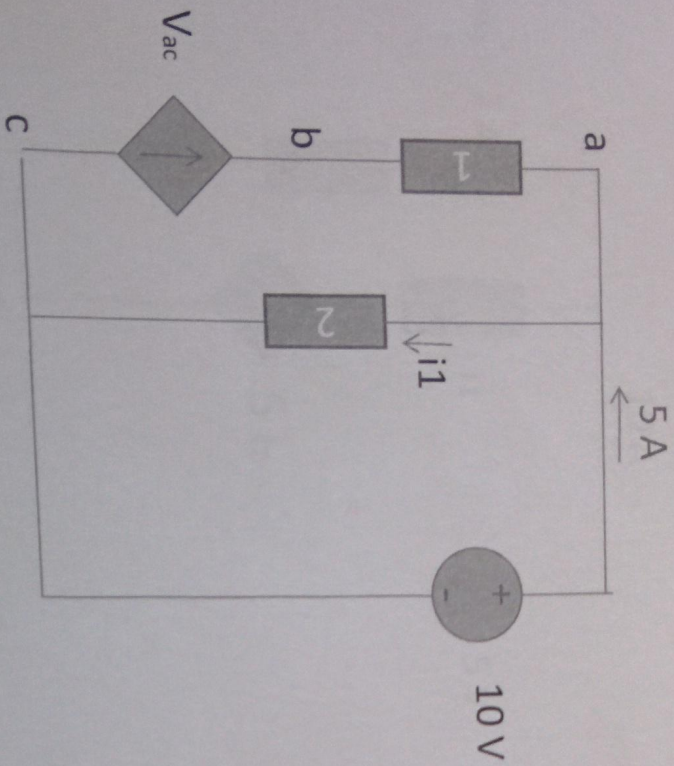


Problem 1: (VCCS) Find i_1 . Is current flowing from b to c or from c to b?



$$V_{ac} = 10V$$

Given the direction of current flow

in VCCS,

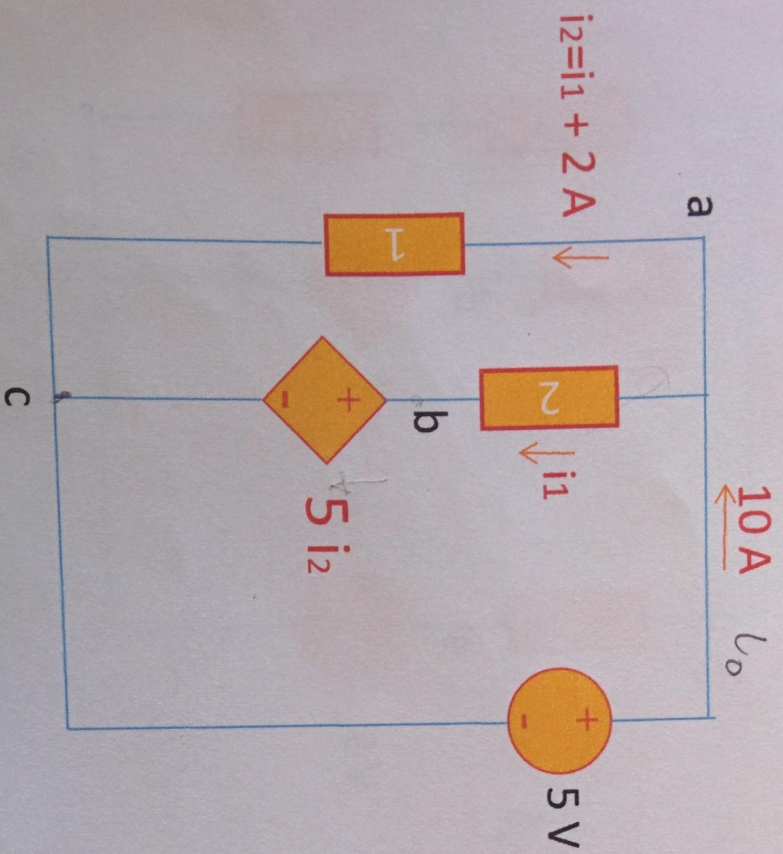
@ node a,

$$5 + 10 = i_1'$$

$$i_1' = 15A$$

The current flows from c to b.

Problem 2 : (CCVS) Find i_1 , i_2 . Find V_{bc}



$$I_0 = i_2 + i_1$$

$$10A = i_1 + (i_1 + 2A)$$

$$10A = 2i_1 + 2A$$

$$8A = 2i_1$$

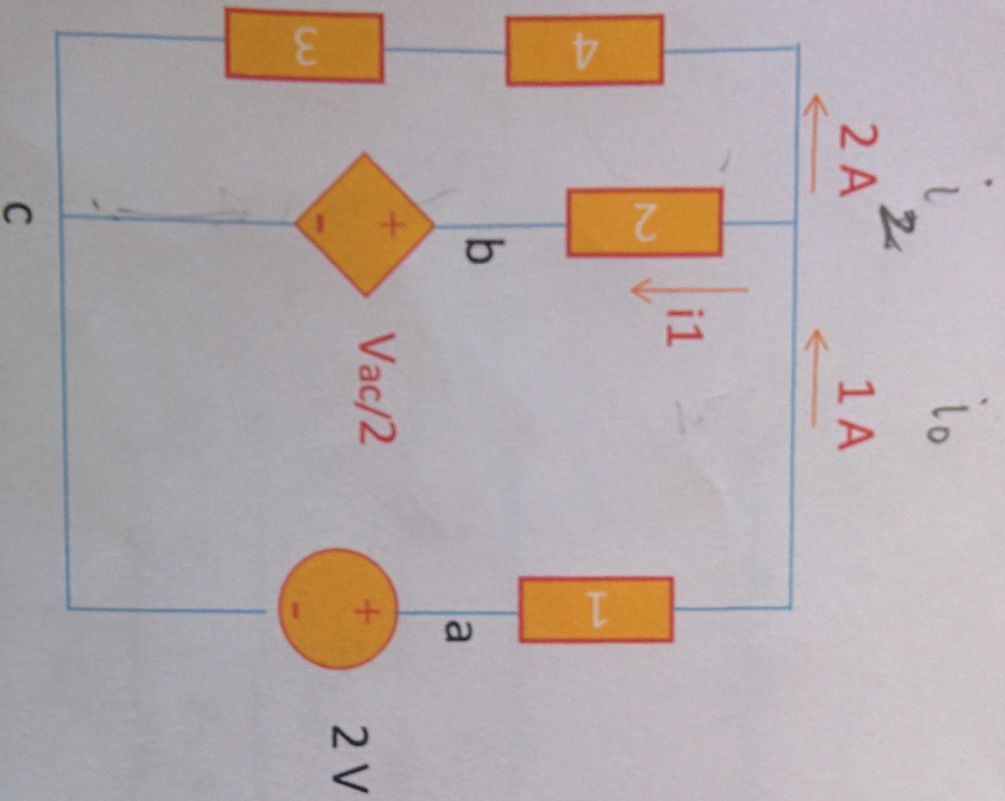
$$i_1 = 4A$$

$$i_2 = 6A$$

$$V_{bc} = 5i_2 = 5(6A) = 30V$$

$$V_{bc} = 30V$$

Problem 3: (VCVS) Find V_{bc} , i_1 .



$$i_0 = i_2 + i_1$$

$$i_0 = i_2 + i_1$$

$$1A = 2A + i_1$$

$$-1A = i_1$$

$$i_1 = -1A$$

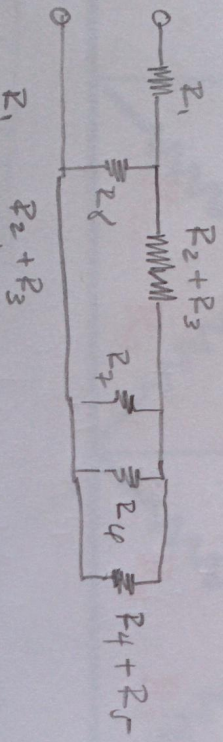
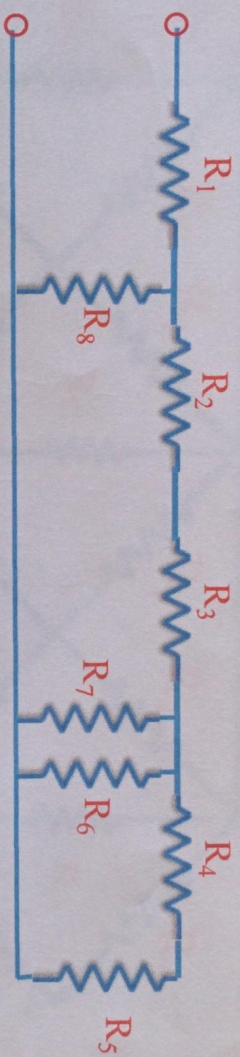
$$V_{bc} = \frac{V_{ac}}{2} = \frac{2V}{2} = 1V$$

$$V_{bc} = 1V$$

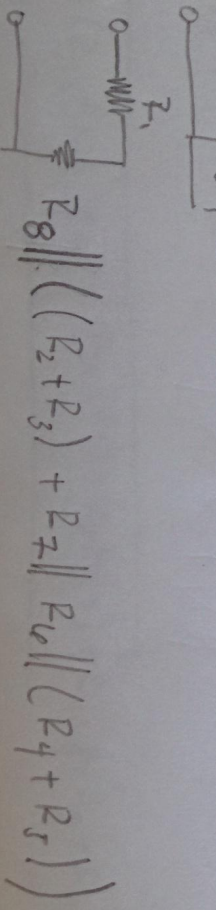
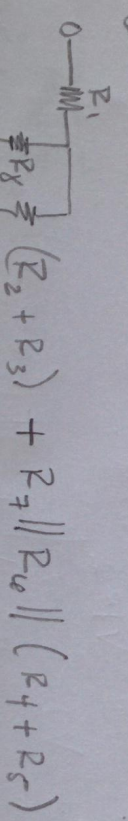
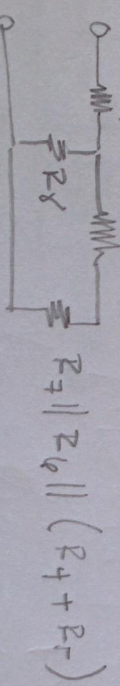
OR

$$V_{bc} = 1V$$

Problem 4: Solve for Req. You may use the parallel notation discussed in class

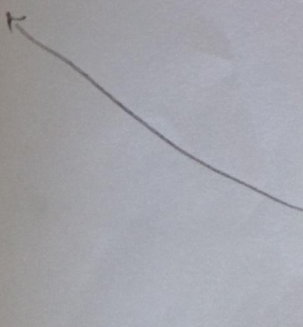


$$R_{eq} = \left[\left((R_4 + R_5) \parallel R_6 \parallel R_7 \right) + R_2 + R_3 \right] \parallel R_8 + R_1$$



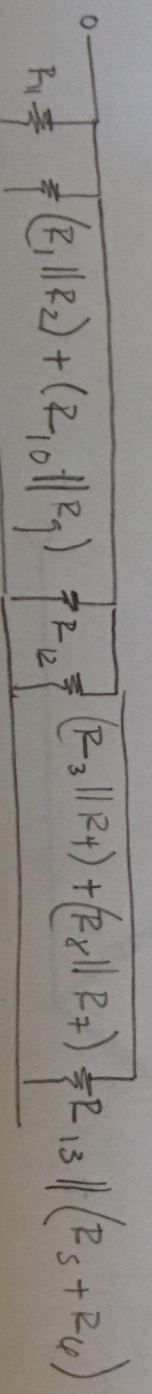
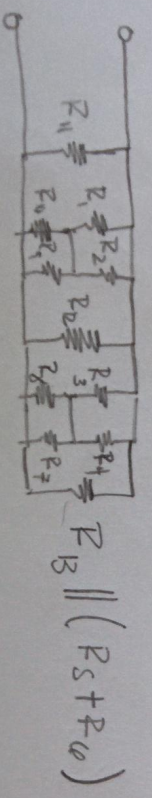
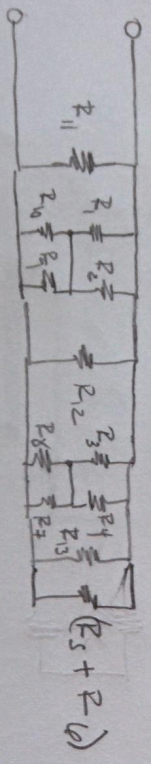
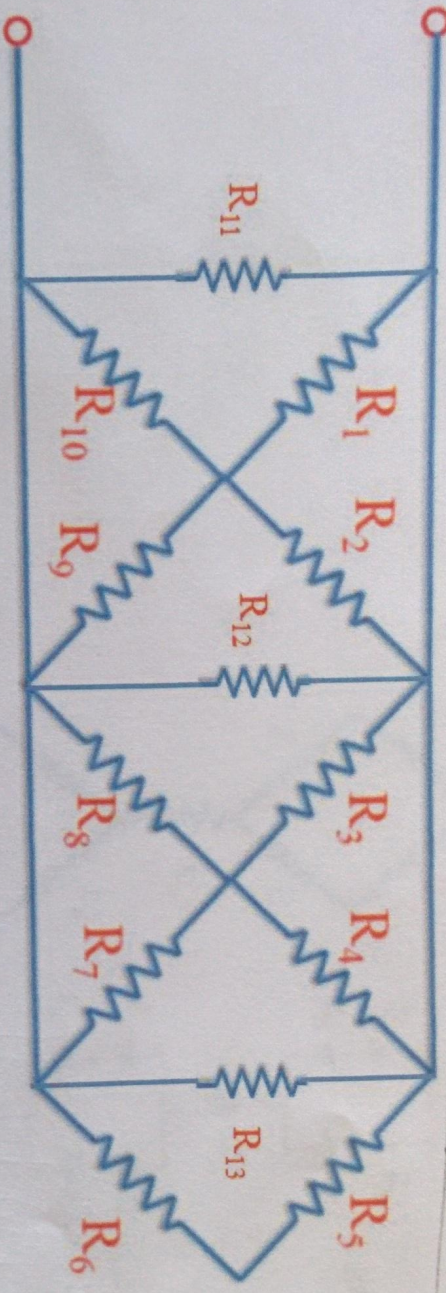
$$R_{eq} = R_1 + \left(R_8 \parallel \left((R_2 + R_3) + R_7 \parallel R_6 \parallel (R_4 + R_5) \right) \right)$$

OR



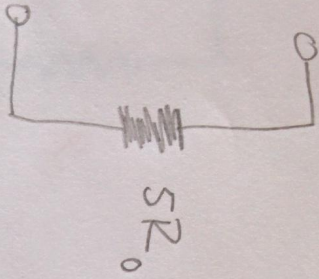
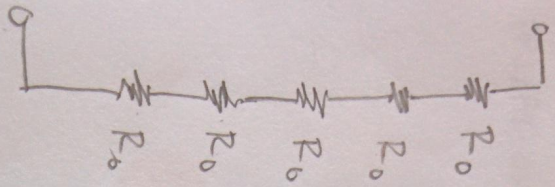
Problem 5: Solve for Req. You may use the parallel notation discussed in class.

$$R_{eq} = R_{11} \parallel \left[(R_1 \parallel R_2) + (R_9 \parallel R_{10}) \right] \parallel R_{12} \parallel \left[(R_3 \parallel R_4) + (R_7 \parallel R_8) \right] \parallel \left[R_{13} \parallel (R_5 + R_6) \right]$$

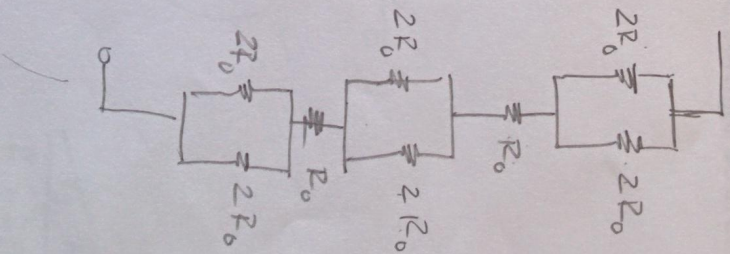
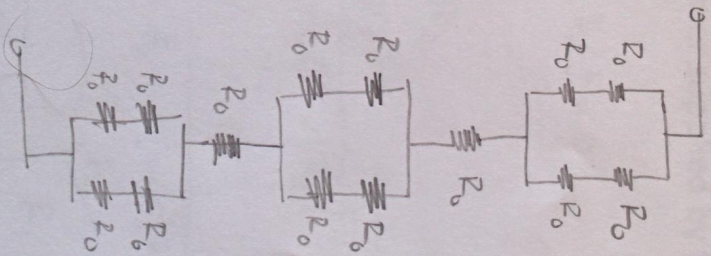
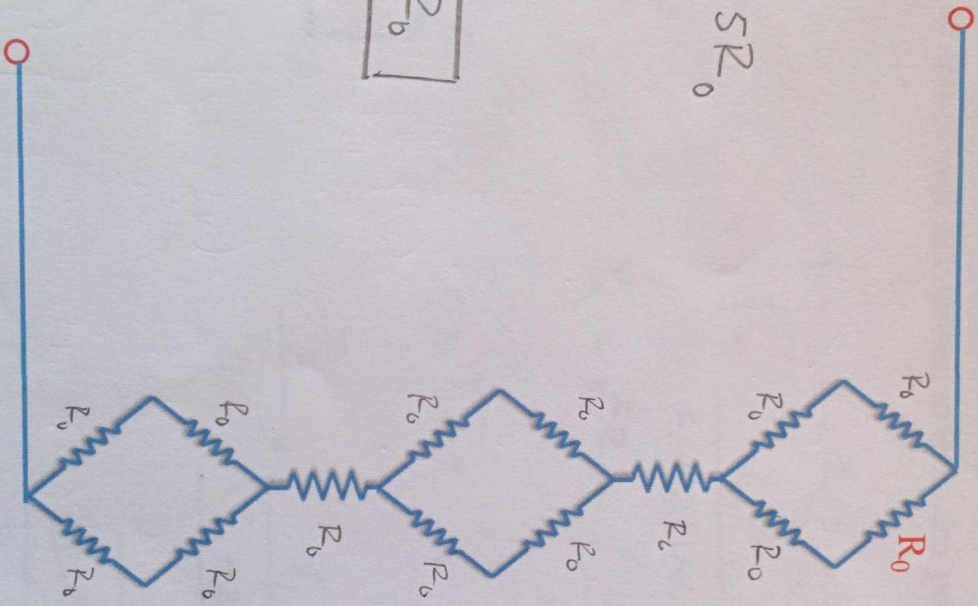


$$R_{eq} = R_{11} \parallel \left((R_1 \parallel R_2) + (R_{10} \parallel R_9) \right) \parallel \left((R_3 \parallel R_4) + (R_8 \parallel R_7) \right) \parallel \left(R_{13} \parallel (R_5 + R_6) \right)$$

Problem 6: Solve for Req. Each resistor is R0 ohms.



$$R_{eq} = 5R_0$$



$$\frac{1}{2R_0} + \frac{1}{2R_0}$$

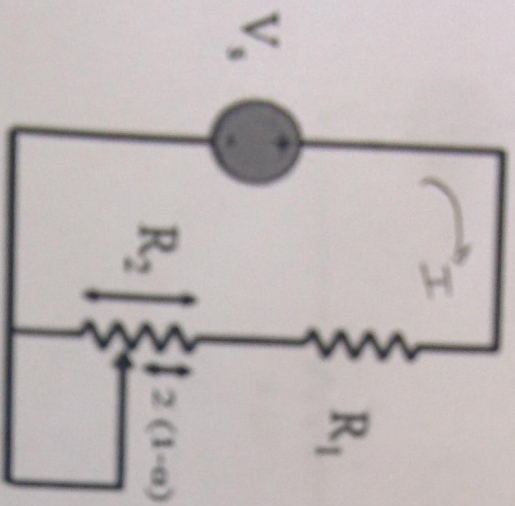
$$\frac{2}{2R_0} = \frac{1}{R_0}$$

$$R_{eq} = R_0$$

$$R_{eq} = 5R_0$$

Problem 7: Potentiometer.

In the circuit below, the wiper divides the potentiometer resistance between $2(1-a)R_2$ and $2aR_2$, where $0 < a < 1$. Find the ratio of the power dissipated in R_1 to the power supplied by the voltage source (P_{R_1}/P_S) as a function of a .



Applying KVL,

$$-V_s + I(R_1 + 2(1-a)R_2) = 0$$

$$\text{or } I = \frac{V_s}{R_1 + 2(1-a)R_2}$$

$$R_1 + 2(1-a)R_2$$

$$V_{R_1} = I R_1 = \frac{V_s \cdot R_1}{R_1 + 2(1-a)R_2}$$

$$R_1 + 2(1-a)R_2$$

$$P_{R_1} = V_{R_1} \cdot I$$

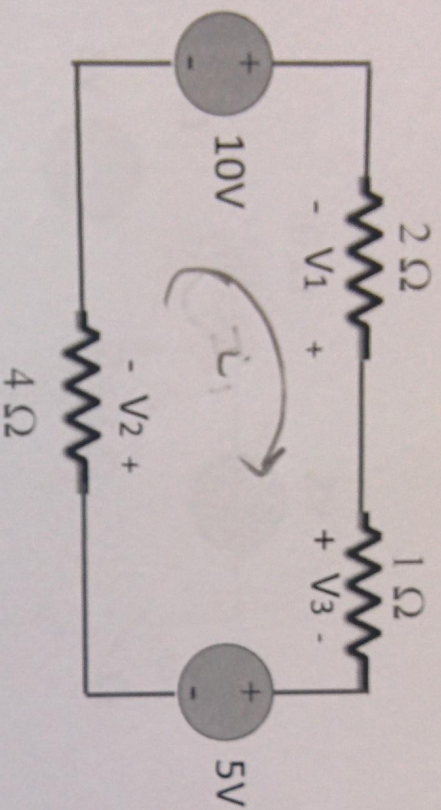
$$P_S = V_s \cdot I$$

$$\frac{P_{R_1}}{P_S} = \frac{V_{R_1} \cdot I}{V_s \cdot I} = \frac{V_s \cdot R_1}{R_1 + 2(1-a)R_2} \cdot \frac{1}{V_s}$$

$$= \frac{R_1}{R_1 + 2(1-a)R_2}$$

$$R_1 + 2(1-a)R_2$$

Problem 8: KVL & Ohm law. Find V_1 , V_2 and V_3 and the current flowing in the circuit below



Applying KVL,

$$-10 + 2 \cdot i + 1 \cdot i + 5 + 4 \cdot i = 0$$

$$\therefore 7i = 5$$

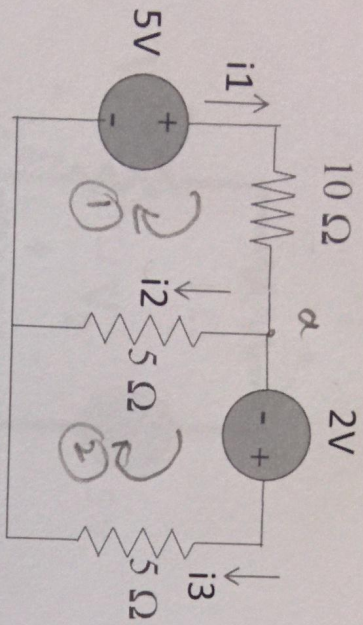
$$i = \frac{5}{7} \text{ A}$$

$$V_1 = -2 \cdot i = -\frac{10}{7} \text{ V}$$

$$V_2 = 4 \cdot i = \frac{20}{7} \text{ V}$$

$$V_3 = 1 \cdot i = \frac{5}{7} \text{ V}$$

Problem 9: KVL, KCL & Ohm Law.
Find i_1 through i_3 in the circuit below.



① node a

$$i_1 = i_2 + i_3$$

① $-5 + 10i_1 + 5i_2 = 0$

② $10i_1 + 5i_2 = 5$ -

③ $-2 + 5i_3 - 5i_2 = 0$

$5i_3 - 5i_2 = 2$ -

substituting for i_1 in ①

$15i_2 + 10i_3 = 5$ -

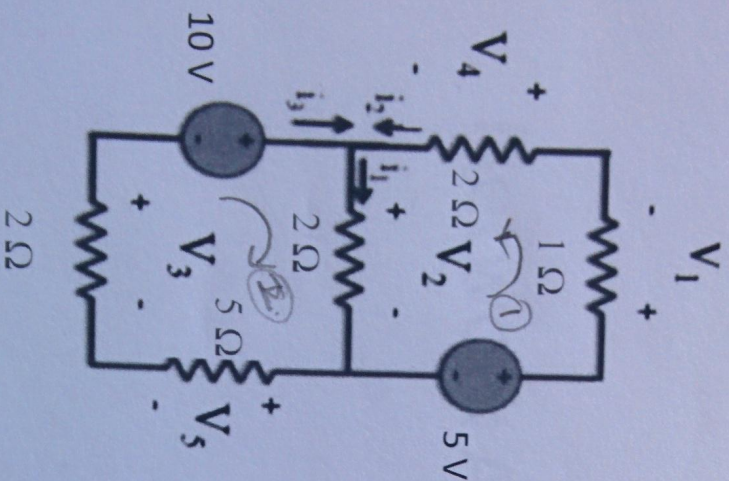
solving equations ② & ③

we get $i_2 = 0.04 \text{ A}$

$i_3 = 0.44 \text{ A}$

$i_1 = 0.48 \text{ A}$

Problem 10: KVL, KCL & Ohm Law.
Find V_1 through V_4 and i_1 through i_3 in the circuit below.



$$i_1 = i_2 + i_3$$

Applying KVL in loop ①.

$$-5 + 1 \cdot i_2 + 2 \cdot i_2 + 2 \cdot i_1 = 0$$

$$2i_1 + 3i_2 = 5$$

substituting for i_1 ,

$$5i_2 + 2i_3 = 5 \quad \text{--- (a)}$$

$$-10 + 2i_1 + 5i_3 + 2i_3 = 0$$

$$2i_1 + 7i_3 = 10 \quad \text{--- (b)}$$

Substituting for i_1 ,

$$2i_2 + 9i_3 = 10 \quad \text{--- (c)}$$

Solving (a) or (c)

$$i_2 = 0.609 \Rightarrow i_1 = 1.584$$

$$i_3 = 0.975$$

$$\begin{aligned} V_1 &= 1 \cdot i_2 = 0.609 \text{ V} \\ V_2 &= 2 \cdot i_1 = 3.168 \text{ V} \\ V_3 &= -2 \cdot i_3 = -1.95 \text{ V} \\ V_4 &= 2 \cdot i_2 = 1.218 \text{ V} \\ V_5 &= 5 \cdot i_3 = 4.875 \text{ V} \end{aligned}$$