

**PROBLEM 1: (10 points) BITCOIN MINING**

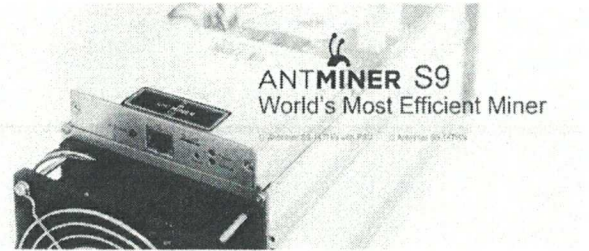
What is the hourly profit or loss if you spend money only on electricity with the Antminer S9 to mine bitcoin? Show your work!

Hourly income (mining) = ¢ 36 (2)

Hourly cost (electricity) = ¢ 22.1 (2)

Hourly profit/loss (circle profit or loss) = ¢ 13.9 (2)

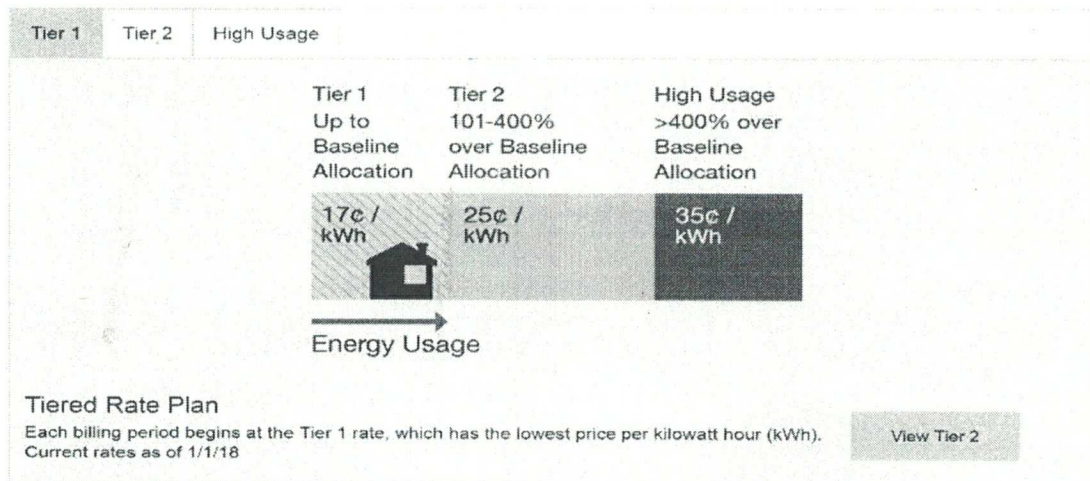
- Hash Rate 13TH/s (this is a measure of the number of hash “computations” per second the S9 can perform). Recall T=tera= $10^{12}$



- **Power Consumption 1300W**

- Assume **Bitcoin Value of 10000\$**

Shown below is the Southern California Edison rate for electricity, current as of 5/1/2018. Assume your household is frugal with electricity usage, so you are in Tier 1.



I will calculate the number of hashes it takes to mine 1 bitcoin for you: The global hash rate (the combined computational capability of all active mining computers in the world) as of 5/1/2018 is 28,791,021,184 GH/s. # hashes to mine 1 bitcoin = global hash rate times ten minutes / 25 =  $(28,791,021,184 * 10^9 \text{ H/s}) * (60 \text{ sec/min}) 10 \text{ min} / 25 = (2.9 * 6/1.25) * 10^{(10+9+1+1-1)} = \text{approx. } 1.3 * 10^{21}$ .

**So:**  $1.3 * 10^{21}$  hashes earns one bitcoin. Use this to determine how many bitcoins per second the Antminer S9 mines, based on its hash rate of 13 TH/s. (H=hash T=Tera)

The electricity cost should be calculated based on the Antminer S9 power consumption of 1300 W.

**PROBLEM 1:**

Hourly income %

$$\text{Antminer Processing Speed} = 13 \frac{\text{TH}}{\text{s}} = 13 \times 10^{12} \frac{\text{H}}{\text{s}}$$

$$1 \text{ bitcoin} = 1.3 \times 10^{21} \text{ H}$$

$$\text{Antminer bitcoin earning rate} = \frac{13 \times 10^{12}}{1.3 \times 10^{21}} \frac{\text{bitcoin}}{\text{s}} = 10^{-8} \frac{\text{bitcoin}}{\text{s}} \textcircled{2}$$

$$\text{Bitcoin earned per hour} = 10^{-8} \times 60 \times 60 = 3.6 \times 10^{-5} \textcircled{2}$$

$$\text{Hourly income} = 3.6 \times 10^{-5} \times 10^4 \text{ \$} = 3.6 \times 10^{-5} \times 10^6 \text{ ¢} = 36 \text{ ¢}$$

Hourly Cost

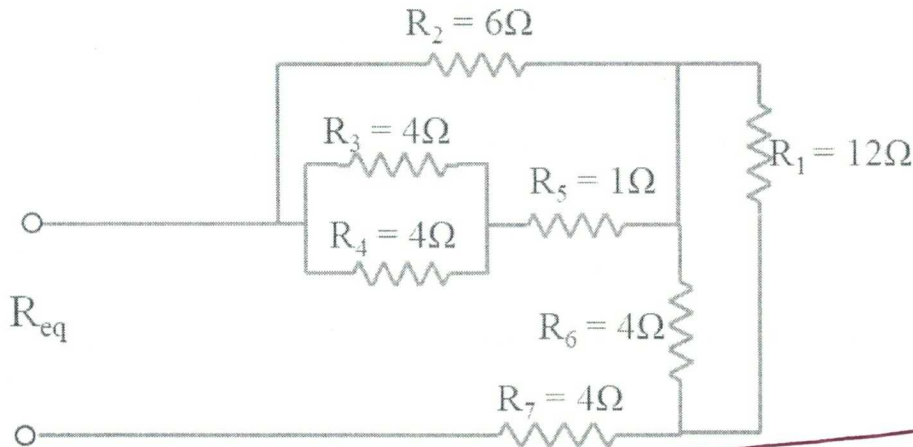
$$= 1.3 \text{ kW} \times \frac{17 \text{ ¢}}{\text{kWh}} = 22.1 \frac{\text{¢}}{\text{hour}}$$

$$\text{Hourly Cost} = 22.1 \text{ ¢}$$

$$\text{Hourly Profit} = 36 \text{ ¢} - 22.1 \text{ ¢} = 13.9 \text{ ¢}$$

**PROBLEM 2: (10 points)**

Find  $R_{eq}$ :



$R_2 = 6\Omega$   
 $R_3 || R_4 = 2\Omega$      $R_5 = 1\Omega$   
 $R_1 || R_6 = 3\Omega$   
 $R_7 = 4\Omega$

understanding  $R_3$  is Parallel with  $R_4$  (2)  
 //  $R_1$  is // //  $R_6$  (2)

understanding  $R_3 || R_4$  is in series with  $R_5$   
 $(R_3 || R_4) + R_5 = 3\Omega$  (2)

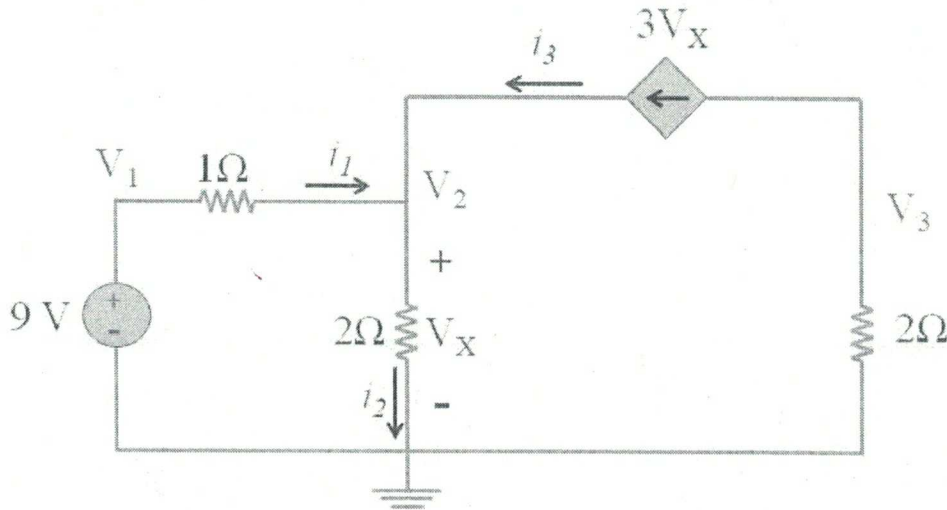
understanding  $R_2$  is in Parallel with  $[(R_3 || R_4) + R_5]$   
 $R_2 || [(R_3 || R_4) + R_5] = 2\Omega$  (2)

$6 || 3 = 2\Omega$

$R_{eq} = 2\Omega + 3\Omega + 4\Omega = 9\Omega$   
 Final Answer (2)

**PROBLEM 3: (40 points)**

Use nodal analysis to find  $V_1$  through  $V_3$  and  $i_1$  through  $i_3$ :



a) What is the value of  $V_1$  (2pts)

$V_1 = 9V$  (2)

b) KCL Equations (20pts)

Write KCL @ Node  $V_2$  to find an equation in terms of the unknown nodal voltages of  $V_1$  through  $V_3$  (10pts)

①  $i_1 + i_3 = i_2 \rightarrow \frac{V_1 - V_2}{1} + 3V_X = \frac{V_2}{2}$

$V_X = V_2 \Rightarrow \frac{V_1 - V_2}{1} + 3V_2 = \frac{V_2}{2} \rightarrow V_1 + 1.5V_2 = 0$

understanding  $V_X = V_2$

(2)

or  $9 + 1.5V_2 = 0$   
or  $V_2 = -6V$

(7)

Write KCL @ Node  $V_3$  to find an equation in terms of the unknown nodal voltages of  $V_1$  through  $V_3$  (10pts)

$$3V_2 + \frac{V_3}{2} = 0 \rightarrow 3V_2 + \frac{V_3}{2} = 0 \quad (10)$$

$$\Rightarrow V_3 = -6V_2 = +36V$$

c) Solve  $V_1$  to  $V_3$  (3pts)

$V_1$	9V	(1)
$V_2$	-6V	(1)
$V_3$	+36V	(1)

d) Find expressions for currents  $i_1$ ,  $i_2$  and  $i_3$  in terms of  $V_1$  through  $V_3$  (12pts)

$i_1$	$\frac{V_1 - V_2}{1}$	(4)
$i_2$	$\frac{V_2}{2}$	(4)
$i_3$	$3V_2$ or $-\frac{V_3}{2}$	(4)

$$i_1 = \frac{V_1 - V_2}{1}$$

$$i_2 = \frac{V_2}{2}$$

$$i_3 = 3V_2 \text{ or } i_3 = -\frac{V_3}{2}$$

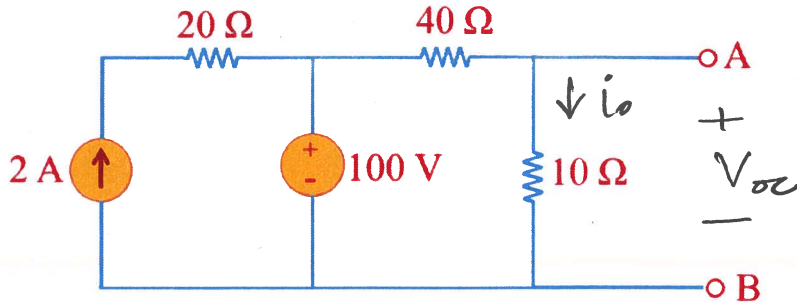
e) Solve  $i_1$  through  $i_3$  (3pts)

$i_1$	15 A	①
$i_2$	-3 A	①
$i_3$	-18 A	①

**PROBLEM 4:** (points) **30**

Find the Thevenin equivalent circuit at terminals AB by finding  $V_{oc}$  and  $I_{sc}$ .

$V_{oc} \equiv V_{ab}(\text{open})$   $I_{sc} \equiv I_{ab}(\text{short } a \text{ to } b)$



10	$V_{oc}$	20V
10	$I_{sc}$	2.5A
4	$V_{Th}$	20V
6	$R_{Th}$	8Ω

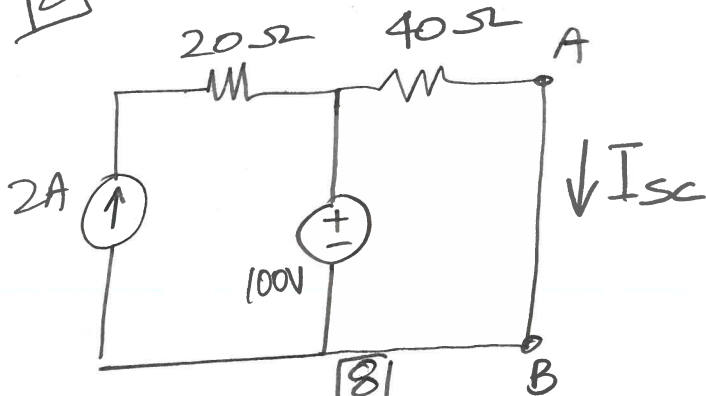
\* Method 1 for  $V_{oc}$  (voltage divider): Method 3: nodal analysis, 2 for each eqn.

$$V_{oc} = 100 \cdot \frac{10}{50} = 20V$$

\* Method 2 for  $V_{oc}$  (KVL):

$$-100 + 50i_o = 0 \Rightarrow i_o = 2A$$

$$V_{oc} = 10 \cdot i_o = 20V$$

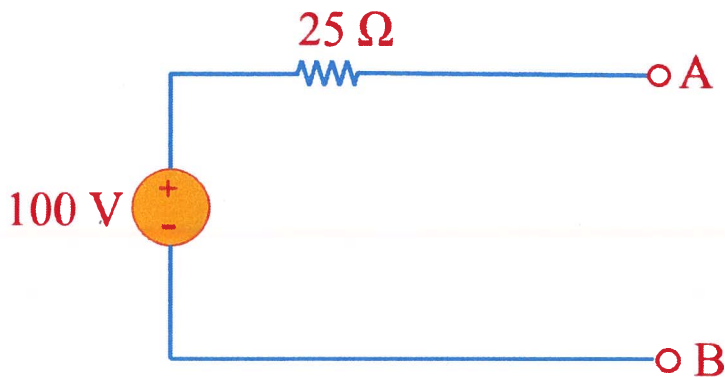


$$-100 + 40I_{sc} = 0 \Rightarrow I_{sc} = 2.5A$$

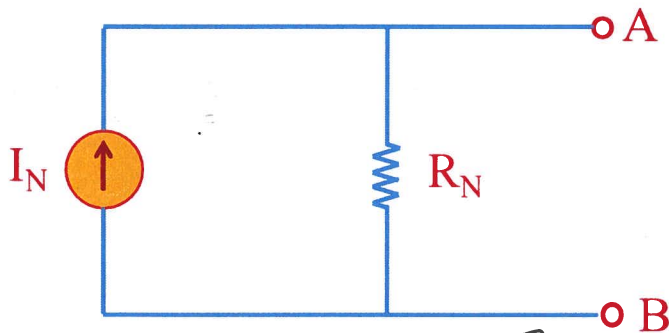
$$R_{Th} = \frac{V_{oc}}{I_{sc}} = \frac{20}{2.5} = 8\Omega$$

**PROBLEM 5: (10 points)**

Find the Norton equivalent circuit at terminals AB by using the given Thevenin circuit. ~~Find the Norton equivalent circuit at terminals AB by using the given Thevenin circuit.~~



$I_N$	4 A
$R_N$	25 $\Omega$



$$R_N = R_{Th}$$

$$I_N = V_{Th} / R_{Th}$$

$$I_N = \frac{V_{Th} \boxed{4}}{R_{Th}} = \frac{100}{25} = \boxed{2} \} \text{ 4A } \text{ (6)}$$

$$R_N = R_{Th} = 25 \Omega \} \text{ (4)}$$