0.041	0.074	0.26
$k_{TH}$ (W/cm $^2$ ·C)	0.46	0.12	0.05	0.68	0.05	—	1.5
$s$ (cm/s)	$1 \times 10^6$	$1 \times 10^6$	—	—	$1 \times 10^3$	—	$1 \times 10^3$
$\tau_n$ (s)	$1 \times 10^{-9}$	—	—	—	—	—	$1 \times 10^{-6}$
$\mu_n$ (cm $^2$ /V·s)	4000	1400	1000	3200	7000	900	800
$\mu_p$ (cm $^2$ /V·s)	250	130	75	150	300	180	400
$v_{sat}$ (cm/s)	$8 \times 10^6$	—	$4.4 \times 10^6$	$1.5 \times 10^7$	$7 \times 10^6$	$6 \times 10^6$	$8 \times 10^6$

Note: When the parameter value of a material (such as  $\text{Al}_{0.3}\text{Ga}_{0.7}\text{As}$ ) is obtained by linearly extrapolating between two extreme materials (such as AlAs and GaAs), an approximate sign is placed in front. All of the values are room-temperature values. Electron mobilities are taken at  $N_d = 1 \times 10^{17} \text{ cm}^{-3}$ . All mobility values are majority carrier values.

$$z' = z/R_0, \quad y' = y/R_0, \quad A_{11}' = A_{11}/R_0, \quad A_{12}' = A_{12}/R_0, \quad A_{21}' = A_{21}/R_0, \quad A_{22}' = A_{22}/R_0,$$

$$B_{11}' = \frac{(z_{11}' - 1)(z_{22}' + 1) + z_{12}' z_{21}'}{(z_{11}' + 1)(z_{22}' + 1) + z_{12}' z_{21}'}, \quad B_{12}' = \frac{(1 - A_{11})(1 + A_{22}) + A_{12} A_{21}}{(1 + A_{11})(1 + A_{22}) - A_{12} A_{21}},$$

$$B_{21}' = \frac{(1 + A_{11})(1 - A_{22}) + A_{12} A_{21}}{(1 + A_{11})(1 + A_{22}) - A_{12} A_{21}}, \quad B_{22}' = \frac{(z_{11}' + 1)(z_{22}' - 1) + z_{12}' z_{21}'}{(z_{11}' + 1)(z_{22}' + 1) + z_{12}' z_{21}'},$$

$$C_{11}' = \frac{2A_{12}}{(z_{11}' + 1)(z_{22}' + 1) + z_{12}' z_{21}'}, \quad C_{12}' = \frac{-2A_{11}}{(1 + A_{11})(1 + A_{22}) - A_{12} A_{21}},$$

$$C_{21}' = \frac{-2A_{22}}{(1 + A_{11})(1 + A_{22}) - A_{12} A_{21}}, \quad C_{22}' = \frac{2A_{21}}{(z_{11}' + 1)(z_{22}' + 1) + z_{12}' z_{21}'},$$

$$D_{11}' = \frac{(1 - A_{11})(1 + A_{22}) + A_{12} A_{21}}{(1 + A_{11})(1 + A_{22}) - A_{12} A_{21}}, \quad D_{12}' = \frac{y_{11}'}{z_{11} z_{22} - z_{21} z_{12}},$$

$$D_{21}' = \frac{-z_{12}}{z_{11} z_{22} - z_{21} z_{12}}, \quad D_{22}' = \frac{-y_{12}}{y_{11} y_{22} - y_{21} y_{12}},$$

$$E_{11}' = \frac{-2A_{12}}{(1 + A_{11})(1 + A_{22}) - A_{12} A_{21}}, \quad E_{12}' = \frac{z_{11}}{z_{11} z_{22} - z_{21} z_{12}},$$

$$E_{21}' = \frac{-z_{21}}{z_{11} z_{22} - z_{21} z_{12}}, \quad E_{22}' = \frac{y_{11}}{y_{11} y_{22} - y_{21} y_{12}},$$

$$F_{11}' = \frac{(1 + A_{11})(1 - A_{22}) + A_{12} A_{21}}{(1 + A_{11})(1 + A_{22}) - A_{12} A_{21}}, \quad F_{12}' = \frac{y_{12}}{z_{11} z_{22} - z_{21} z_{12}},$$

$$F_{21}' = \frac{z_{12}}{z_{11} z_{22} - z_{21} z_{12}}, \quad F_{22}' = \frac{-y_{11}}{y_{11} y_{22} - y_{21} y_{12}},$$

$$G_{11}' = \frac{A_{11} z_{11} z_{22} - z_{21} z_{12}}{z_{22}}, \quad G_{12}' = \frac{z_{12}}{z_{22}},$$

$$G_{21}' = \frac{-z_{21}}{z_{22}}, \quad G_{22}' = \frac{-y_{11}}{z_{22}},$$

$$H_{11}' = \frac{1}{y_{11}}, \quad H_{12}' = \frac{1}{y_{11}},$$

$$H_{21}' = \frac{A_{12} - A_{22} A_{21}}{A_{22}}, \quad H_{22}' = \frac{1}{y_{11}},$$

$$I_{11}' = \frac{-A_{12}}{A_{11}}, \quad I_{12}' = \frac{-y_{12}}{y_{11}},$$

$$I_{21}' = \frac{-A_{22}}{A_{11}}, \quad I_{22}' = \frac{-y_{11}}{y_{11}},$$

$$J_{11}' = \frac{A_{12} A_{21} - A_{11} A_{22}}{A_{11}}, \quad J_{12}' = \frac{A_{22} - A_{12} A_{21}}{A_{11}},$$

$$J_{21}' = \frac{A_{12} - A_{11} A_{22}}{A_{11}}, \quad J_{22}' = \frac{y_{12} z_{22} - y_{21} z_{12}}{y_{11}}$$

FIGURE 4-17. Conversion table between the  $s$ ,  $y$ ,  $z$ ,  $s'$ , and  $h$ -parameters.