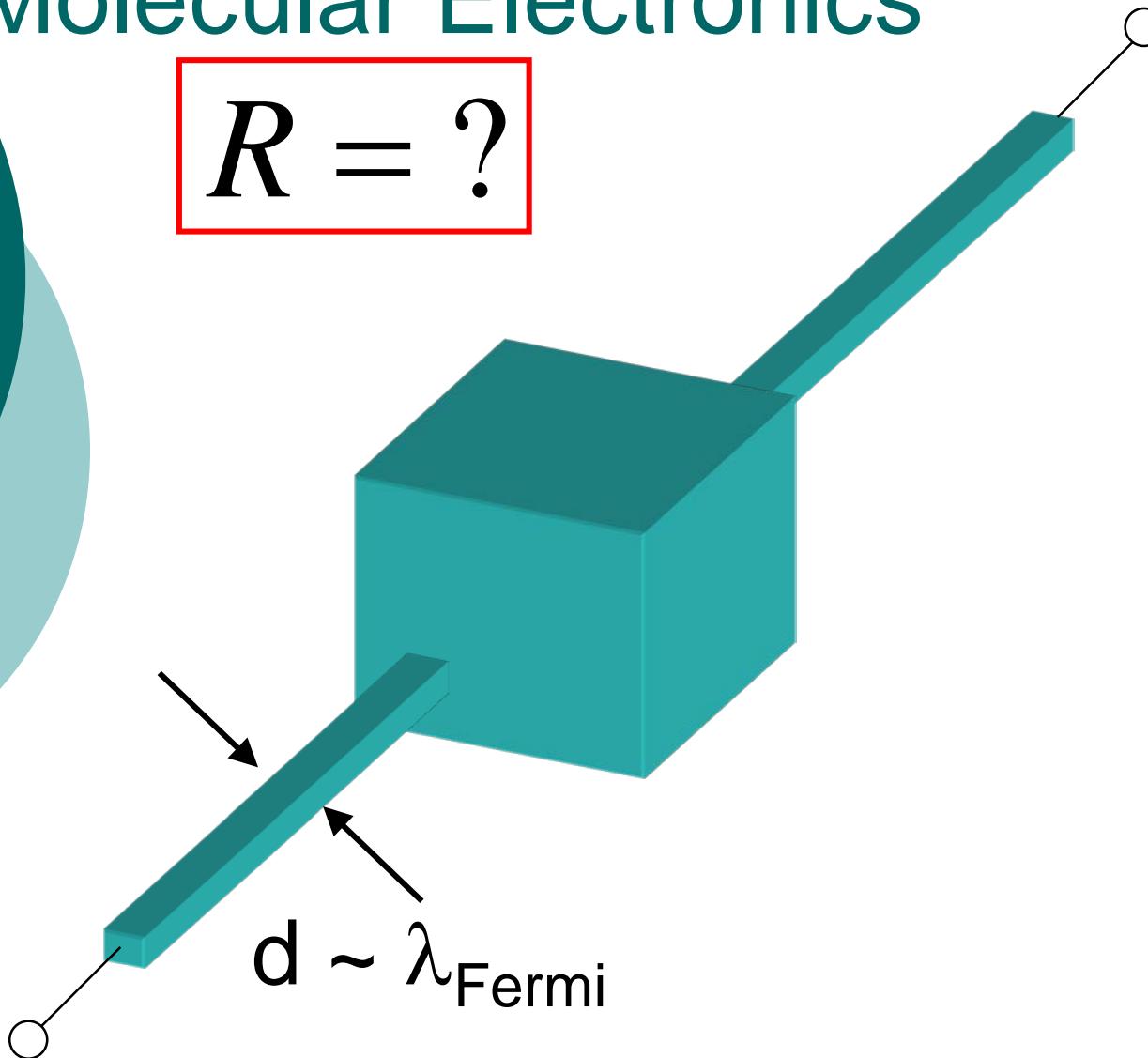


# Lecture 12: Quantum dots and Molecular Electronics

$$R = ?$$

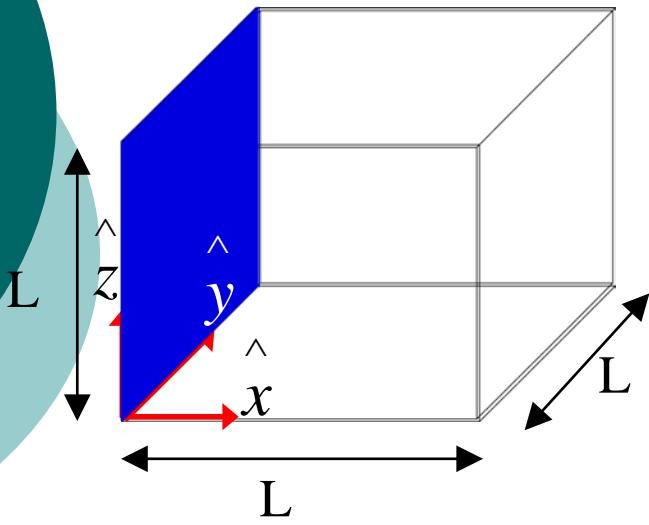


# Readings that cover this lecture

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- Ferry, pp. 209-226
- Hanson, pp. 125-127

# Particle in a box



We can do the same for y, z:

$$\psi(\vec{r}) = (2i)^3 A \cdot \sin(k_{n_x} x) \cdot \sin(k_{n_y} y) \cdot \sin(k_{n_z} z)$$

$$k_{n_x} = n_x \pi / L$$

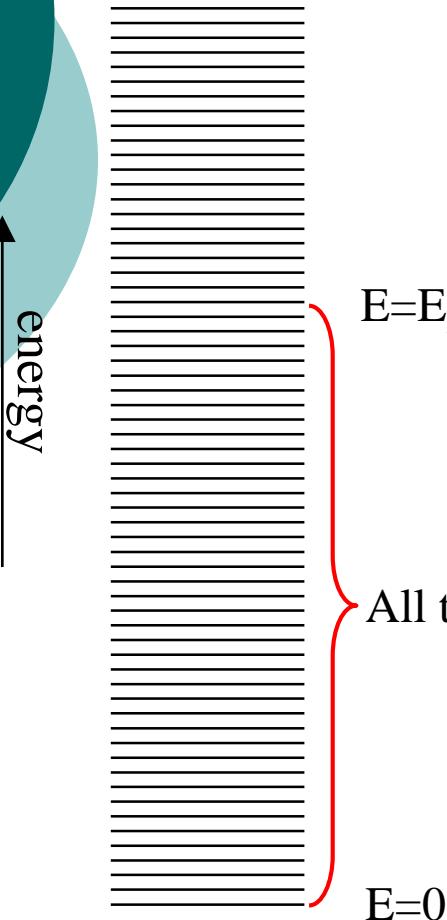
$$k_{n_y} = n_y \pi / L$$

$$k_{n_z} = n_z \pi / L$$

$$E = \frac{\hbar^2 (k_{n_x}^2 + k_{n_y}^2 + k_{n_z}^2)}{2m} = \frac{\hbar^2 (\pi/L)^2}{2m} (n_x^2 + n_y^2 + n_z^2)$$

These are the allowed energy levels, or “quantum states”

# Fermi gas

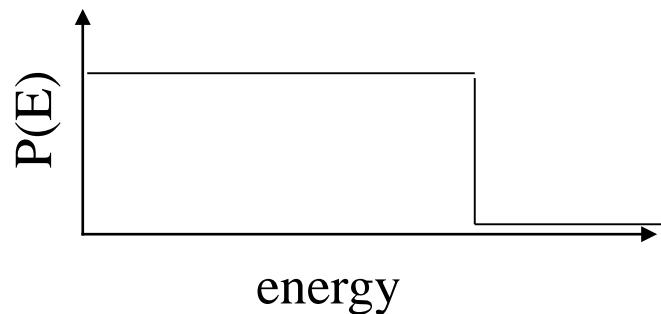


At zero temperature, as we add electrons to the box, we gradually fill up all the states.  
**(DISCUSS PAULI EXCLUSION PRINCIPLE -IMPORTANT!)**

When we are done filling the box, the energy of the last electron is called the “Fermi energy.”

“Gas” means we neglect electron-electron interactions.

All these states are filled with electrons.



# Particle in a box

$$\psi(\vec{r}) = (2i)^3 A \cdot \sin(k_{n_x} x) \cdot \sin(k_{n_y} y) \cdot \sin(k_{n_z} z)$$



$$k_{n_x} = n_x \pi / L$$

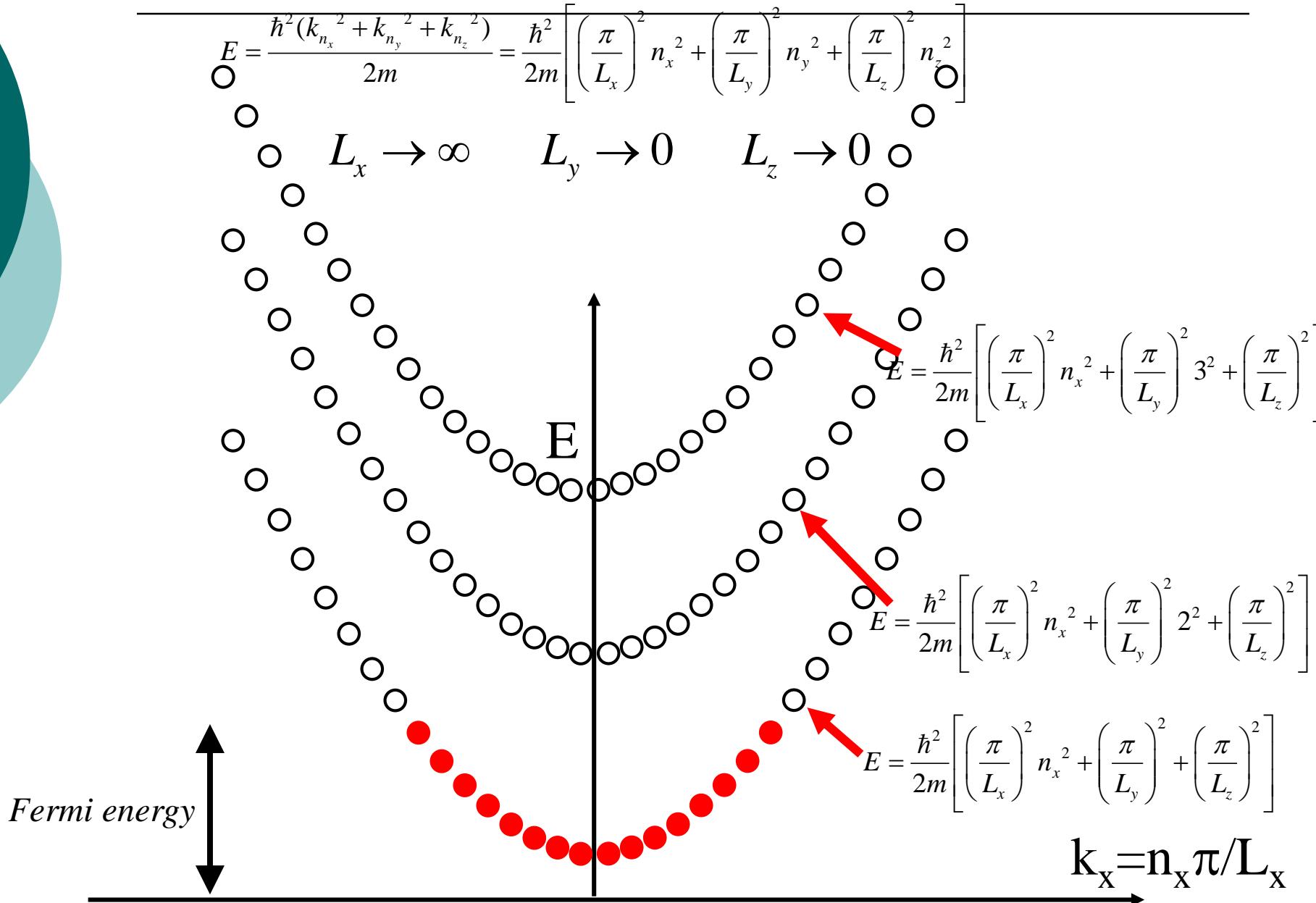
$$k_{n_y} = n_y \pi / L$$

$$k_{n_z} = n_z \pi / L$$

$$E = \frac{\hbar^2 (k_{n_x}^2 + k_{n_y}^2 + k_{n_z}^2)}{2m} = \frac{\hbar^2}{2m} \left[ \left( \frac{\pi}{L_x} \right)^2 n_x^2 + \left( \frac{\pi}{L_y} \right)^2 n_y^2 + \left( \frac{\pi}{L_z} \right)^2 n_z^2 \right]$$

These are the allowed energy levels, or “quantum states”

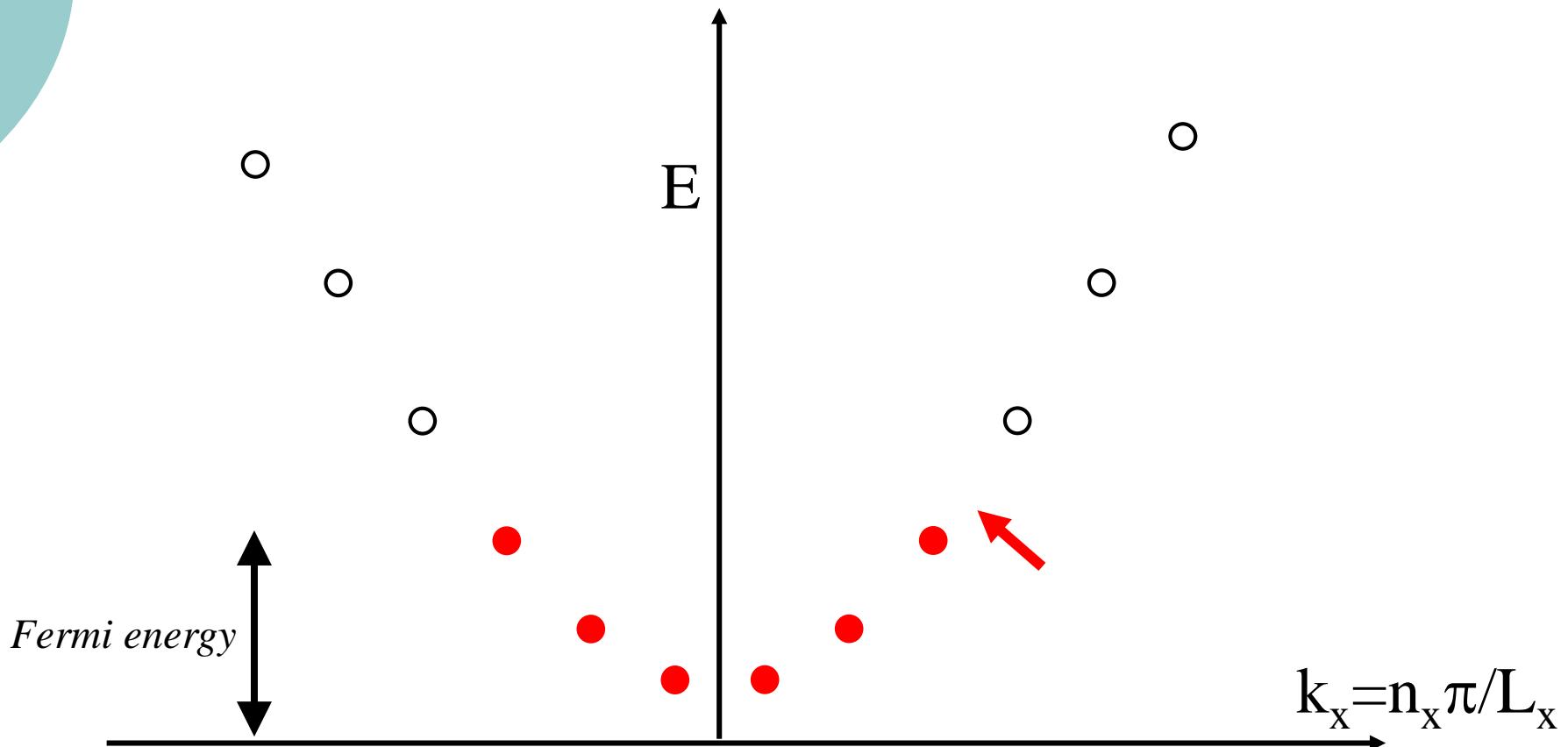
# 1d system:



# 0d system

$$E = \frac{\hbar^2(k_{n_x}^2 + k_{n_y}^2 + k_{n_z}^2)}{2m} = \frac{\hbar^2}{2m} \left[ \left( \frac{\pi}{L_x} \right)^2 n_x^2 + \left( \frac{\pi}{L_y} \right)^2 n_y^2 + \left( \frac{\pi}{L_z} \right)^2 n_z^2 \right]$$

$$L_x \rightarrow 0 \quad L_y \rightarrow 0 \quad L_z \rightarrow 0$$

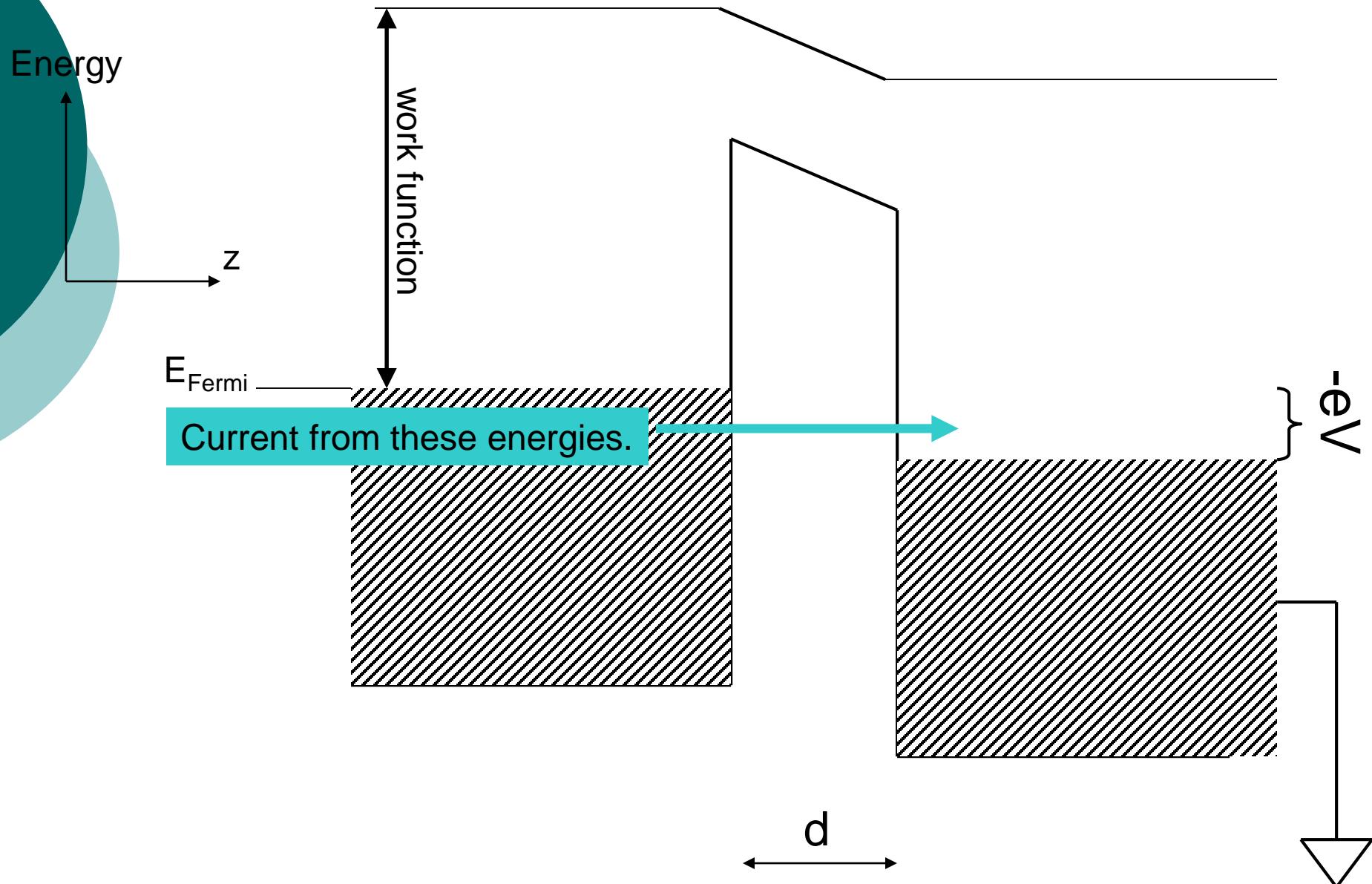


# Energy scales

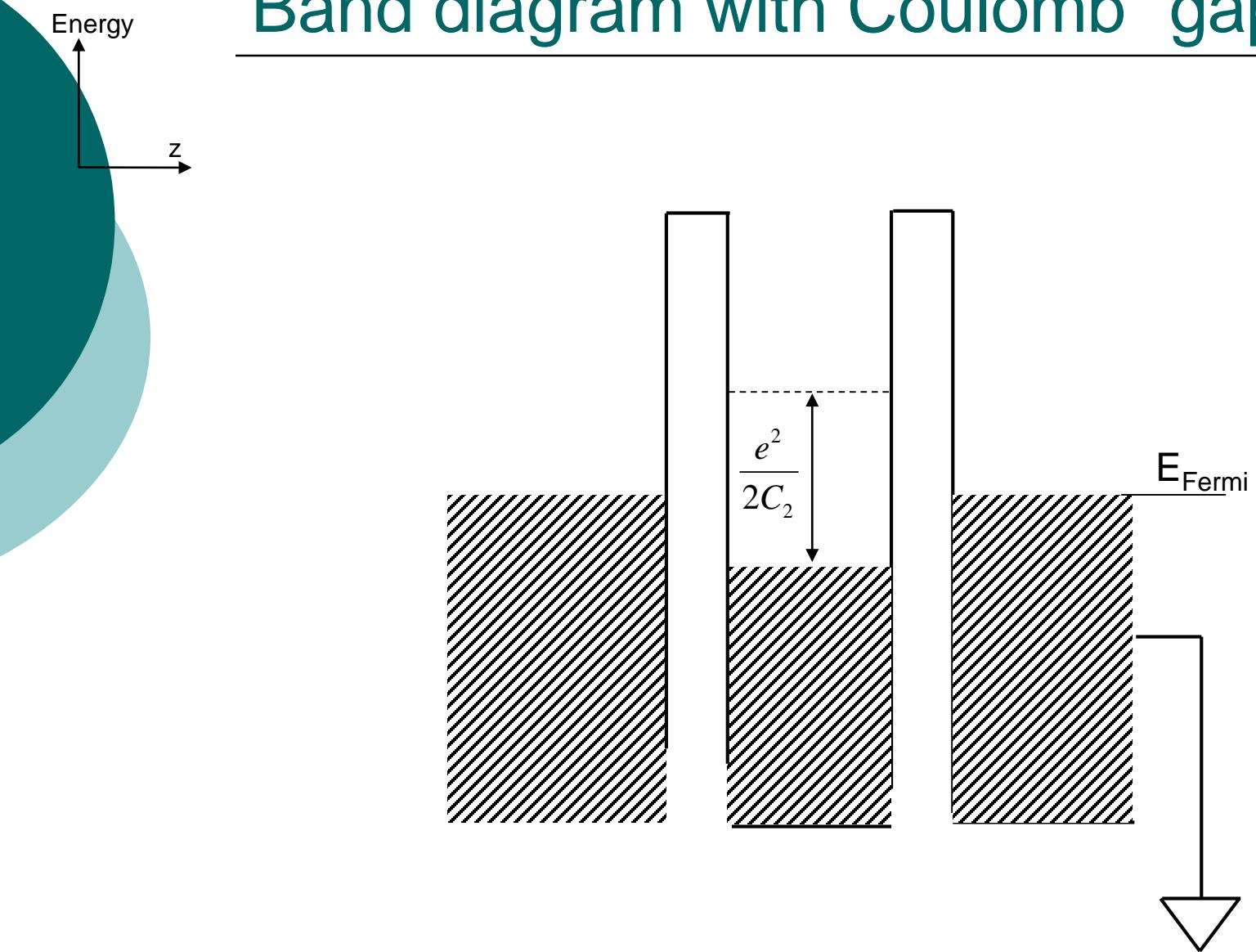
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- Charging energy
- Single electron energy level spacing
- Temperature

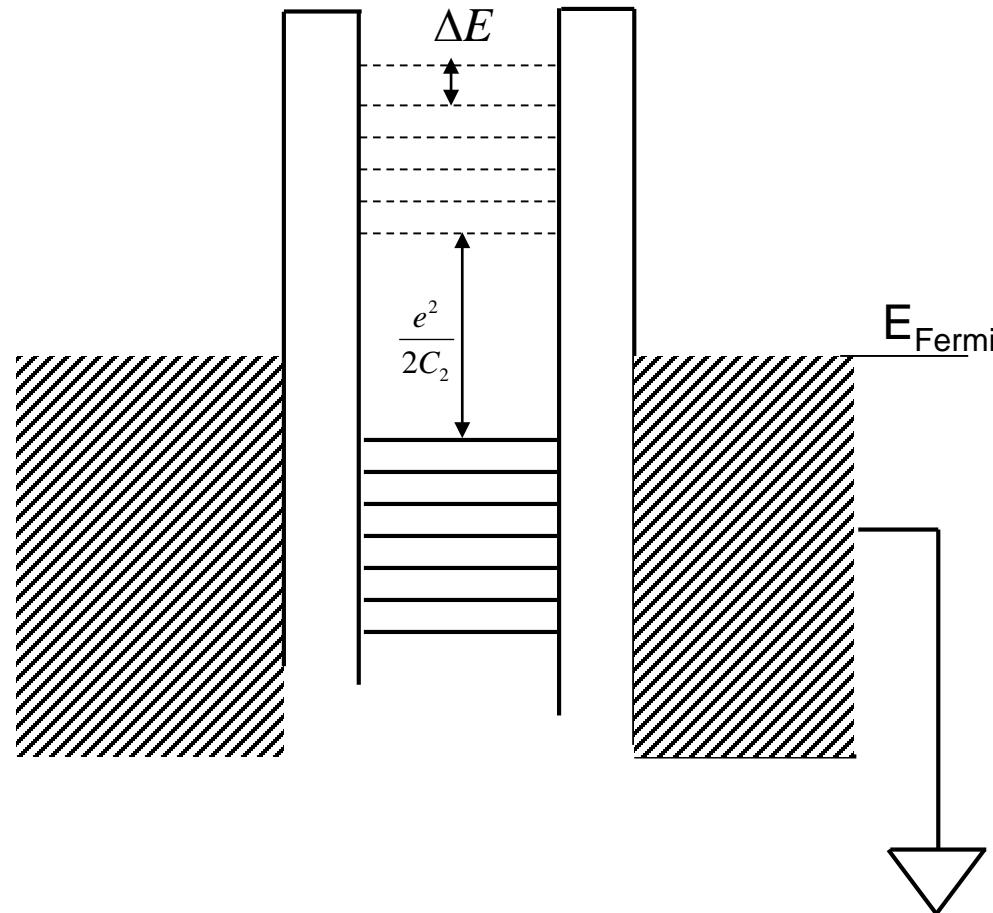
## Continuum band diagrams like this no longer apply



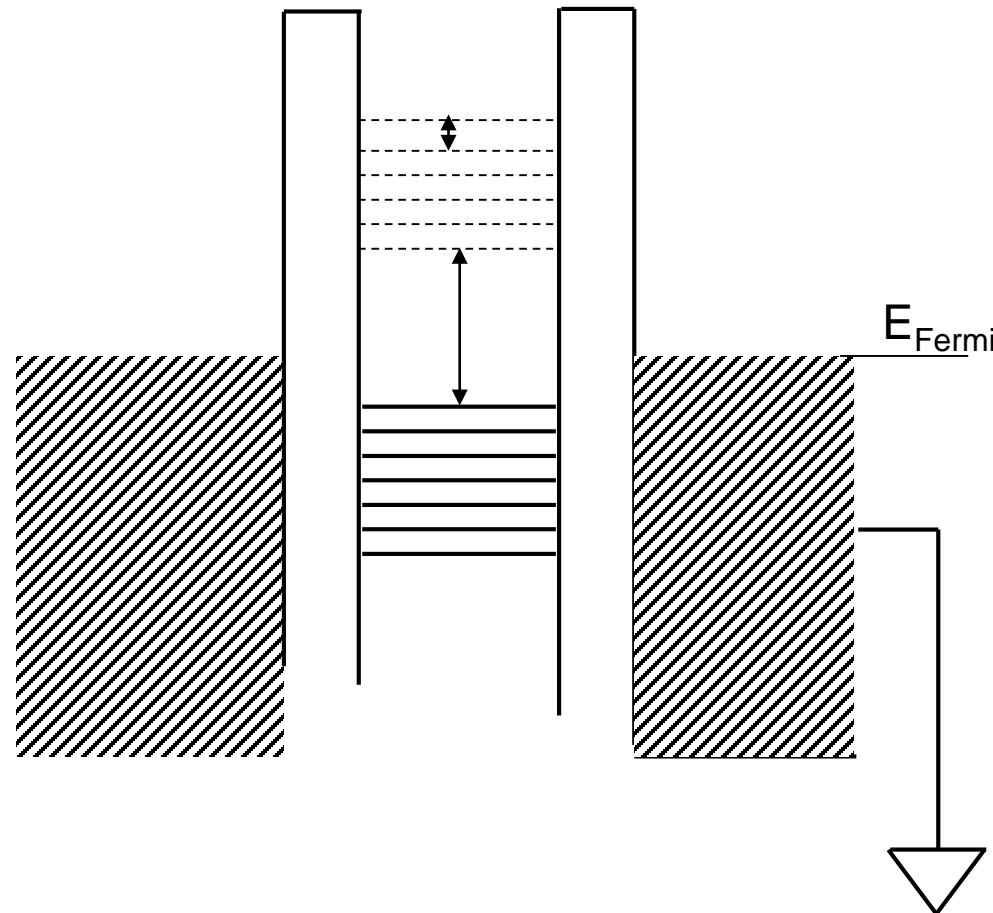
# Band diagram with Coulomb “gap”



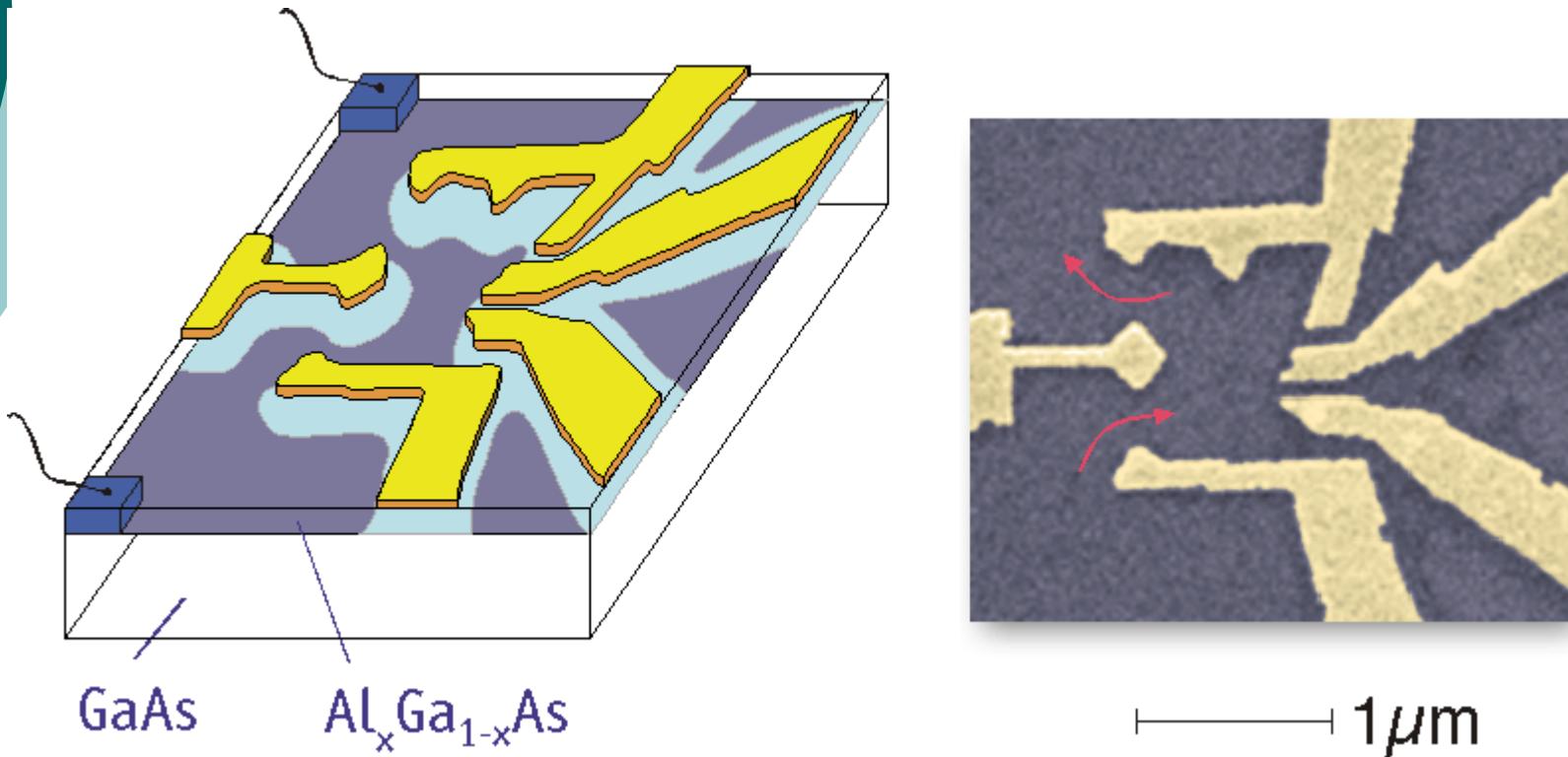
# Band diagram with Coulomb “gap” and accounting for 0d states:



# Band diagram with Coulomb “gap” and accounting for 0d states:

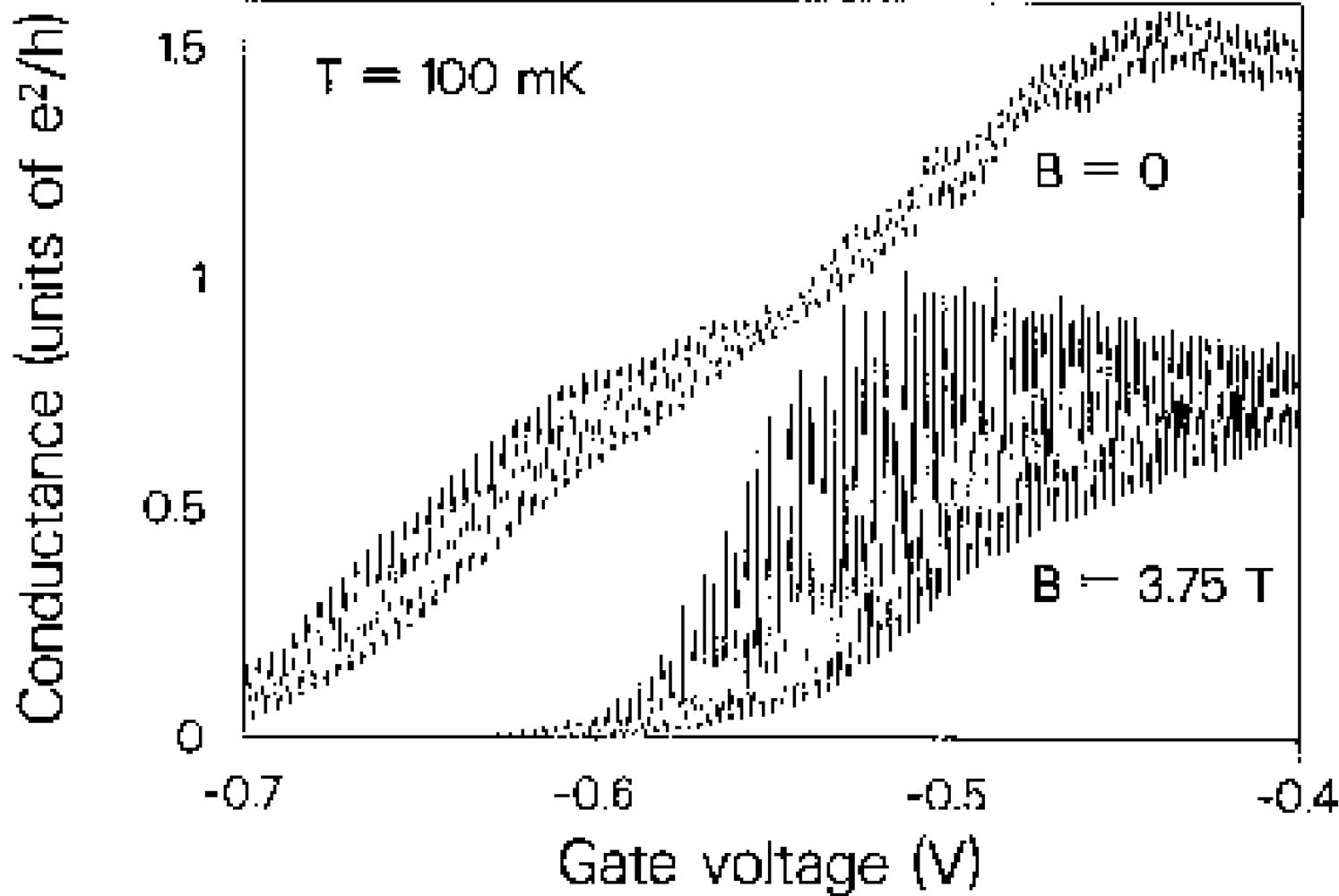


# Experimental realization w/2DEGS



- <http://marcuslab.harvard.edu/res.php>

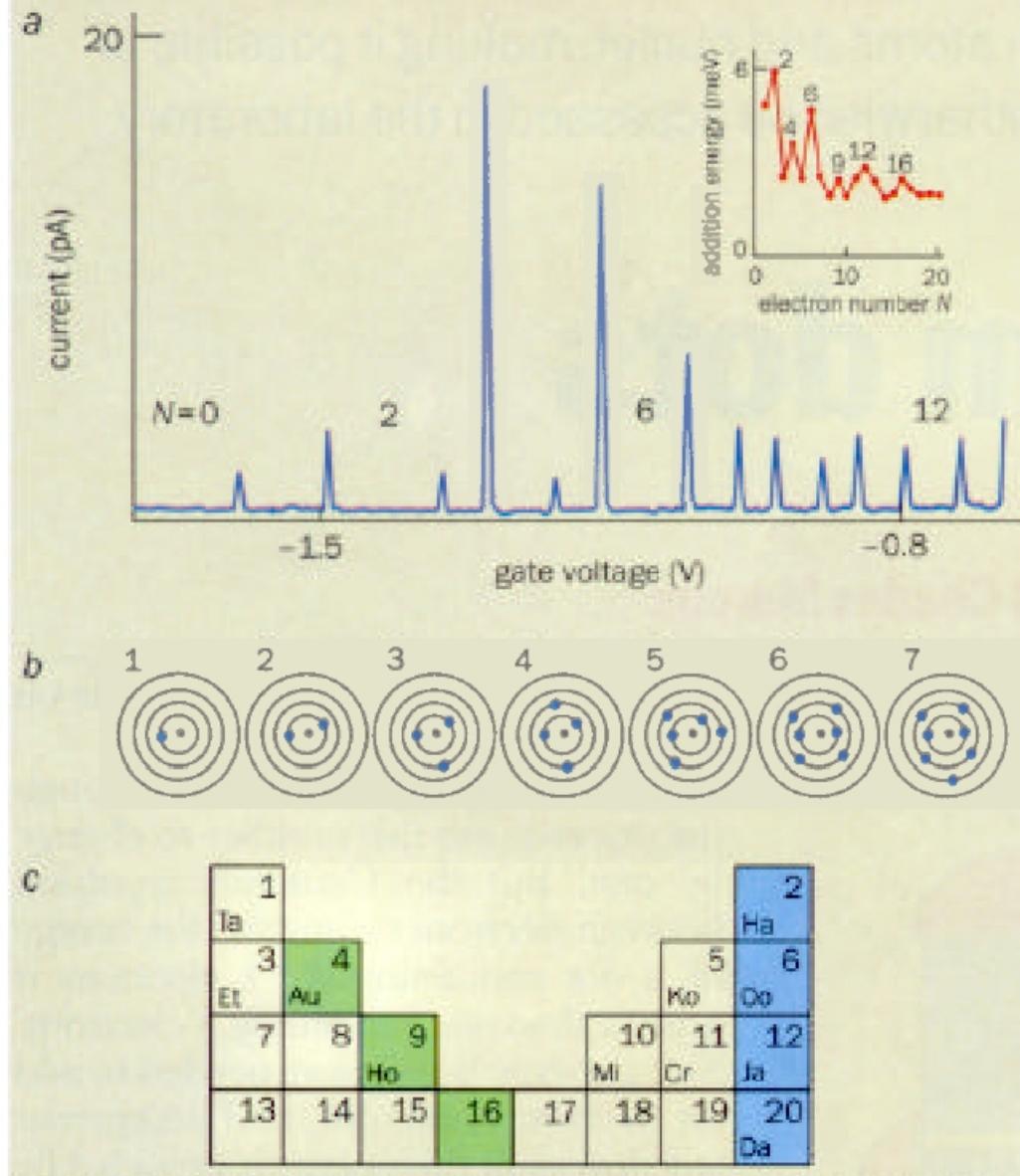
# Results



From .P. Kouwenhoven, C.M. Marcus, P.L. McEuen, S. Tarucha, R.M. Westervelt, and N.S. Wingreen  
Electron Transport in Quantum Dots  
Nato ASI conference proceedings, ed. By L. P. Kouwenhoven, G. Sch&amp;ouml;n, L.L. Sohn (Kluwer, Dordrecht, 1997)

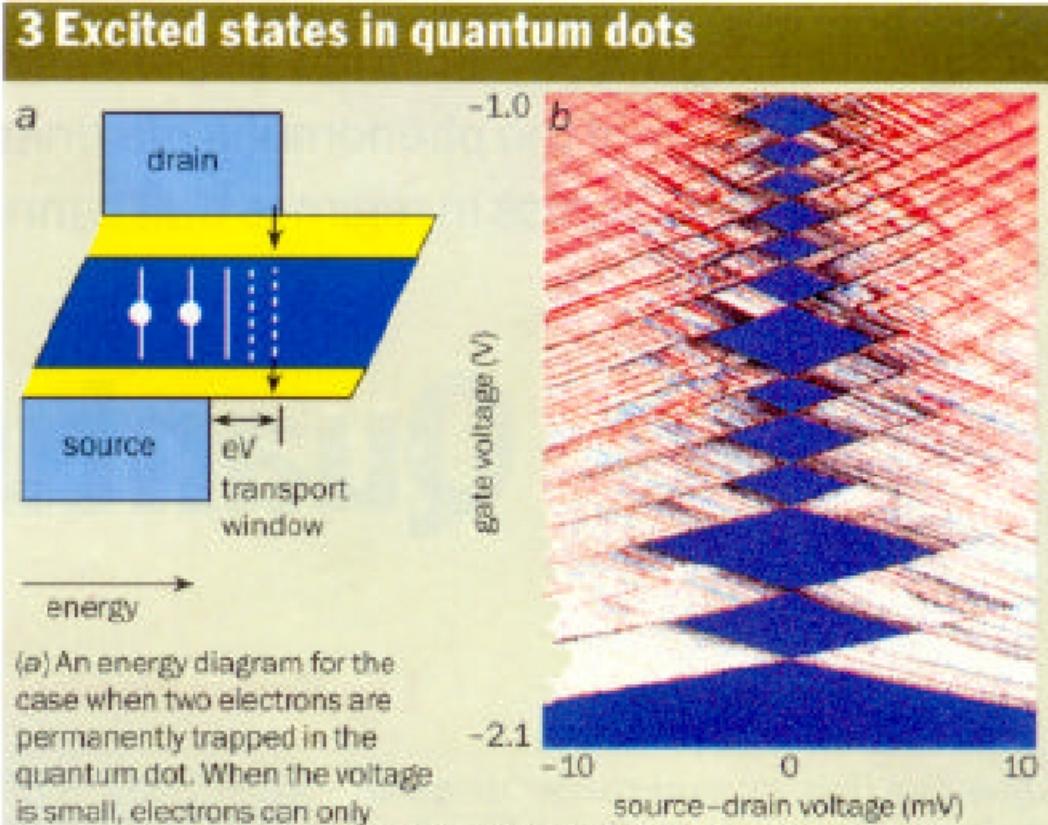
# Artificial atoms

## 2 Artificial atoms



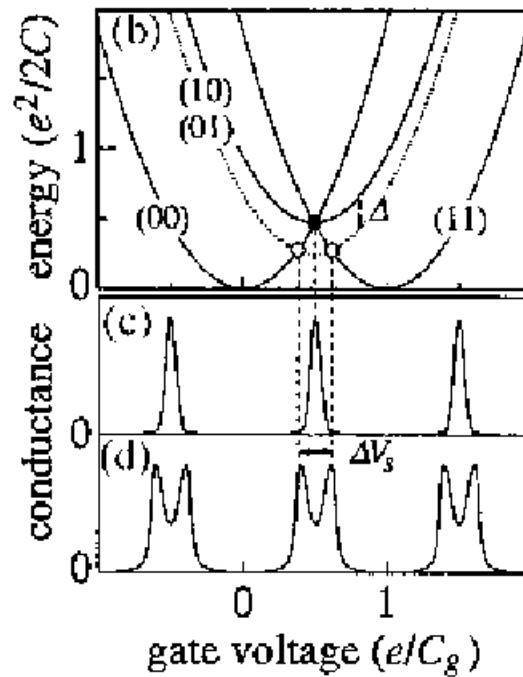
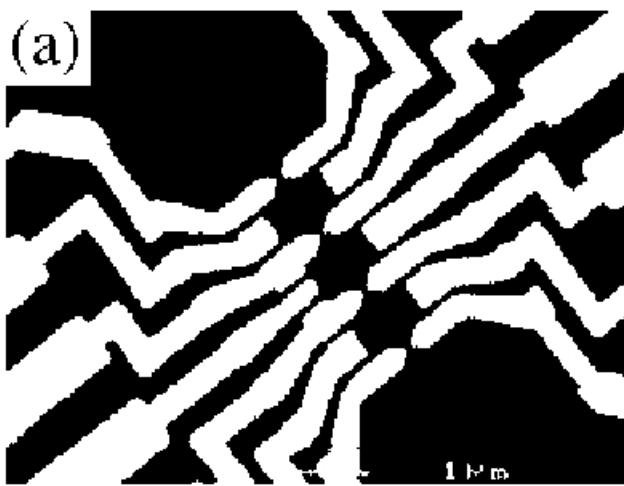
Leo Kouwenhoven and Charles Marcus  
Quantum Dots  
Physics World, June 1998

# Coulomb diamonds



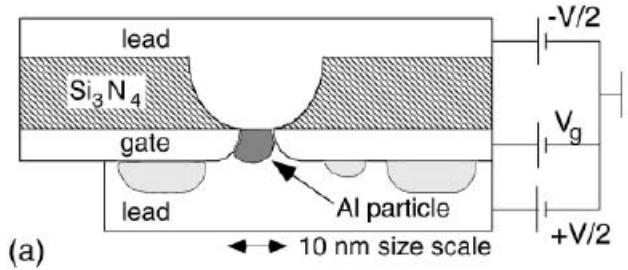
Leo Kouwenhoven and Charles Marcus  
Quantum Dots  
Physics World, June 1998

# Artificial molecules

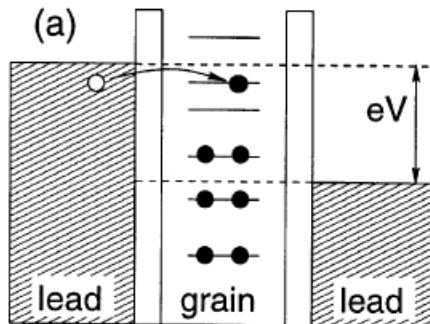


From .P. Kouwenhoven, C.M. Marcus, P.L. McEuen, S. Tarucha, R.M. Westervelt, and N.S. Wingreen  
Electron Transport in Quantum Dots  
Nato ASI conference proceedings, ed. By L. P. Kouwenhoven, G. Sch&amp;ouml;n, L.L. Sohn (Kluwer, Dordrecht, 1997)

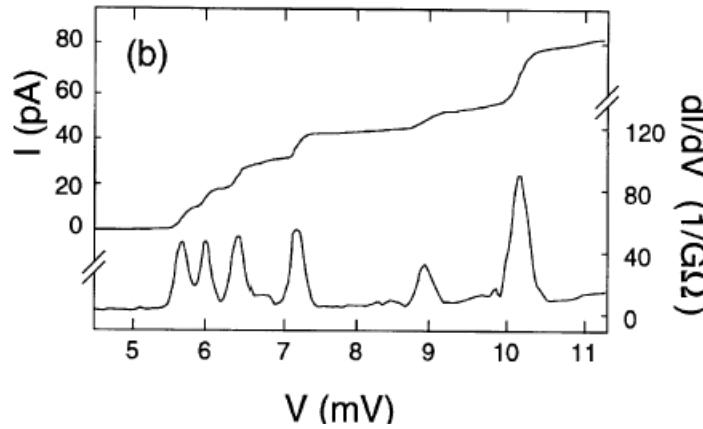
# Metallic quantum dots



(a)



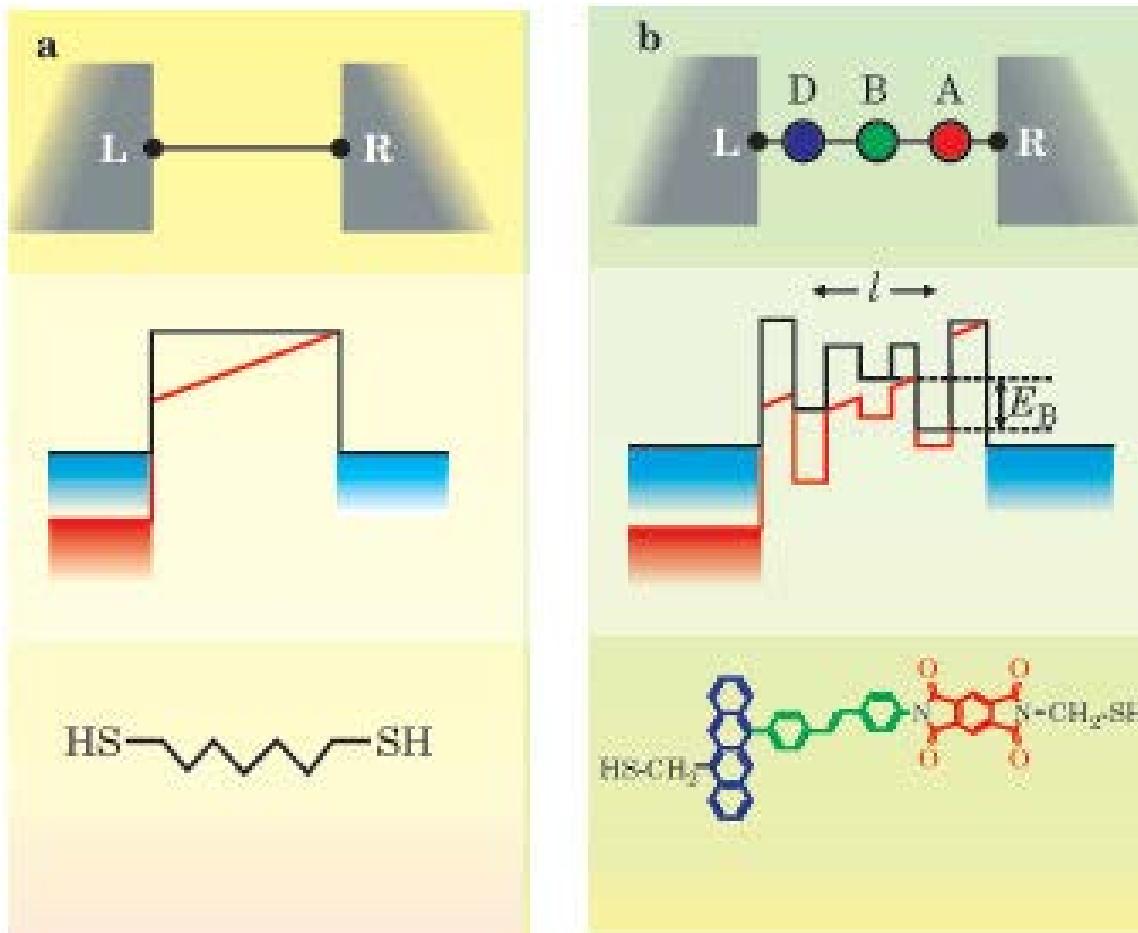
(a)



(b)

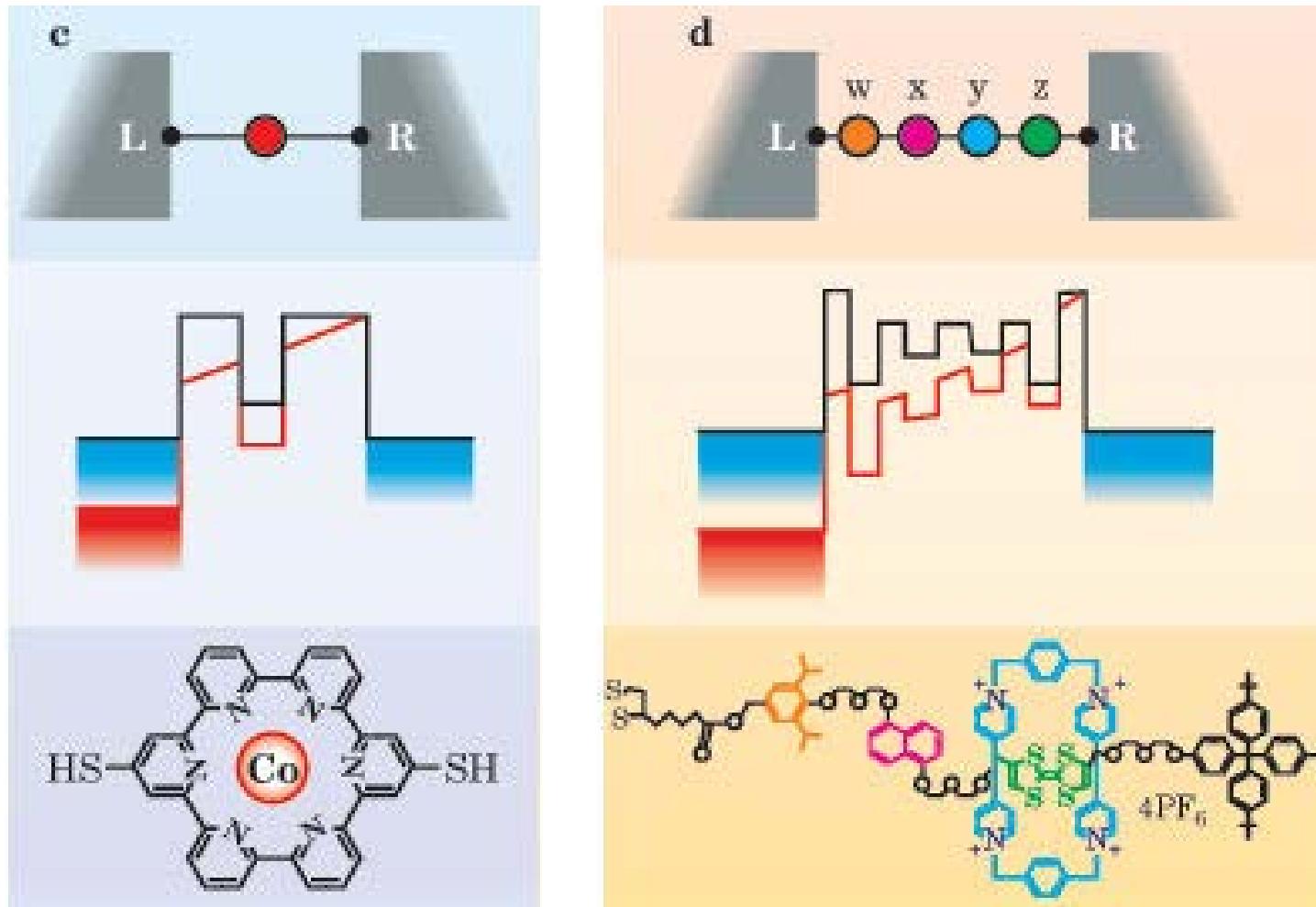
Spectroscopy of Discrete Energy Levels in Ultrasmall Metallic Grains, Jan von Delft and D. C. Ralph, [Physics Reports 345, 61 \(2001\)](#).

# Molecular electronics



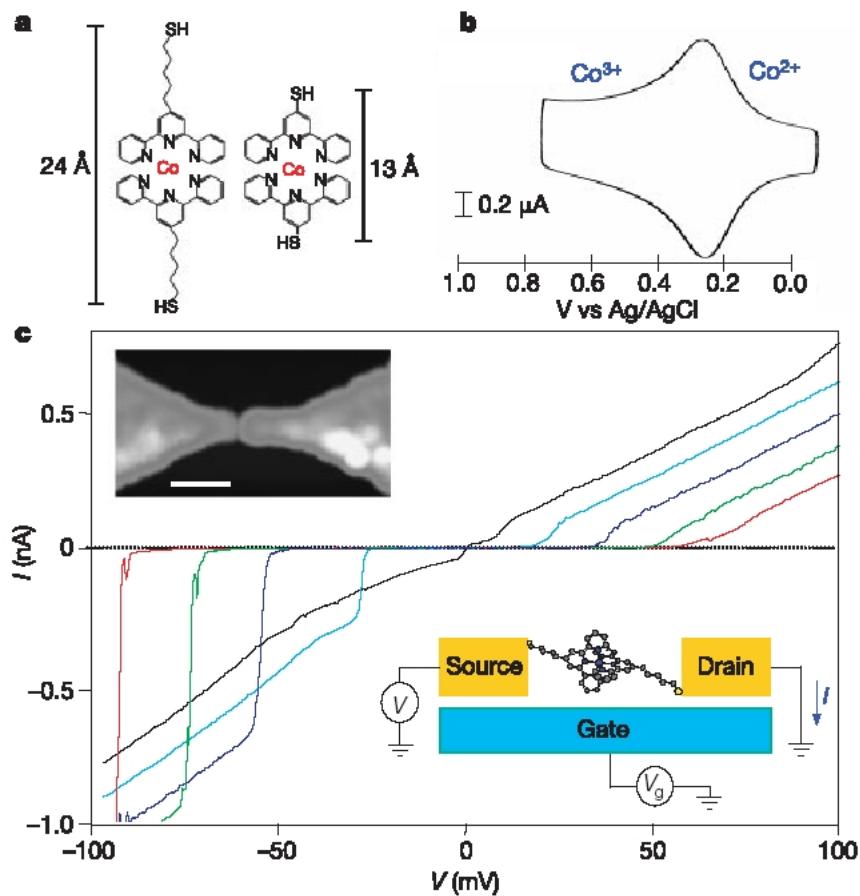
J. Heath, Physics Today, May 2003

# Molecular electronics

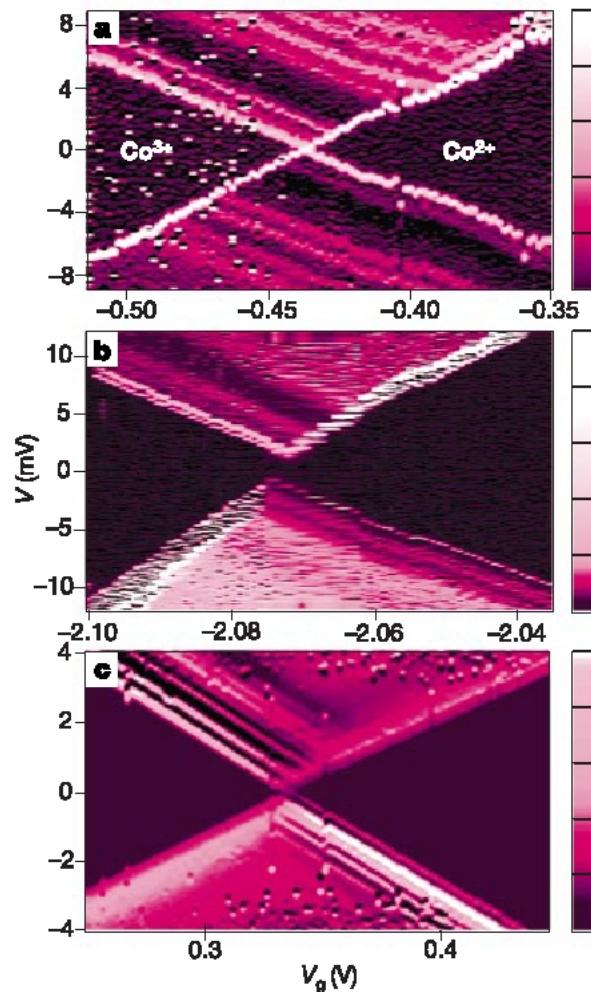


J. Heath, Physics Today, May 2003

# Molecular electronics



**Figure 1** The molecules used in this study and their electronic properties. **a**, Structure of  $[\text{Co}(\text{tpy}-\text{(CH}_2)_5\text{-SH})_2]^{2+}$  (where tpy-(CH<sub>2</sub>)<sub>5</sub>-SH is 4'-(5-mercaptopentyl)-2,2':6',2''-terpyridinyl) and  $[\text{Co}(\text{tpy-SH})_2]^{2+}$  (where tpy-SH is 4'-(mercapto)-2,2':6',2''-terpyridinyl). The scale bars show the lengths of the molecules as calculated by energy minimization.



"Coulomb blockade and the Kondo effect in single-atom transistors," Jiwoong Park, Abhay N. Pasupathy, Jonas I. Goldsmith, Connie Chang, Yuval Yaish, Jason R. Petta, Marie Rinkoski, James P. Sethna, Hector D. Abruna, Paul L. McEuen & Daniel C. Ralph, *Nature*, 417, 722-725 (2002).