

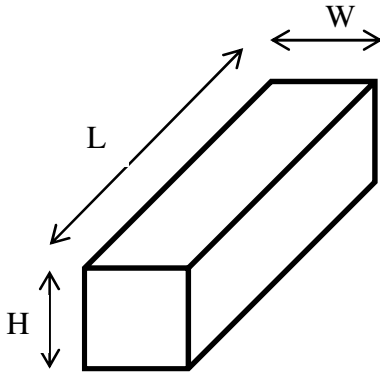
1	2	3	4	Total
/25	/25	/25	/25	/100

**DO NOT BEGIN THE EXAM
UNTIL YOU ARE TOLD TO
DO SO.**

PROBLEM ONE: (25 points)

A Silicon bar at room temperature is doped with $N_A = 10^{17} \text{ cm}^{-3}$ and $N_D = 0$.

Calculate the Resistance in (Ω) of the bar with $L = 100\mu\text{m}$ and Height = Width = $1\mu\text{m}$.

**Solution:**

$$R = \rho \frac{l}{A}$$

8 pts for writing correct formula.

From the resistivity chart, $\rho \approx 0.2 \Omega\text{-cm}$ for $N_A = 10^{17} \text{ cm}^{-3}$ 7 pts for correct approximation
Acceptable range (0.1 to 0.3)

$$R = 0.2 \Omega\text{-cm} \frac{100\mu\text{m}}{(1\mu\text{m})^2} = 200\text{k}\Omega$$

10pts for correct set up calculation

Acceptable range (150k to 250k)

PROBLEM TWO(25 points):

From problem #1, Find $E_C - E_F$ and $E_F - E_V$. Sketch the Band Diagram and indicate your findings.

Solution:

$$E_i - E_F = kT \ln(N_A / n_i) = 0.0259 \ln(10^7) = 0.417 eV$$

2pts for correct equation

2pts for correct natural log approximation

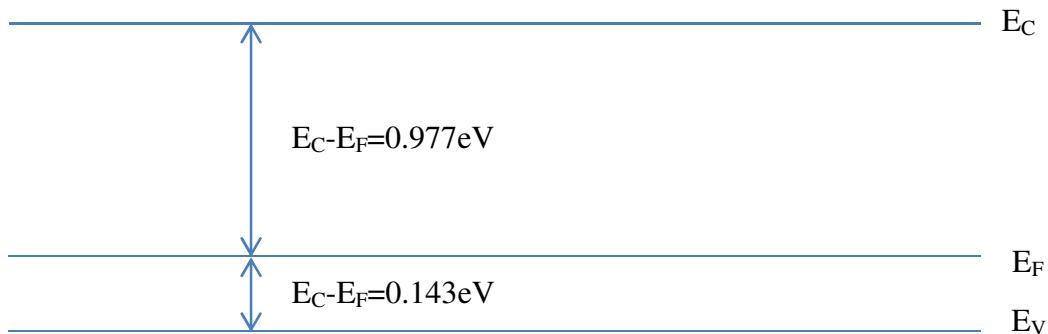
2pts for correct answer : Acceptable range (0.4 to 0.5)

$$E_C - E_F = Eg / 2 + (E_i - E_F) = 0.56 + 0.417 = 0.977 eV$$

6pts for correct $E_C - E_F$ Acceptable range (0.85 to 0.99)

$$E_F - E_V = Eg - (E_C - E_F) = 1.12 eV - 0.977 eV = 0.143 eV$$

6pts for correct $E_F - E_V$ Acceptable range (0.1 to 0.25)



3.5 pts for correct $E_C - E_F$ Drawing. Acceptable range (0.85 to 0.99)

3.5 pts for correct $E_F - E_V$ Drawing. Acceptable range (0.1 to 0.25)

PROBLEM THREE(25 points):

Given Silicon at room temperature with $E_C - E_F = 0.3eV$ and same geometry as problem #1. Calculate:

- the electron concentration (n in cm^{-3})
- hole concentration (p in cm^{-3})
- resistivity (ρ in $\Omega\text{-cm}$)
- majority carrier mobility (μ in $cm^2/V\text{-s}$)
- dopant concentration (in cm^{-3})

Solution:

a)

$$E_C - E_F = 0.3eV$$

$$E_F - E_i = 0.56eV - 0.3eV = 0.26eV$$

$$E_F - E_i = kT \ln(n / n_i) = 0.0259 \ln(n / 10^{10}) \quad \text{5pts for setting for } E_F - E_i \text{ equation}$$

$$n = 2.289 * 10^{14} cm^{-3}$$

Acceptable range (10^{14} - $9.9 * 10^{14}$)

b)

$$p = n_i^2 / n = 4.368 * 10^5 cm^{-3}$$

5pts for correct answer.

Acceptable range (10^4 - $9.9 * 10^4$)

c), d), e)

$$\text{With } n \gg p, N_D \approx n = 2.289 * 10^{14} cm^{-3}$$

5pts for correct assumption.

$$\mu_n \approx 1500 cm^2 / V * s \text{ from the mobility chart.}$$

5pts for correct approximation.

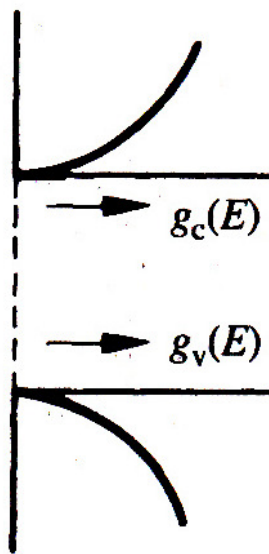
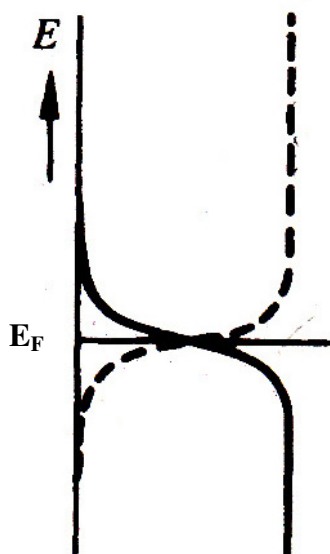
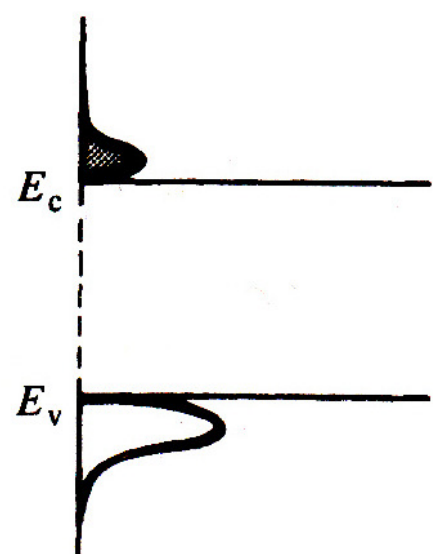
Acceptable range (1000-2000)

$$\rho = \frac{1}{q\mu_n N_D} = \frac{1}{1.6 * 10^{-19} * 1500 * 2.289 * 10^{14}} = 18.2 \Omega\text{-cm} \quad \text{5pts for correct resistivity}$$

Acceptable range (10-30)

PROBLEM FOUR(25 points):

Sketch the probability distribution function $f(E)$ for electrons, $1-f(E)$ for holes, density of states $g_c(E)$ for electrons, $g_v(E)$ for holes, and the energy distribution of carriers $f(E)*g_c(E)$ for electrons and $g_v(E)*(1-f(E))$ for holes problem #1.

Density of States**Probability distribution function****Energy distribution of carriers**

5pts for correct drawing of $g_c(E)$ for electrons.

5pts for correct drawing of $g_v(E)$ for holes.

5pts for correct drawing of $f(E)$ and $1-f(E)$ note* (if you did not draw $1-f(E)$, at least make some sort of mention of it on the plot for answer to be accepted)

5pts for correct drawing of $f(E)*g_c(E)$

5pts for correct drawing of $g_v(E)*(1-f(E))$