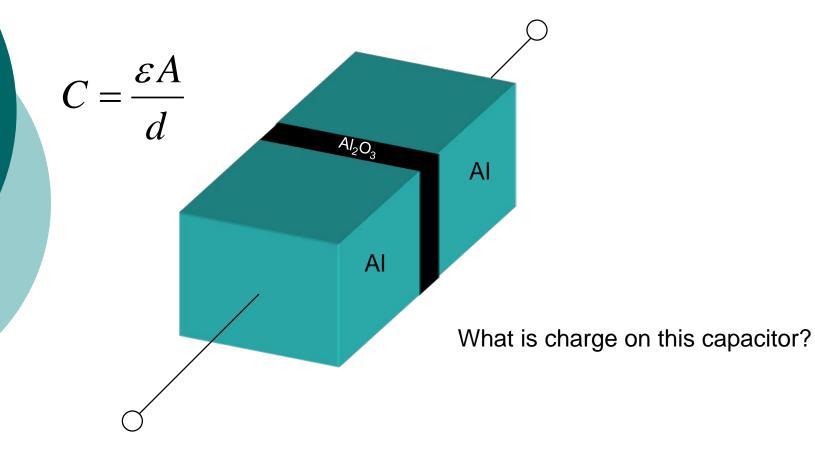
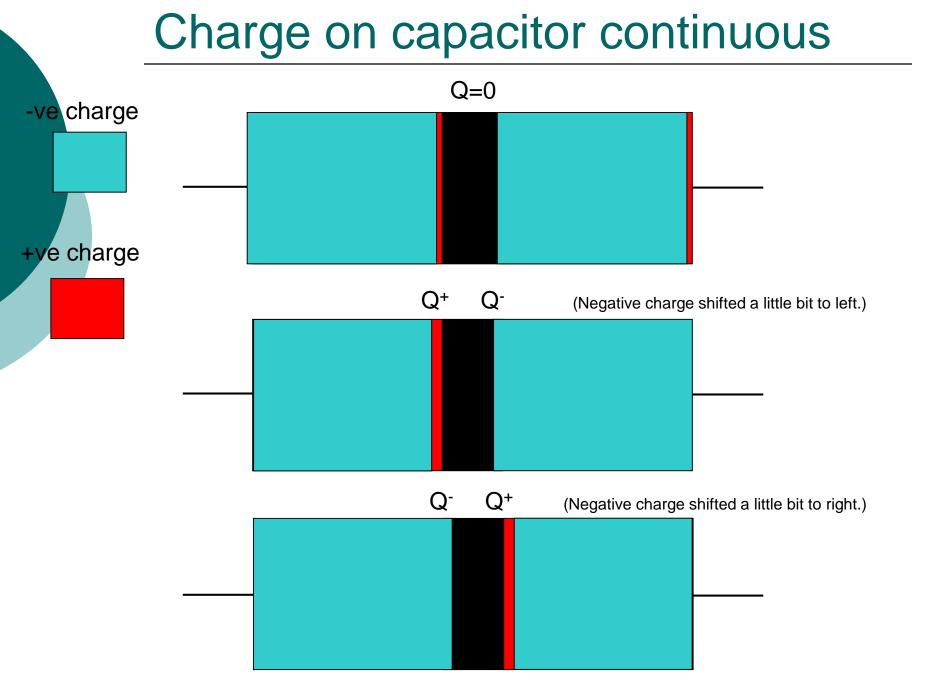
# Lecture 5: Coulomb blockade

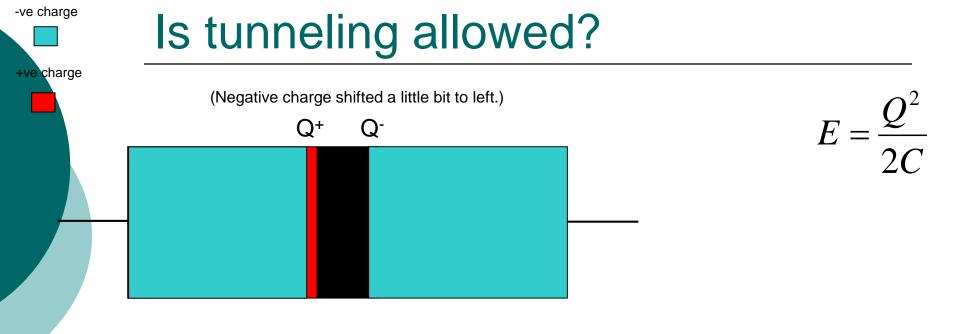


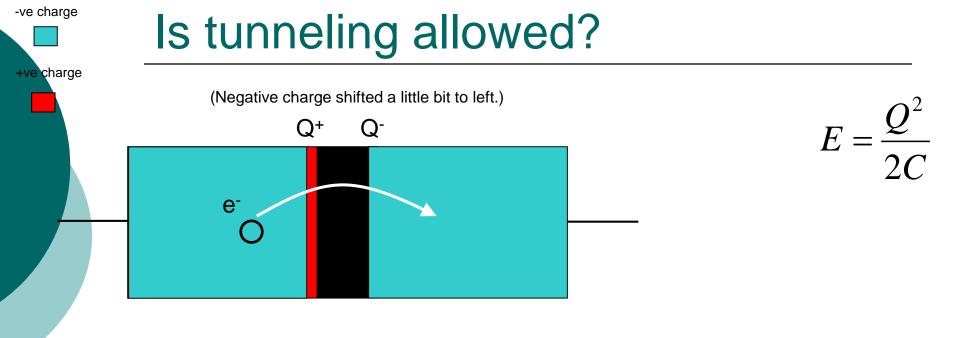
# Readings this lecture covers

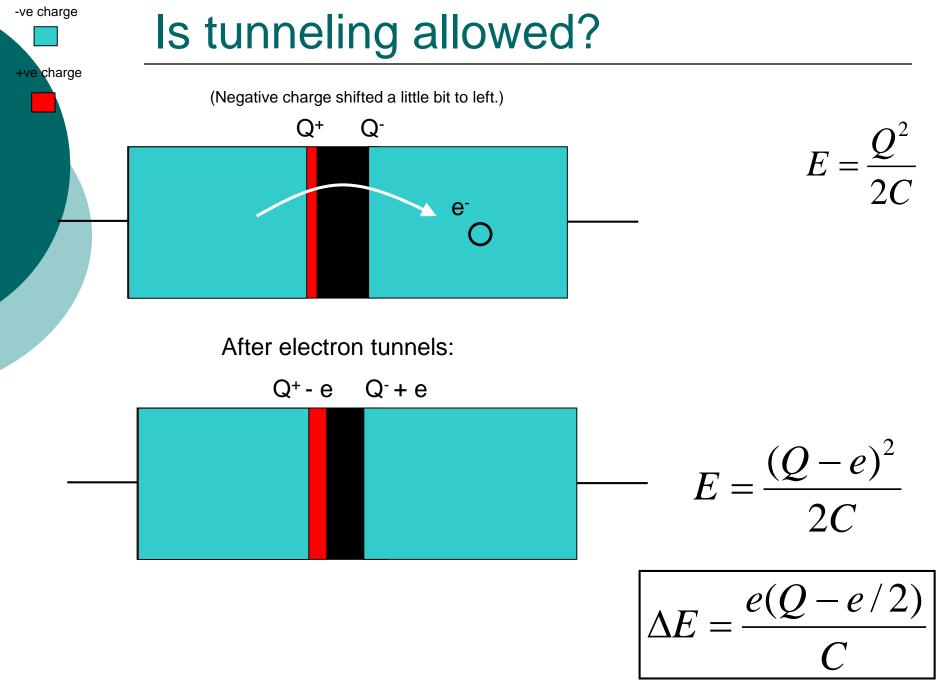
o Ferry pp. 226-244

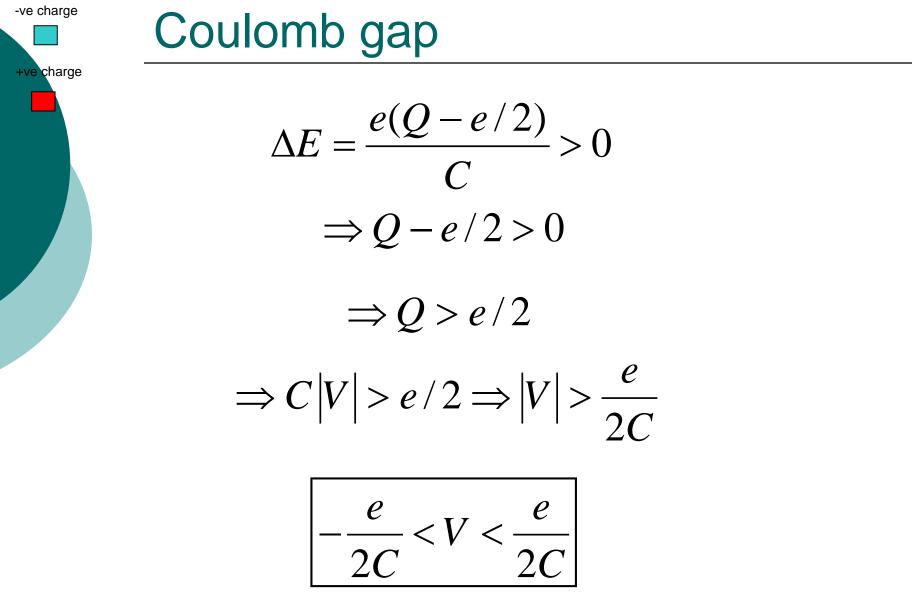
- o Hanson, pp. 212-244
- Cleland PRL, PRB (reading packet)
- Devoret chapter in Single Charge Tunneling (reading packet)
- Grabert chapter (reading packet)
- These chapters are covered all the way to (and including) lecture 8





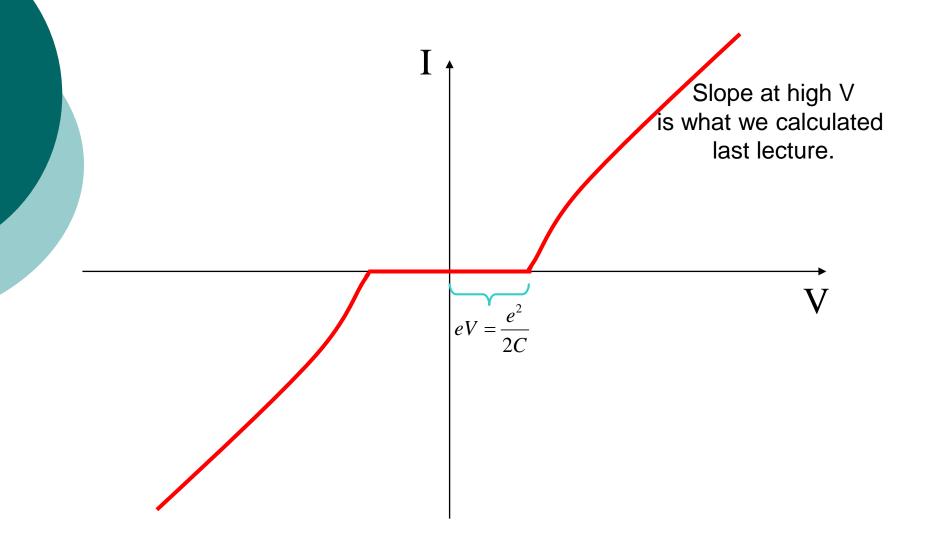






Tunneling only under these conditions, *otherwise no tunneling!* 

### I-V curve

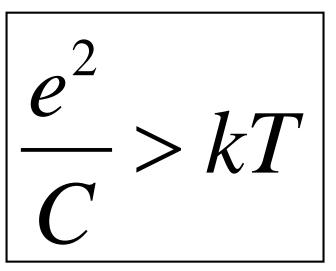


## Temperature

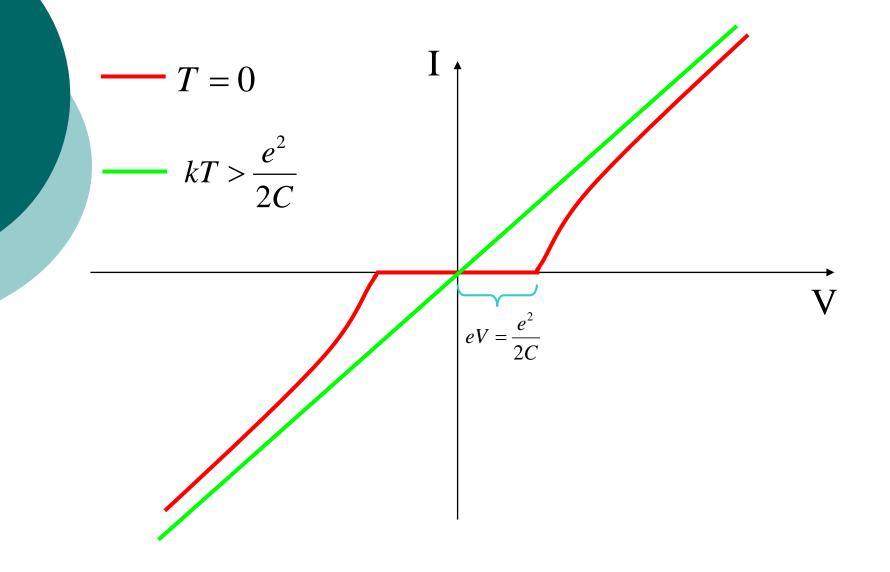
$$\Delta E = \frac{e(Q - e/2)}{C}$$

can be less than 0 if thermal energy available

Criteria to observe coulomb gap behavior:



#### I-V curve vs. temperature



# Numbers

Class demo: 1 nm barrier, 1 mm x 1 mm junction:

$$C = \frac{\varepsilon A}{d} = \frac{10 \cdot 8.85 \cdot 10^{-12} \, F \, / \, m (10^{-3} \, m)^2}{10^{-9} \, m} \approx 10^{-7} \, F$$
$$\frac{e^2}{C} > kT \implies T < \frac{e^2}{Ck} = \frac{(1.6 \cdot 10^{-19} \, coulomb)^2}{10^{-7} \, F \cdot 1.38 \cdot 10^{-23} \, J \, / \, K} \approx 10^{-8} \, K$$

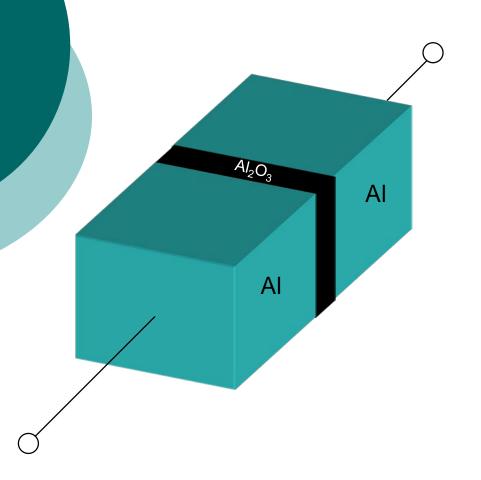
Practically impossible.

Best lithographic junction: 1 nm barrier, 100 nm x 100 nm junction:

$$C \approx 10^{-15} F \Longrightarrow T < 1K$$

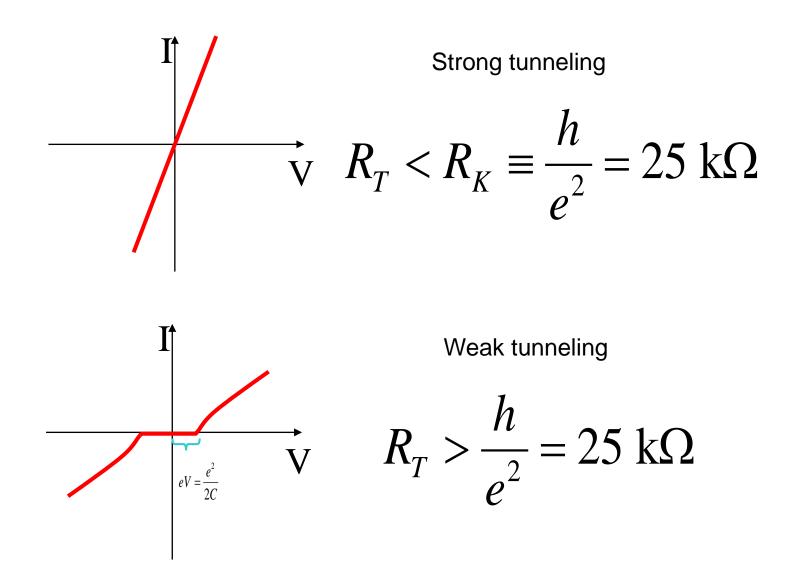
Possible to achieve in the lab.

# Quantum mechanics

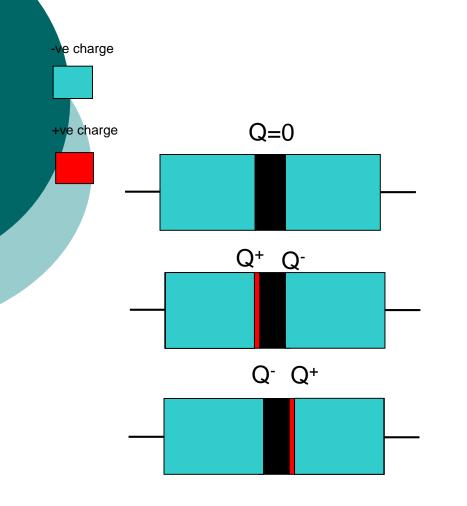


- For strong tunneling, electron can have a large probability to be on both sides at the same time.
- This means the system energy cannot be defined by localizing the electron on only one side.
- This makes coulomb blockade irrelevant.

# I-V curve vs. tunnel strength

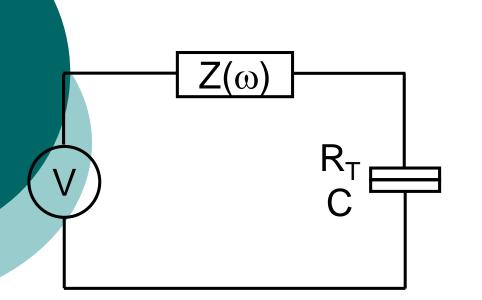


#### Charge on capacitor is a quantum variable



- We don't always know what Q is.
- Treating Q as a quantum variable, there is a certain probability for the system to have a certain value of Q.
- Should describe a "wave function" for Q: Ψ(Q) just like wave function for position Ψ(x)
- Now, we need quantum theory of electric circuits.

# Quantum theory of electric circuits



- At DC, can have current bias or voltage bias depending on Z(dc) vs. R<sub>T</sub>.
- At AC, almost always have Z(ω) < R<sub>T</sub> because of lead capacitance (typically pF).

Full quantum treatment beyond the scope of this class.

In order to see Coulomb blockage,

need current bias all the way up to  $1/(R_{K}C)$  which is typically 10 GHz, i.e.:

$$Z(\omega) > R_T$$
 for all  $\omega \le \frac{1}{R_K C} \sim 10 \text{ GHz}$ 

**Requirements for Coulomb blockade** 

# $okT < e^2/C$ (hard) $OR_T > R_K (25 k\Omega)$ (harder) $oZ(\omega) > R_{T}$ at all frequencies up to $1/R_{K}C$ (hardest)

Achieved by Cleland PhD thesis, Berkeley 1992. (Congratulations, Andrew.)